

$C_6^6$ 

No. 173

 $P6_3$ 

Axes	Coordinates	Wyckoff positions		
		$ 2a$	$ 2b$	$ 6c$
<b>I Maximal translationengleiche subgroups</b>				
[2] $P3$ (143)		$ 2 \times 1a$	$ 1b; 1c$	$ 2 \times 3d$
[3] $P112_1$ (4)		$ 2a$	$ 2a$	$ 3 \times 2a$
<b>II Maximal klassengleiche subgroups</b>				
Enlarged unit cell, non-isomorphic				
[3] $P6_5$ (170) $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$	$x, y, \frac{1}{3}z; \pm(0, 0, \frac{1}{3})$	$ 6a$	$ 6a$	$ 3 \times 6a$
[3] $P6_1$ (169) $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$	$x, y, \frac{1}{3}z; \pm(0, 0, \frac{1}{3})$	$ 6a$	$ 6a$	$ 3 \times 6a$
Enlarged unit cell, isomorphic				
[3] $P6_3$ $\mathbf{a}, \mathbf{b}, 3\mathbf{c}$	$x, y, \frac{1}{3}z; \pm(0, 0, \frac{1}{3})$	$ 3 \times 2a$	$ 3 \times 2b$	$ 3 \times 6c$
[p] $P6_3$ $\mathbf{a}, \mathbf{b}, p\mathbf{c}$	$x, y, \frac{1}{p}z; +(0, 0, \frac{u}{p})$ $p = \text{prime} > 2; u = 1, \dots, p-1$	$ p \times 2a$	$ p \times 2b$	$ p \times 6c$
[3] $P6_3$ $2\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, \mathbf{c}$	$\frac{1}{3}(x+y), \frac{1}{3}(-x+2y), z; \pm(\frac{1}{3}, \frac{2}{3}, 0)$	$ 2a; 2 \times 2b$	$ 6c$	$ 3 \times 6c$
[7] $P6_3$ $3\mathbf{a}+\mathbf{b}, -\mathbf{a}+2\mathbf{b}, \mathbf{c}$	$\frac{1}{7}(2x+y), \frac{1}{7}(-x+3y), z;$ $\pm(\frac{1}{7}, \frac{3}{7}, 0); \pm(\frac{3}{7}, \frac{2}{7}, 0); \pm(\frac{5}{7}, \frac{1}{7}, 0)$	$ 2a; 2 \times 6c$	$ 2b; 2 \times 6c$	$ 7 \times 6c$
[7] $P6_3$ $3\mathbf{a}+2\mathbf{b}, -2\mathbf{a}+\mathbf{b}, \mathbf{c}$	$\frac{1}{7}(x+2y), \frac{1}{7}(-2x+3y), z;$ $\pm(\frac{2}{7}, \frac{3}{7}, 0); \pm(\frac{3}{7}, \frac{1}{7}, 0); \pm(\frac{1}{7}, \frac{5}{7}, 0)$	$ 2a; 2 \times 6c$	$ 2b; 2 \times 6c$	$ 7 \times 6c$
[p] $P6_3$ $q\mathbf{a}+r\mathbf{b}, -r\mathbf{a}+(q-r)\mathbf{b}, \mathbf{c}$	$\frac{1}{p}((q-r)x+ry), \frac{1}{p}(-rx+qy), z;$ $+(\frac{ur}{p}, \frac{rq}{p}, 0)$ $p = \text{prime} = q^2 - qr + r^2 = 6n + 1;$ $q, r = 1, 2, \dots; q > r; u = 1, \dots, p-1$	$ 2a; \frac{p-1}{3} \times 6c$	$ 2b; \frac{p-1}{3} \times 6c$	$ p \times 6c$
[4] $P6_3$ $2\mathbf{a}, 2\mathbf{b}, \mathbf{c}$	$\frac{1}{2}x, \frac{1}{2}y, z; +(\frac{1}{2}, 0, 0);$ $+(0, \frac{1}{2}, 0); +(\frac{1}{2}, \frac{1}{2}, 0)$	$ 2a; 6c$	$ 2b; 6c$	$ 4 \times 6c$
[ $p^2$ ] $P6_3$ $p\mathbf{a}, p\mathbf{b}, \mathbf{c}$	$\frac{1}{p}x, \frac{1}{p}y, z; +(\frac{u}{p}, \frac{v}{p}, 0)$ $p = \text{prime} = 3n - 1; u, v = 1, \dots, p-1$	$ 2a; \frac{p^2-1}{3} \times 6c$	$ 2b; \frac{p^2-1}{3} \times 6c$	$ p^2 \times 6c$