## 2. DIFFRACTION GEOMETRY AND ITS PRACTICAL REALIZATION

published by Wilson (1963, 1974). His work provides the mathematical foundation for understanding the origin and treatment of the various sources of errors. The major aberrations are described in the following and are illustrated with experimental profiles and plots of computed data for better visualization and interpretation of the effects. The information can be used to correct the experimental data, interpret the profile broadening and shifts, and evaluate the precision of the analysis. Chapter 5.2 contains tables listing the centroid displacements and variances of the various aberrations.

The magnitudes of the aberrations and their effects are illustrated in Figs. 2.3.1.8(a) and (b), which show the Cu  $K\alpha_1, K\alpha_2$  spectrum inside the experimental profile. At high  $2\theta$ 's, the shape of the experimental profile is largely determined by the spectral distribution, but at low  $2\theta$ 's the aberrations are the principal contributors. The basic experimental high-resolution profile shapes from specimens without appreciable broadening effects (NIST silicon powder standard) are shown in Figs. 2.3.1.8(c)-(f). The solid-line profiles were obtained with a reflection specimen (Fig. 2.3.1.3), and the dashed-line profiles with transmission-specimen geometry (Fig. 2.3.1.12). The differences in the  $K\alpha_1, K\alpha_2$  doublet separations are explained in Subsection 2.3.1.2. These profiles are the basic instrument functions which show the profile shapes contained in all

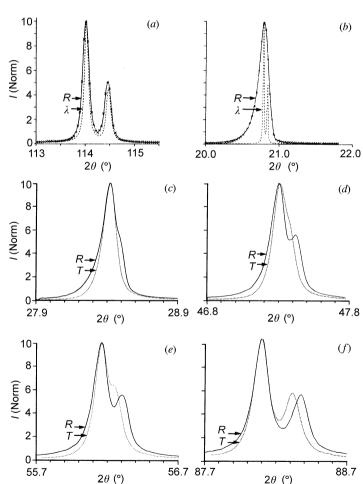


Fig. 2.3.1.8. Diffractometer profiles. (a) and (b) Spectral profiles  $\lambda$  of Cu  $K\alpha$  doublet (dashed-line profiles) inside experimental profiles R (solid line). (c)–(f) Experimental profiles with reflection specimen (R) geometry (Fig. 2.3.1.3) with  $\alpha_{\rm ES}$  1° and  $\alpha_{\rm RS}$  0.046° (solid line profiles), and transmission specimen (T) (Fig. 2.3.1.12) with  $\alpha_{\rm ES}$  2° and receiving axial divergence parallel slits (dotted profiles). Cu  $K\alpha$  radiation. (a) Si(531), (b) quartz(100), (c) Si(111), (d) Si(220), (e) Si(311), and (f) Si(422).

reflections recorded with these methods. The shapes are modified by changing slit sizes.

## 2.3.1.1.5. Focal line and receiving-slit widths

The projected source width  $F_w$  and receiving-slit width  $RS_w$  each add a symmetrical broadening to the profiles that is constant for all angles. Both the profile width and the intensity increase with increasing take-off angle (Section 2.3.5). However, the contribution of  $F_w$  is small when the line focus is used, Fig. 2.3.1.9(a). The receiving slit can easily be changed and it is one of the most important elements in controlling the profile width, intensity, and peak-to-background ratio, as is shown in Figs. 2.3.1.9(a) and (c). Because of the contributions of other broadening factors,  $\alpha_{RS}$  can be about twice  $\alpha_F$  (line focus) without significant loss of resolution.

The projected width of the X-ray tube focus  $F_w$  is given in equation (2.3.1.2). The aperture is

$$\alpha_F = 2 \arctan(F_w/2R). \tag{2.3.1.8}$$

For a line focus with actual width  $F_w'=1\,\mathrm{mm},\ \psi=5^\circ,$  and  $R=185\,\mathrm{mm},\ \alpha_F=0.011^\circ.$  The receiving-slit aperture is

$$\alpha_{RS} = 2 \arctan(RS_w/2R). \tag{2.3.1.9}$$

For RS<sub>w</sub> = 0.2 mm and R = 185 mm.  $\alpha_{RS}$  is 0.062°. The FWHM of the profiles is always greater than the receiving-slit aperture because of the other broadening factors.

## 2.3.1.1.6. Aberrations related to the specimen

The major displacement errors arising from the specimen are (1) displacement of the specimen surface from the axis of rotation, (2) use of a flat rather than a curved specimen, and (3) specimen transparency. These are illustrated schematically for the focusing plane in Fig. 2.3.1.10(a). The rays from a highly absorbing or very thin specimen with the same curvature as the focusing circle converge at A without broadening and at the correct  $2\theta$ . The rays from the flat surface cause an asymmetric profile shifted to B. Penetration of the beam below the surface combined with the flat specimen causes additional broadening and a shift to C.

The most frequent and usually the largest source of angular errors arises from displacement of the specimen surface from the diffractometer axis of rotation. It is not easy to avoid and may arise from several sources. It is advisable to check the reproducibility of inserting the specimen in the diffractometer by recording an isolated peak at low  $2\theta$  for each insertion. If only a radial displacement s occurs, the reflection is shifted

$$\Delta 2\theta(\text{rad}) = \pm 2s\cos\theta/R, \qquad (2.3.1.10)$$

where R is the diffractometer radius. A plot of equation (2.3.1.10) is shown in Fig. 2.3.1.10(b). The shift is to larger or smaller angles depending on the direction of the displacement and there is no broadening if the displacement is only radial and relatively small. Even a small displacement causes a relatively large shift; for example, if  $s = +0.1 \,\mathrm{mm}$  and  $R = 185 \,\mathrm{mm}$ ,  $\Delta 2\theta = +0.06^{\circ}$  at  $20^{\circ}2\theta$ . This gives rise to a systematic error in the recorded reflection angles, which increases with decreasing  $2\theta$ . It could be handled with a  $\cos\theta\cot\theta$  plot, providing it was the only source of error. There are other possible sources of displacement such as (a) if the bearing surface of the specimen post was not machined to lie exactly on the axis of rotation, (b) improper specimen preparation or insertion in which the surface was not exactly coincident with the bearing surface or (c) nonplanar specimen surface, irregularities, large particle sizes, and specimen transparency. Source (a) leads to a constant error