

Laue class  $D_{3d} - \bar{3}m$ 

6. SCANNING TABLES

Trigonal

 No. 159  $P31c$ 
 $\mathcal{G} = P31c$ 
 $C_{3v}^4$ 

| Orientation orbit<br>( <i>hkil</i> ) | Conventional basis<br>of the scanning group |                               |                               | Scanning<br>group<br>$\mathcal{H}$ | Linear<br>orbit<br>$s\mathbf{d}$                     | Sectional<br>layer group<br>$\mathcal{L}(s\mathbf{d})$ |     |  |
|--------------------------------------|---|-------------------------------|-------------------------------|------------------------------------|--|--|-----|--|
| (0001)                               | <b>a</b>                                    | <b>b</b>                      | <b>c</b>                      | $P31c$                             | $[s\mathbf{d}, (s + \frac{1}{2})\mathbf{d}]$         | $p3$   | L65 |  |
| (01 $\bar{1}$ 0)                     | <b>c</b>                                    | <b>a</b>                      | <b>a + 2b</b>                 | $A11a$                             | $[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$               | $p11a$   | L05 |  |
| ( $\bar{1}$ 010)                     | <b>c</b>                                    | <b>b</b>                      | $-(2\mathbf{a} + \mathbf{b})$ |                                    | $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$     | $p11n$   | L05 |  |
| (1 $\bar{1}$ 00)                     | <b>c</b>                                    | $-(\mathbf{a} + \mathbf{b})$  | <b>(a - b)</b>                |                                    | $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$ | $p1$   | L01 |  |
| ( $\bar{1}$ 2 $\bar{1}$ 0)           | <b>c</b>                                    | <b>2a + b</b>                 | <b>b</b>                      | $A1a1$                             | $[s\mathbf{d}, (s + \frac{1}{2})\mathbf{d}]$         | $p1a1$   | L12 |  |
| ( $\bar{1}$ $\bar{1}$ 20)            | <b>c</b>                                    | <b>(b - a)</b>                | $-(\mathbf{a} + \mathbf{b})$  |                                    |  |  |     |  |
| (2 $\bar{1}$ 10)                     | <b>c</b>                                    | $-(\mathbf{a} + 2\mathbf{b})$ | <b>a</b>                      |                                    |  |  |     |  |

 No. 160  $R3m$ 
 $\mathcal{G} = R3m$ 
 $C_{3v}^5$ 

| Orientation orbit                 |                                  | Conventional basis<br>of the scanning group |                              |                              | Scanning<br>group<br>$\mathcal{H}$ | Linear<br>orbit<br>$s\mathbf{d}$  | Sectional<br>layer group<br>$\mathcal{L}(s\mathbf{d})$ |        |     |
|-----------------------------------|----------------------------------|---|------------------------------|------------------------------|------------------------------------|---|--|--------|-----|
| HEXAG.<br>AXES<br>( <i>hkil</i> ) | RHOMB.<br>AXES<br>( <i>hkl</i> ) | <b>a'</b>                                   | <b>b'</b>                    | <b>d</b>                     |                                    |   |  |        |     |
| (0001)                            | (111)                            | <b>a</b>                                    | <b>b</b>                     | <b>c</b>                     | $R3m$                              | $[s\mathbf{d}, (s + \frac{1}{3})\mathbf{d}, (s + \frac{2}{3})\mathbf{d}]$ | $p3m1$   | L69    |     |
| (01 $\bar{1}$ 0)                  | (11 $\bar{1}$ )                  | <b>c</b>                                    | <b>a</b>                     | $-\mathbf{c}_r$              | $I1m1$                             | $[s\mathbf{d}, (s + \frac{1}{2})\mathbf{d}]$                              | $p1m1$   | L11    |     |
| ( $\bar{1}$ 010)                  | ( $\bar{1}$ 11)                  | <b>c</b>                                    | <b>b</b>                     | $-\mathbf{a}_r$              |                                    |   |  |        |     |
| (1 $\bar{1}$ 00)                  | (1 $\bar{1}$ 1)                  | <b>c</b>                                    | $-(\mathbf{a} + \mathbf{b})$ | $-\mathbf{b}_r$              |                                    |   |  |        |     |
| ( $\bar{1}$ 2 $\bar{1}$ 0)        | (01 $\bar{1}$ )                  | <b>c</b>                                    | <b>a<sub>r</sub></b>         | <b>b</b>                     | $I11m$                             | $[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$                                    | $p11m$   | L04    |     |
| ( $\bar{1}$ $\bar{1}$ 20)         | ( $\bar{1}$ 01)                  | <b>c</b>                                    | <b>b<sub>r</sub></b>         | $-(\mathbf{a} + \mathbf{b})$ |                                    |   | $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$       | $p11n$ | L05 |
| (2 $\bar{1}$ 10)                  | (1 $\bar{1}$ 0)                  | <b>c</b>                                    | <b>c<sub>r</sub></b>         | <b>a</b>                     |                                    |   | $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$   | $p1$   | L01 |

 No. 161  $R3c$ 
 $\mathcal{G} = R3c$ 
 $C_{3v}^6$ 

| Orientation orbit                 |                                  | Conventional basis<br>of the scanning group |                              |                              | Scanning<br>group<br>$\mathcal{H}$ | Linear<br>orbit<br>$s\mathbf{d}$   | Sectional<br>layer group<br>$\mathcal{L}(s\mathbf{d})$ |        |     |
|-----------------------------------|----------------------------------|---|------------------------------|------------------------------|------------------------------------|--|--|--------|-----|
| HEXAG.<br>AXES<br>( <i>hkil</i> ) | RHOMB.<br>AXES<br>( <i>hkl</i> ) | <b>a'</b>                                   | <b>b'</b>                    | <b>d</b>                     |                                    |  |  |        |     |
| (0001)                            | (111)                            | <b>a</b>                                    | <b>b</b>                     | <b>c</b>                     | $R3c$                              | $[s\mathbf{d}, (s + \frac{1}{6})\mathbf{d}, (s + \frac{1}{3})\mathbf{d}, (s + \frac{1}{2})\mathbf{d}, (s + \frac{2}{3})\mathbf{d}, (s + \frac{5}{6})\mathbf{d}]$ | $p3$   | L65    |     |
| (01 $\bar{1}$ 0)                  | (11 $\bar{1}$ )                  | <b>c</b>                                    | <b>a</b>                     | $-\mathbf{c}_r$              | $I1a1$                             | $[s\mathbf{d}, (s + \frac{1}{2})\mathbf{d}]$   | $p1a1$   | L12    |     |
| ( $\bar{1}$ 010)                  | ( $\bar{1}$ 11)                  | <b>c</b>                                    | <b>b</b>                     | $-\mathbf{a}_r$              |                                    |  |  |        |     |
| (1 $\bar{1}$ 00)                  | (1 $\bar{1}$ 1)                  | <b>c</b>                                    | $-(\mathbf{a} + \mathbf{b})$ | $-\mathbf{b}_r$              |                                    |  |  |        |     |
| ( $\bar{1}$ 2 $\bar{1}$ 0)        | (01 $\bar{1}$ )                  | <b>c</b>                                    | <b>a<sub>r</sub></b>         | <b>b</b>                     | $I11a$                             | $[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$   | $p11a$   | L05    |     |
| ( $\bar{1}$ $\bar{1}$ 20)         | ( $\bar{1}$ 01)                  | <b>c</b>                                    | <b>b<sub>r</sub></b>         | $-(\mathbf{a} + \mathbf{b})$ |                                    |  | $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$       | $p11b$ | L05 |
| (2 $\bar{1}$ 10)                  | (1 $\bar{1}$ 0)                  | <b>c</b>                                    | <b>c<sub>r</sub></b>         | <b>a</b>                     |                                    |  | $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$   | $p1$   | L01 |

Arithmetic classes  $321P$ ,  $3m1P$  and  $\bar{3}m1P$

| Orientation orbit<br>( <i>hkl</i> )   | Conventional basis of the scanning group |  |  | Auxiliary basis of the scanning group |                    |                              |
|---|--|--|--|---------------------------------------|--------------------|------------------------------|
|   | <b>a'</b>                                | <b>b'</b>                                    | <b>d</b>                                     | $\hat{\mathbf{a}}$                    | $\hat{\mathbf{b}}$ | $\hat{\mathbf{c}}$           |
| ( $0h\bar{h}l$ )  | <b>a</b>                                 | $n(\mathbf{a} + 2\mathbf{b}) - m\mathbf{c}$  | $p(\mathbf{a} + 2\mathbf{b}) + q\mathbf{c}$  | <b>a + 2b</b>                         | <b>c</b>           | <b>a</b>                     |
| ( $\bar{h}0hl$ )  | <b>b</b>                                 | $-n(2\mathbf{a} + \mathbf{b}) - m\mathbf{c}$ | $-p(2\mathbf{a} + \mathbf{b}) + q\mathbf{c}$ | $-(2\mathbf{a} + \mathbf{b})$         | <b>c</b>           | <b>b</b>                     |
| ( $h\bar{h}0l$ )  | $-(\mathbf{a} + \mathbf{b})$             | $n(\mathbf{a} - \mathbf{b}) - m\mathbf{c}$   | $p(\mathbf{a} - \mathbf{b}) + q\mathbf{c}$   | <b>a - b</b>                          | <b>c</b>           | $-(\mathbf{a} + \mathbf{b})$ |
| $l$ odd $\Rightarrow n = l, m = 2h$ ; $l$ even $\Rightarrow n = l/2, m = h$ |  |  |  |                                       |                    |                              |

Arithmetic classes  $321P$ ,  $3m1P$  and  $\bar{3}m1P$

| Serial No.       | 150     | 152          | 154          | 156        | 158        | 164          | 165          |
|------------------|---------|--------------|--------------|------------|------------|--------------|--------------|
| Group type       | $D_3^2$ | $D_3^4$      | $D_3^6$      | $C_{3v}^1$ | $C_{3v}^2$ | $D_{3d}^3$   | $D_{3d}^4$   |
| Group            | $P321$  | $P3_121$     | $P3_221$     | $P3m1$     | $P3c1$     | $\bar{P}3m1$ | $\bar{P}3c1$ |
| ( $0h\bar{h}l$ ) | $B112$  | $B112$ (c/3) | $B112$ (c/6) | $B11m$     | $B11b$     | $B112/m$     | $B112/b$     |
| ( $\bar{h}0hl$ ) |         | $B112$ (c/6) | $B112$ (c/3) |            |            |              |              |
| ( $h\bar{h}0l$ ) |         | $B112$       | $B112$       |            |            |              |              |

Centring type  $R$

Arithmetic classes  $32R$ ,  $3mR$  and  $\bar{3}mR$

| Orientation orbit  |                               | Conventional basis of the scanning group |             |             | Auxiliary basis of the scanning group |                      |                              |
|--|-------------------------------|--|-------------|-------------|---------------------------------------|----------------------|------------------------------|
| HEXAG. AXES<br>( <i>hkl</i> )  | RHOMB. AXES<br>( <i>hkl</i> ) | <b>a'</b>                                | <b>b'</b>   | <b>d</b>    | $\hat{\mathbf{a}}$                    | $\hat{\mathbf{b}}$   | $\hat{\mathbf{c}}$           |
| ( $0h\bar{h}l$ )   | ( <i>hhl</i> )                | <b>a</b>                                 | $nc - mc_r$ | $pc + qc_r$ | <b>c</b>                              | <b>c<sub>r</sub></b> | <b>a</b>                     |
| ( $\bar{h}0hl$ )   | ( <i>lhh</i> )                | <b>b</b>                                 | $nc - ma_r$ | $pc + qa_r$ | <b>c</b>                              | <b>a<sub>r</sub></b> | <b>b</b>                     |
| ( $h\bar{h}0l$ )   | ( <i>hlh</i> )                | $-(\mathbf{a} + \mathbf{b})$             | $nc - mb_r$ | $pc + qb_r$ | <b>c</b>                              | <b>b<sub>r</sub></b> | $-(\mathbf{a} + \mathbf{b})$ |
| Transformation of indices from hexagonal to auxiliary monoclinic basis<br>$l$ odd $\Rightarrow n = l - 2h, m = 6h$ ; $l$ even $\Rightarrow n = l/2 - h, m = 3h$    |                               |  |             |             |                                       |                      |                              |
| Transformation of indices from rhombohedral to auxiliary monoclinic basis<br>$l$ odd $\Rightarrow n = l, m = 2h + l$ ; $l$ even $\Rightarrow n = l/2, m = h + l/2$ |                               |  |             |             |                                       |                      |                              |

Arithmetic classes  $32R$ ,  $3mR$  and  $\bar{3}mR$

| Serial No.       | 155            | 160        | 161        | 166         | 167         |
|------------------|----------------|------------|------------|-------------|-------------|
| Group type       | $D_3^7$        | $C_{3v}^5$ | $C_{3v}^6$ | $D_{3d}^5$  | $D_{3d}^6$  |
| Group            | $R32$          | $R3m$      | $R3c$      | $\bar{R}3m$ | $\bar{R}3c$ |
| HEXAG. AXES      | RHOMB. AXES    |            |            |             |             |
| ( $0h\bar{h}l$ ) | ( <i>hhl</i> ) | $I112$     | $I11m$     | $I11a$      | $I112/m$    |
| ( $\bar{h}0hl$ ) | ( <i>lhh</i> ) |            |            |             | $I112/a$    |
| ( $h\bar{h}0l$ ) | ( <i>hlh</i> ) |            |            |             |             |