

1.2. GUIDE TO THE USE OF THE SUBPERIODIC GROUP TABLES

Table 1.2.14.2. Projection of three-dimensional symmetry elements (layer and rod groups)

Symmetry element in three dimensions		Symmetry element in projection	
<i>Arbitrary orientation</i>			
Symmetry centre $\bar{1}$		Rotation point 2 at projection of centre	
<i>Parallel to projection direction</i>			
Rotation axis	2, 3, 4, 6	Rotation point	2, 3, 4, 6
Screw axis	2_1	Rotation point	2
	$3_1, 3_2$		3
	$4_1, 4_2, 4_3$		4
	$6_1, 6_2, 6_3, 6_4, 6_5$		6
Rotoinversion axis	$\bar{4}$	Rotation point	4
	$\bar{6} \equiv 3/m$		3 (with overlap of atoms)
	$\bar{3} \equiv 3 \times \bar{1}$		6
Reflection plane m		Reflection line m	
Glide plane with \perp component [†]		Glide line g	
Glide plane without \perp component [†]		Reflection line m	
<i>Normal to projection direction</i>			
Rotation axis	2, 4, 6	Reflection line m	
	3	None	
Screw axis	$4_2, 6_2, 6_4$	Reflection line m	
	$2_1, 4_1, 4_3, 6_1, 6_3, 6_5$	Glide line g	
	$3_1, 3_2$	None	
Rotoinversion axis	$\bar{4}$	Reflection line m parallel to axis	
	$\bar{6} \equiv 3/m$	Reflection line m perpendicular to axis	
	$\bar{3} \equiv 3 \times \bar{1}$	Rotation point 2 (at projection of centre)	
Reflection plane m		None, but overlap of atoms	
Glide plane with glide component \mathbf{t}		Translation \mathbf{t}	

[†] The term 'with \perp component' refers to the component of the glide vector normal to the projection direction.

Table 1.2.14.3. Projection of two-dimensional symmetry elements (frieze groups)

Symmetry element in two dimensions		Symmetry element in projection	
Rotation point 2		Reflection point m	
<i>Parallel to projection direction</i>			
Reflection line m		Reflection point m	
Glide line g		Reflection point m	
<i>Normal to projection direction</i>			
Reflection line m		None (with overlap of atoms)	
Glide line g with glide component \mathbf{t}		Translation \mathbf{t}	

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II klassengleiche or k subgroups.

Type **II** is subdivided again into two blocks:

IIa: the conventional cells of **G** and **S** are the same, and

IIb: the conventional cell of **S** is larger than that of **G**.

Block **IIa** has no entries for subperiodic groups with a primitive cell. Only in the case of the nine centred layer groups are there entries, when it contains those maximal subgroups **S** which have lost all the centring translations of **G** but none of the integral translations.

 1.2.15.1.1. Blocks **I** and **IIa**

In blocks **I** and **IIa**, every maximal subgroup **S** of a subperiodic group **G** is listed with the following information:

[i] HMS1 (HMS2) Sequence of numbers

The symbols have the following meaning:

[i]: index of **S** in **G**.

HMS1: short Hermann–Mauguin symbol of **S**, referred to the coordinate system and setting of **G**; this symbol may be unconventional.

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(HMS2): conventional short Hermann–Mauguin symbol of **S**, given only if HMS1 is not in conventional short form.

Sequence of numbers: coordinate triplets of **G** retained in **S**. The numbers refer to the numbering scheme of the coordinate triplets of the general position. For the centred layer groups the following abbreviations are used:

Block I (all translations retained). *Number* +: coordinate triplet given by *Number*, plus that obtained by adding the centring translation $(1/2, 1/2, 0)$ of **G**. (*Numbers*) +: the same as above, but applied to all *Numbers* between parentheses.

Block IIa (not all translations retained). *Number* + $(1/2, 1/2, 0)$: coordinate triplet obtained by adding the translation $(1/2, 1/2, 0)$ to the triplet given by *Number*. (*Numbers*) + $(1/2, 1/2, 0)$: the same as above, but applied to all *Numbers* between parentheses.

Examples

(1) **G**: Layer group $c211$ (L10)

I	[2]	$c1$	$(p1)$	$1+$
IIa	[2]	$p2_111$	$1; 2 + (1/2, 1/2, 0)$	
	[2]	$p211$	$1; 2$	

where the numbers have the following meaning:

$1+$	x, y, z	$x + 1/2, y + 1/2, z$
$1; 2$	x, y, z	x, \bar{y}, \bar{z}
$1; 2+$	x, y, z	$x + 1/2, \bar{y} + 1/2, \bar{z}$

(2) **G**: Rod group $\#422$ (R30)

I	[2]	$\#411$ ($\#4$)	$1; 2; 3; 4$
	[2]	$\#221$ ($\#222$)	$1; 2; 5; 6$
	[2]	$\#212$ ($\#222$)	$1; 2; 7; 8$

The HMS1 symbol in each of the three subgroups **S** is given in the tetragonal coordinate system of the group **G**. In the first case,

references