

$Pn\bar{3}$

T_h^2

$m\bar{3}$

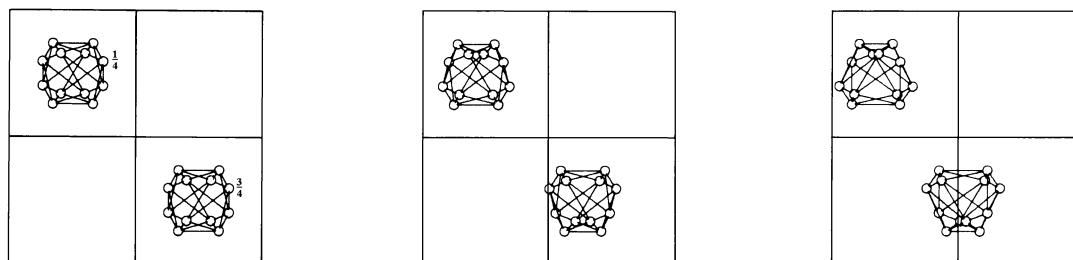
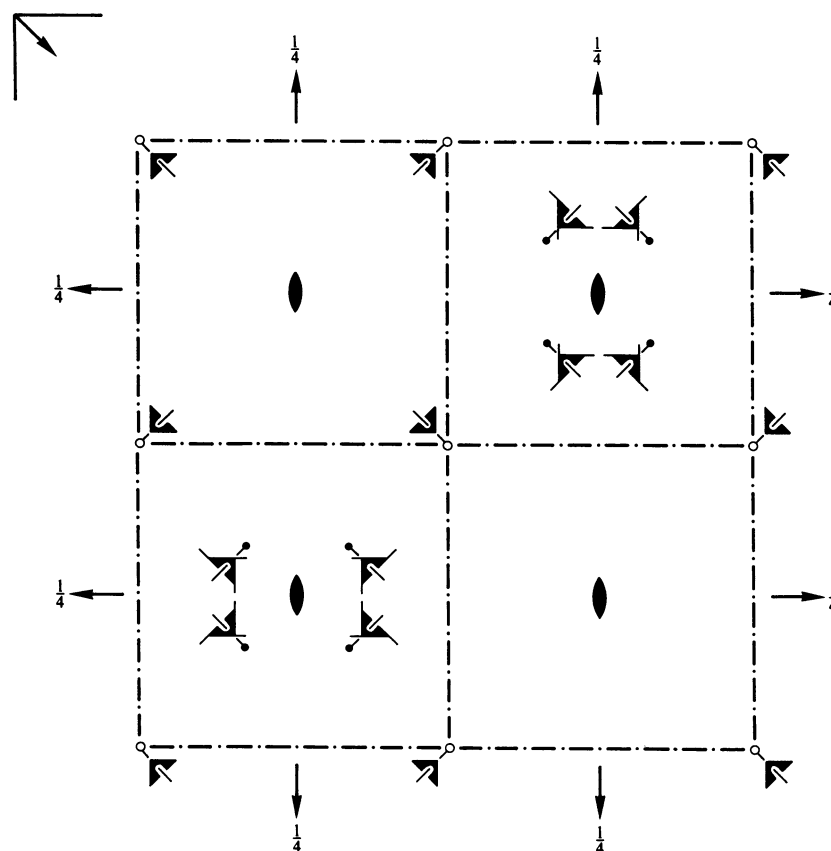
Cubic

No. 201

$P2/n\bar{3}$

Patterson symmetry $Pm\bar{3}$

ORIGIN CHOICE 2



Origin at centre ($\bar{3}$), at $\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$ from 23

Asymmetric unit $-\frac{1}{4} \leq x \leq \frac{3}{4}; -\frac{1}{4} \leq y \leq \frac{1}{4}; -\frac{1}{4} \leq z \leq \frac{1}{4}; y \leq \min(x, \frac{1}{2} - x); z \leq y$
Vertices $-\frac{1}{4}, -\frac{1}{4}, -\frac{1}{4}; \frac{3}{4}, -\frac{1}{4}, -\frac{1}{4}; \frac{1}{4}, \frac{1}{4}, -\frac{1}{4}; \frac{1}{4}, \frac{1}{4}, \frac{1}{4}$

Symmetry operations

- | | | | |
|-------------------------------------|--|--|--|
| (1) 1 | (2) 2 $\frac{1}{4}, \frac{1}{4}, z$ | (3) 2 $\frac{1}{4}, y, \frac{1}{4}$ | (4) 2 $x, \frac{1}{4}, \frac{1}{4}$ |
| (5) 3^+ x, x, x | (6) 3^+ $\bar{x}, x + \frac{1}{2}, \bar{x}$ | (7) 3^+ $x + \frac{1}{2}, \bar{x}, \bar{x}$ | (8) 3^+ $\bar{x} + \frac{1}{2}, \bar{x} + \frac{1}{2}, x$ |
| (9) 3^- x, x, x | (10) 3^- $x + \frac{1}{2}, \bar{x}, \bar{x}$ | (11) 3^- $\bar{x} + \frac{1}{2}, \bar{x} + \frac{1}{2}, x$ | (12) 3^- $\bar{x}, x + \frac{1}{2}, \bar{x}$ |
| (13) $\bar{1}$ 0,0,0 | (14) $n(\frac{1}{2}, \frac{1}{2}, 0)$ $x, y, 0$ | (15) $n(\frac{1}{2}, 0, \frac{1}{2})$ $x, 0, z$ | (16) $n(0, \frac{1}{2}, \frac{1}{2})$ $0, y, z$ |
| (17) $\bar{3}^+$ $x, x, x; 0, 0, 0$ | (18) $\bar{3}^+$ $\bar{x} - 1, x + \frac{1}{2}, \bar{x}; -\frac{1}{2}, 0, \frac{1}{2}$ | (19) $\bar{3}^+$ $x - \frac{1}{2}, \bar{x} + 1, \bar{x}; 0, \frac{1}{2}, -\frac{1}{2}$ | (20) $\bar{3}^+$ $\bar{x} + \frac{1}{2}, \bar{x} - \frac{1}{2}, x; \frac{1}{2}, -\frac{1}{2}, 0$ |
| (21) $\bar{3}^-$ $x, x, x; 0, 0, 0$ | (22) $\bar{3}^-$ $x + \frac{1}{2}, \bar{x} - 1, \bar{x}; 0, -\frac{1}{2}, \frac{1}{2}$ | (23) $\bar{3}^-$ $\bar{x} - \frac{1}{2}, \bar{x} + \frac{1}{2}, x; -\frac{1}{2}, \frac{1}{2}, 0$ | (24) $\bar{3}^-$ $\bar{x} + 1, x - \frac{1}{2}, \bar{x}; \frac{1}{2}, 0, -\frac{1}{2}$ |

Generators selected (1); $t(1,0,0)$; $t(0,1,0)$; $t(0,0,1)$; (2); (3); (5); (13)

Positions

Multiplicity, Wyckoff letter, Site symmetry	Coordinates	Reflection conditions
		h, k, l cyclically permutable General:
24 h 1	(1) x, y, z (2) $\bar{x} + \frac{1}{2}, \bar{y} + \frac{1}{2}, z$ (3) $\bar{x} + \frac{1}{2}, y, \bar{z} + \frac{1}{2}$ (4) $x, \bar{y} + \frac{1}{2}, \bar{z} + \frac{1}{2}$ (5) z, x, y (6) $z, \bar{x} + \frac{1}{2}, \bar{y} + \frac{1}{2}$ (7) $\bar{z} + \frac{1}{2}, \bar{x} + \frac{1}{2}, y$ (8) $\bar{z} + \frac{1}{2}, x, \bar{y} + \frac{1}{2}$ (9) y, z, x (10) $\bar{y} + \frac{1}{2}, z, \bar{x} + \frac{1}{2}$ (11) $y, \bar{z} + \frac{1}{2}, \bar{x} + \frac{1}{2}$ (12) $\bar{y} + \frac{1}{2}, \bar{z} + \frac{1}{2}, x$ (13) $\bar{x}, \bar{y}, \bar{z}$ (14) $x + \frac{1}{2}, y + \frac{1}{2}, \bar{z}$ (15) $x + \frac{1}{2}, \bar{y}, z + \frac{1}{2}$ (16) $\bar{x}, y + \frac{1}{2}, z + \frac{1}{2}$ (17) $\bar{z}, \bar{x}, \bar{y}$ (18) $\bar{z}, x + \frac{1}{2}, y + \frac{1}{2}$ (19) $z + \frac{1}{2}, x + \frac{1}{2}, \bar{y}$ (20) $z + \frac{1}{2}, \bar{x}, y + \frac{1}{2}$ (21) $\bar{y}, \bar{z}, \bar{x}$ (22) $y + \frac{1}{2}, \bar{z}, x + \frac{1}{2}$ (23) $\bar{y}, z + \frac{1}{2}, x + \frac{1}{2}$ (24) $y + \frac{1}{2}, z + \frac{1}{2}, \bar{x}$	$0kl : k + l = 2n$ $h00 : h = 2n$

Special: as above, plus

12 g 2..	$x, \frac{3}{4}, \frac{1}{4}$ $\bar{x}, \frac{1}{4}, \frac{3}{4}$	$\bar{x} + \frac{1}{2}, \frac{3}{4}, \frac{1}{4}$ $x + \frac{1}{2}, \frac{1}{4}, \frac{3}{4}$	$\frac{1}{4}, x, \frac{3}{4}$ $\frac{3}{4}, \bar{x}, \frac{1}{4}$	$\frac{1}{4}, \bar{x} + \frac{1}{2}, \frac{3}{4}$ $\frac{3}{4}, x + \frac{1}{2}, \frac{1}{4}$	$\frac{3}{4}, \frac{1}{4}, x$ $\frac{1}{4}, \frac{3}{4}, \bar{x}$	$\frac{3}{4}, \frac{1}{4}, \bar{x} + \frac{1}{2}$ $\frac{1}{4}, \frac{3}{4}, x + \frac{1}{2}$	$hkl : h + k + l = 2n$
12 f 2..	$x, \frac{1}{4}, \frac{1}{4}$ $\bar{x}, \frac{3}{4}, \frac{3}{4}$	$\bar{x} + \frac{1}{2}, \frac{1}{4}, \frac{1}{4}$ $x + \frac{1}{2}, \frac{3}{4}, \frac{3}{4}$	$\frac{1}{4}, x, \frac{1}{4}$ $\frac{3}{4}, \bar{x}, \frac{3}{4}$	$\frac{1}{4}, \bar{x} + \frac{1}{2}, \frac{1}{4}$ $\frac{3}{4}, x + \frac{1}{2}, \frac{3}{4}$	$\frac{1}{4}, \frac{1}{4}, x$ $\frac{3}{4}, \frac{3}{4}, \bar{x}$	$\frac{1}{4}, \frac{1}{4}, \bar{x} + \frac{1}{2}$ $\frac{3}{4}, \frac{3}{4}, x + \frac{1}{2}$	$hkl : h + k + l = 2n$
8 e .3.	x, x, x $\bar{x}, \bar{x}, \bar{x}$	$\bar{x} + \frac{1}{2}, \bar{x} + \frac{1}{2}, x$ $x + \frac{1}{2}, x + \frac{1}{2}, \bar{x}$	$\bar{x} + \frac{1}{2}, x, \bar{x} + \frac{1}{2}$ $x + \frac{1}{2}, \bar{x}, x + \frac{1}{2}$	$x, \bar{x} + \frac{1}{2}, \bar{x} + \frac{1}{2}$ $\bar{x}, x + \frac{1}{2}, x + \frac{1}{2}$			no extra conditions
6 d 222..	$\frac{1}{4}, \frac{3}{4}, \frac{3}{4}$	$\frac{3}{4}, \frac{1}{4}, \frac{3}{4}$	$\frac{3}{4}, \frac{3}{4}, \frac{1}{4}$	$\frac{3}{4}, \frac{1}{4}, \frac{1}{4}$	$\frac{1}{4}, \frac{3}{4}, \frac{1}{4}$	$\frac{1}{4}, \frac{1}{4}, \frac{3}{4}$	$hkl : h + k + l = 2n$
4 c . $\bar{3}$.	$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$	$0, 0, \frac{1}{2}$	$0, \frac{1}{2}, 0$	$\frac{1}{2}, 0, 0$			$hkl : h + k, h + l, k + l = 2n$
4 b . $\bar{3}$.	$0, 0, 0$	$\frac{1}{2}, \frac{1}{2}, 0$	$\frac{1}{2}, 0, \frac{1}{2}$	$0, \frac{1}{2}, \frac{1}{2}$			$hkl : h + k, h + l, k + l = 2n$
2 a 23.	$\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$	$\frac{3}{4}, \frac{3}{4}, \frac{3}{4}$					$hkl : h + k + l = 2n$

Symmetry of special projections

Along [001] $c2mm$

$\mathbf{a}' = \mathbf{a}$ $\mathbf{b}' = \mathbf{b}$

Origin at $\frac{1}{4}, \frac{1}{4}, z$

Along [111] $p6$

$\mathbf{a}' = \frac{1}{3}(2\mathbf{a} - \mathbf{b} - \mathbf{c})$ $\mathbf{b}' = \frac{1}{3}(-\mathbf{a} + 2\mathbf{b} - \mathbf{c})$

Origin at x, x, x

Along [110] $p2mm$

$\mathbf{a}' = \frac{1}{2}(-\mathbf{a} + \mathbf{b})$ $\mathbf{b}' = \mathbf{c}$

Origin at $x, x, 0$

Maximal non-isomorphic subgroups

I	[2] $P23$ (195)	1; 2; 3; 4; 5; 6; 7; 8; 9; 10; 11; 12
	[3] $Pn1$ ($Pnnn$, 48)	1; 2; 3; 4; 13; 14; 15; 16
	[4] $P1\bar{3}$ ($R\bar{3}$, 148)	1; 5; 9; 13; 17; 21
	[4] $P1\bar{3}$ ($R\bar{3}$, 148)	1; 6; 12; 13; 18; 24
	[4] $P1\bar{3}$ ($R\bar{3}$, 148)	1; 7; 10; 13; 19; 22
	[4] $P1\bar{3}$ ($R\bar{3}$, 148)	1; 8; 11; 13; 20; 23

IIa none

IIb [2] $Fd\bar{3}$ ($\mathbf{a}' = 2\mathbf{a}, \mathbf{b}' = 2\mathbf{b}, \mathbf{c}' = 2\mathbf{c}$) (203)

Maximal isomorphic subgroups of lowest index

IIc [27] $Pn\bar{3}$ ($\mathbf{a}' = 3\mathbf{a}, \mathbf{b}' = 3\mathbf{b}, \mathbf{c}' = 3\mathbf{c}$) (201)

Minimal non-isomorphic supergroups

I [2] $Pn\bar{3}n$ (222); [2] $Pn\bar{3}m$ (224)

II [2] $Im\bar{3}$ (204); [4] $Fm\bar{3}$ (202)