

P2

No. 3

P121**C₂**UNIQUE AXIS *b***Generators selected** (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; (2)**General position**

Multiplicity,
Wyckoff letter,
Site symmetry

2 *e* 1**Coordinates**(1) x,y,z (2) \bar{x},\bar{y},\bar{z} **I Maximal *translationengleiche* subgroups**[2] $P1$ (1) 1**II Maximal *klassengleiche* subgroups****• Enlarged unit cell**[2] $\mathbf{b}' = 2\mathbf{b}$
 $P12_1$ (4) $\langle 2 + (0,1,0) \rangle$
 $P12_1$ (3) $\langle 2 \rangle$
 $\mathbf{a}, 2\mathbf{b}, \mathbf{c}$
 $\mathbf{a}, 2\mathbf{b}, \mathbf{c}$
[2] $\mathbf{c}' = 2\mathbf{c}$
 $P12_1$ (3) $\langle 2 \rangle$
 $P12_1$ (3) $\langle 2 + (0,0,1) \rangle$
 $\mathbf{a}, \mathbf{b}, 2\mathbf{c}$
 $\mathbf{a}, \mathbf{b}, 2\mathbf{c}$
 $0, 0, 1/2$
[2] $\mathbf{a}' = 2\mathbf{a}$
 $P12_1$ (3) $\langle 2 \rangle$
 $P12_1$ (3) $\langle 2 + (1,0,0) \rangle$
 $2\mathbf{a}, \mathbf{b}, \mathbf{c}$
 $2\mathbf{a}, \mathbf{b}, \mathbf{c}$
 $1/2, 0, 0$
[2] $\mathbf{a}' = 2\mathbf{a}$, $\mathbf{c}' = 2\mathbf{c}$
 $B12_1$ (3, $P12_1$) $\langle 2 \rangle$
 $B12_1$ (3, $P12_1$) $\langle 2 + (0,0,1) \rangle$
 $\mathbf{a} - \mathbf{c}, \mathbf{b}, 2\mathbf{c}$
 $\mathbf{a} - \mathbf{c}, \mathbf{b}, 2\mathbf{c}$
 $0, 0, 1/2$
[2] $\mathbf{a}' = 2\mathbf{a}$, $\mathbf{b}' = 2\mathbf{b}$
 $C12_1$ (5) $\langle 2 \rangle$
 $C12_1$ (5) $\langle 2 + (1,0,0) \rangle$
 $2\mathbf{a}, 2\mathbf{b}, \mathbf{c}$
 $2\mathbf{a}, 2\mathbf{b}, \mathbf{c}$
 $1/2, 0, 0$
[2] $\mathbf{b}' = 2\mathbf{b}$, $\mathbf{c}' = 2\mathbf{c}$
 $A12_1$ (5, $C12_1$) $\langle 2 \rangle$
 $A12_1$ (5, $C12_1$) $\langle 2 + (0,0,1) \rangle$
 $2\mathbf{c}, 2\mathbf{b}, -\mathbf{a} - 2\mathbf{c}$
 $2\mathbf{c}, 2\mathbf{b}, -\mathbf{a} - 2\mathbf{c}$
 $0, 0, 1/2$
[2] $\mathbf{a}' = 2\mathbf{a}$, $\mathbf{b}' = 2\mathbf{b}$, $\mathbf{c}' = 2\mathbf{c}$
 $F12_1$ (5, $C12_1$) $\langle 2 \rangle$
 $F12_1$ (5, $C12_1$) $\langle 2 + (1,0,0) \rangle$
 $2\mathbf{a}, 2\mathbf{b}, -\mathbf{a} + \mathbf{c}$
 $2\mathbf{a}, 2\mathbf{b}, -\mathbf{a} + \mathbf{c}$
 $1/2, 0, 0$
[3] $\mathbf{b}' = 3\mathbf{b}$
 $P12_1$ (3) $\langle 2 \rangle$
 $P12_1$ (3) $\langle 2 + (0,0,2) \rangle$
 $\mathbf{a}, 3\mathbf{b}, \mathbf{c}$
 $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$
 $0, 0, 1$
[3] $\mathbf{c}' = 3\mathbf{c}$
 $\left\{ \begin{array}{l} P12_1 \text{ (3)} \\ P12_1 \text{ (3)} \\ P12_1 \text{ (3)} \end{array} \right. \quad \begin{array}{l} \langle 2 \rangle \\ \langle 2 + (0,0,2) \rangle \\ \langle 2 + (0,0,4) \rangle \end{array}$
 $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$
 $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$
 $0, 0, 2$
[3] $\mathbf{a}' = \mathbf{a} - \mathbf{c}$, $\mathbf{c}' = 3\mathbf{c}$
 $\left\{ \begin{array}{l} P12_1 \text{ (3)} \\ P12_1 \text{ (3)} \\ P12_1 \text{ (3)} \end{array} \right. \quad \begin{array}{l} \langle 2 \rangle \\ \langle 2 + (0,0,2) \rangle \\ \langle 2 + (0,0,4) \rangle \end{array}$
 $\mathbf{a} - \mathbf{c}, \mathbf{b}, 3\mathbf{c}$
 $\mathbf{a} - \mathbf{c}, \mathbf{b}, 3\mathbf{c}$
 $0, 0, 1$
[3] $\mathbf{a}' = \mathbf{a} - 2\mathbf{c}$, $\mathbf{c}' = 3\mathbf{c}$
 $\left\{ \begin{array}{l} P12_1 \text{ (3)} \\ P12_1 \text{ (3)} \\ P12_1 \text{ (3)} \end{array} \right. \quad \begin{array}{l} \langle 2 \rangle \\ \langle 2 + (0,0,2) \rangle \\ \langle 2 + (0,0,4) \rangle \end{array}$
 $\mathbf{a} - 2\mathbf{c}, \mathbf{b}, 3\mathbf{c}$
 $\mathbf{a} - 2\mathbf{c}, \mathbf{b}, 3\mathbf{c}$
 $0, 0, 1$
[3] $\mathbf{a}' = 3\mathbf{a}$
 $\left\{ \begin{array}{l} P12_1 \text{ (3)} \\ P12_1 \text{ (3)} \\ P12_1 \text{ (3)} \end{array} \right. \quad \begin{array}{l} \langle 2 \rangle \\ \langle 2 + (2,0,0) \rangle \\ \langle 2 + (4,0,0) \rangle \end{array}$
 $3\mathbf{a}, \mathbf{b}, \mathbf{c}$
 $3\mathbf{a}, \mathbf{b}, \mathbf{c}$
 $1, 0, 0$
 $3\mathbf{a}, \mathbf{b}, \mathbf{c}$
 $2, 0, 0$

• Series of maximal isomorphic subgroups

[p] $\mathbf{b}' = p\mathbf{b}$ $P121$ (3)	$\langle 2 \rangle$ $p > 1$ no conjugate subgroups	$\mathbf{a}, p\mathbf{b}, \mathbf{c}$	
[p] $\mathbf{a}' = \mathbf{a} - q\mathbf{c}$, $\mathbf{c}' = p\mathbf{c}$ $P121$ (3)	$\langle 2 + (0, 0, 2u) \rangle$ $p > 2$; $0 \leq q < p$; $0 \leq u < p$ p conjugate subgroups for each pair of q and prime p	$\mathbf{a} - q\mathbf{c}, \mathbf{b}, p\mathbf{c}$	$0, 0, u$
[p] $\mathbf{a}' = p\mathbf{a}$ $P121$ (3)	$\langle 2 + (2u, 0, 0) \rangle$ $p > 2$; $0 \leq u < p$ p conjugate subgroups for the prime p	$p\mathbf{a}, \mathbf{b}, \mathbf{c}$	$u, 0, 0$

I Minimal *translationengleiche* supergroups

[2] $P12/m$ (10); [2] $P12/c1$ (13); [2] $P222$ (16); [2] $P222_1$ (17); [2] $P2_12_12$ (18); [2] $C222$ (21); [2] $Pmm2$ (25); [2] $Pcc2$ (27); [2] $Pma2$ (28); [2] $Pnc2$ (30); [2] $Pba2$ (32); [2] $Pnn2$ (34); [2] $Cmm2$ (35); [2] $Ccc2$ (37); [2] $P4$ (75); [2] $P4_2$ (77); [2] $P\bar{4}$ (81); [3] $P6$ (168); [3] $P6_2$ (171); [3] $P6_4$ (172)

II Minimal non-isomorphic *klassengleiche* supergroups

• Additional centring translations

[2] $C121$ (5); [2] $A121$ (5, $C121$); [2] $I121$ (5, $C121$)

• Decreased unit cell

none

(Continued from the following page)

• Series of maximal isomorphic subgroups

[p] $\mathbf{c}' = p\mathbf{c}$ $P112$ (3)	$\langle 2 \rangle$ $p > 1$ no conjugate subgroups	$\mathbf{a}, \mathbf{b}, p\mathbf{c}$	
[p] $\mathbf{a}' = p\mathbf{a}$, $\mathbf{b}' = -qa + \mathbf{b}$ $P112$ (3)	$\langle 2 + (2u, 0, 0) \rangle$ $p > 2$; $0 \leq q < p$; $0 \leq u < p$ p conjugate subgroups for each pair of q and prime p	$p\mathbf{a}, -qa + \mathbf{b}, \mathbf{c}$	$u, 0, 0$
[p] $\mathbf{b}' = p\mathbf{b}$ $P112$ (3)	$\langle 2 + (0, 2u, 0) \rangle$ $p > 2$; $0 \leq u < p$ p conjugate subgroups for the prime p	$\mathbf{a}, p\mathbf{b}, \mathbf{c}$	$0, u, 0$

I Minimal *translationengleiche* supergroups

[2] $P112/m$ (10); [2] $P112/a$ (13); [2] $P222$ (16); [2] $P222_1$ (17); [2] $P2_12_12$ (18); [2] $C222$ (21); [2] $Pmm2$ (25); [2] $Pcc2$ (27); [2] $Pma2$ (28); [2] $Pnc2$ (30); [2] $Pba2$ (32); [2] $Pnn2$ (34); [2] $Cmm2$ (35); [2] $Ccc2$ (37); [2] $P4$ (75); [2] $P4_2$ (77); [2] $P\bar{4}$ (81); [3] $P6$ (168); [3] $P6_2$ (171); [3] $P6_4$ (172)

II Minimal non-isomorphic *klassengleiche* supergroups

• Additional centring translations

[2] $A112$ (5); [2] $B112$ (5, $A112$); [2] $I112$ (5, $A112$)

• Decreased unit cell

none