

Hexagonal

6. SCANNING TABLES

 Laue class $D_{6h} - 6/mmm$

 No. 186 $P6_3mc$

$$\mathcal{G} = P6_3mc$$

 C_{6v}^4

Orientation orbit (<i>hkil</i>)	Conventional basis of the scanning group			Scanning group \mathcal{H}	Linear orbit sd	Sectional layer group $\mathcal{L}(sd)$	
(0001)	a	b	c	$P6_3mc$	$[sd, (s + \frac{1}{2})d]$	$p3m1$	L69
(01 $\bar{1}$ 0)	c	a	a + 2b	$A2_1ma$	$[0d, \frac{1}{2}d]$	$p2_1ma$	L28
($\bar{1}$ 010)	c	b	$-(2a + b)$		$[\frac{1}{4}d, \frac{3}{4}d]$	$p2_1mn$	L32
(1 $\bar{1}$ 00)	c	$-(a + b)$	(a - b)		$[\pm sd, (\pm s + \frac{1}{2})d]$	$p1m1$	L11
($\bar{1}$ 2 $\bar{1}$ 0)	c	2a + b	b	$A2_1am$	$[0d, \frac{1}{2}d]$	$p2_1am$	L29
($\bar{1}$ 120)	c	(b - a)	$-(a + b)$		$[\frac{1}{4}d, \frac{3}{4}d]$	$p2_1ab$ (b' /4)	L33
(2 $\bar{1}$ 10)	c	$-(a + 2b)$	a		$[\pm sd, (\pm s + \frac{1}{2})d]$	$p1a1$	L12

 Geometric class $D_{3h} - \bar{6}m2$ and $\bar{6}2m$

 No. 187 $P\bar{6}m2$

$$\mathcal{G} = P\bar{6}m2$$

 D_{3h}^1

Orientation orbit (<i>hkil</i>)	Conventional basis of the scanning group			Scanning group \mathcal{H}	Linear orbit sd	Sectional layer group $\mathcal{L}(sd)$		
(0001)	a	b	c	$P\bar{6}m2$	$0d, \frac{1}{2}d$ $[sd, -sd]$	$p\bar{6}m2$ $p3m1$	L78 L69	
(01 $\bar{1}$ 0)	c	a	a + 2b	$Amm2$	$[sd, (s + \frac{1}{2})d]$	$pmm2$	L23	
($\bar{1}$ 010)	c	b	$-(2a + b)$					
(1 $\bar{1}$ 00)	c	$-(a + b)$	(a - b)					
($\bar{1}$ 2 $\bar{1}$ 0)	c	2a + b	b	$Am2m$	$[0d, \frac{1}{2}d]$	$pm2m$	L27	
($\bar{1}$ 120)	c	(b - a)	$-(a + b)$		$[\frac{1}{4}d, \frac{3}{4}d]$	$pm2_1b$	L28	
(2 $\bar{1}$ 10)	c	$-(a + 2b)$	a		$[\pm sd, (\pm s + \frac{1}{2})d]$	$pm11$	L11	

 No. 188 $P\bar{6}c2$

$$\mathcal{G} = P\bar{6}c2$$

 D_{3h}^2

Orientation orbit (<i>hkil</i>)	Conventional basis of the scanning group			Scanning group \mathcal{H}	Linear orbit sd	Sectional layer group $\mathcal{L}(sd)$		
(0001)	a	b	c	$P\bar{6}c2$	$[0d, \frac{1}{2}d]$ $[\frac{1}{4}d, \frac{3}{4}d]$ $[\pm sd, (\pm s + \frac{1}{2})d]$	$p312$ $p\bar{6}$ $p3$	L67 L74 L65	
(01 $\bar{1}$ 0)	c	a	a + 2b	$Ama2$	$[sd, (s + \frac{1}{2})d]$	$pma2$	L24	
($\bar{1}$ 010)	c	b	$-(2a + b)$					
(1 $\bar{1}$ 00)	c	$-(a + b)$	(a - b)					
($\bar{1}$ 2 $\bar{1}$ 0)	c	2a + b	b	$Am2a$	$[0d, \frac{1}{2}d]$	$pm2a$	L31	
($\bar{1}$ 120)	c	(b - a)	$-(a + b)$		$[\frac{1}{4}d, \frac{3}{4}d]$	$pm2_1n$ (a' /4)	L32	
(2 $\bar{1}$ 10)	c	$-(a + 2b)$	a		$[\pm sd, (\pm s + \frac{1}{2})d]$	$pm11$ (a' /4)	L11	

Auxiliary tables for Laue class $D_{6h} - 6/mmm$

Centring type P

Orientation orbit ($hkil$)	Conventional basis of the scanning group			Auxiliary basis of the scanning group		
	\mathbf{a}'	\mathbf{b}'	\mathbf{d}	$\hat{\mathbf{a}}$	$\hat{\mathbf{b}}$	$\hat{\mathbf{c}}$
$(\overline{mnm} + n0)$	\mathbf{c}	$n\mathbf{a} - m\mathbf{b}$	$p\mathbf{a} + q\mathbf{b}$	\mathbf{a}	\mathbf{b}	\mathbf{c}
$(\overline{m} + \overline{nmn}0)$	\mathbf{c}	$m\mathbf{a} + (m+n)\mathbf{b}$	$-q\mathbf{a} + (p-q)\mathbf{b}$	\mathbf{b}	$-(\mathbf{a} + \mathbf{b})$	\mathbf{c}
$(\overline{nm} + \overline{nm}0)$	\mathbf{c}	$-(m+n)\mathbf{a} - n\mathbf{b}$	$(q-p)\mathbf{a} - p\mathbf{b}$	$-(\mathbf{a} + \mathbf{b})$	\mathbf{a}	\mathbf{c}
$(\overline{nmn} + n0)$	$-\mathbf{c}$	$m\mathbf{a} - n\mathbf{b}$	$-q\mathbf{a} - p\mathbf{b}$	$-\mathbf{b}$	$-\mathbf{a}$	$-\mathbf{c}$
$(\overline{m} + \overline{nm}0)$	\mathbf{c}	$n\mathbf{a} + (m+n)\mathbf{b}$	$p\mathbf{a} + (p-q)\mathbf{b}$	$\mathbf{a} + \mathbf{b}$	$-\mathbf{b}$	$-\mathbf{c}$
$(\overline{mm} + \overline{nn}0)$	$-\mathbf{c}$	$-(m+n)\mathbf{a} - m\mathbf{b}$	$(q-p)\mathbf{a} + q\mathbf{b}$	$-\mathbf{a}$	$\mathbf{a} + \mathbf{b}$	$-\mathbf{c}$
$(0h\overline{hl})$	\mathbf{a}	$n(\mathbf{a} + 2\mathbf{b}) - m\mathbf{c}$	$p(\mathbf{a} + 2\mathbf{b}) + q\mathbf{c}$	$\mathbf{a} + 2\mathbf{b}$	\mathbf{c}	\mathbf{a}
$(0h\overline{h}\overline{l})$	$-\mathbf{a}$	$n(\mathbf{a} + 2\mathbf{b}) + m\mathbf{c}$	$p(\mathbf{a} + 2\mathbf{b}) - q\mathbf{c}$			
$(\overline{h}0hl)$	\mathbf{b}	$-n(2\mathbf{a} + \mathbf{b}) - m\mathbf{c}$	$-p(2\mathbf{a} + \mathbf{b}) + q\mathbf{c}$	$-(2\mathbf{a} + \mathbf{b})$	\mathbf{c}	\mathbf{b}
$(\overline{h}0h\overline{l})$	$-\mathbf{b}$	$-n(2\mathbf{a} + \mathbf{b}) + m\mathbf{c}$	$-p(2\mathbf{a} + \mathbf{b}) - q\mathbf{c}$			
$(h\overline{h}0l)$	$-(\mathbf{a} + \mathbf{b})$	$n(\mathbf{a} - \mathbf{b}) - m\mathbf{c}$	$p(\mathbf{a} - \mathbf{b}) + q\mathbf{c}$	$\mathbf{a} - \mathbf{b}$	\mathbf{c}	$-(\mathbf{a} + \mathbf{b})$
$(h\overline{h}0\overline{l})$	$(\mathbf{a} + \mathbf{b})$	$n(\mathbf{a} - \mathbf{b}) + m\mathbf{c}$	$p(\mathbf{a} - \mathbf{b}) - q\mathbf{c}$			
$l \text{ odd} \Rightarrow n = l, m = 2h; l \text{ even} \Rightarrow n = l/2, m = h$						
$(\overline{h}2h\overline{hl})$	$2\mathbf{a} + \mathbf{b}$	$n\mathbf{b} - m\mathbf{c}$	$p\mathbf{b} + q\mathbf{c}$	\mathbf{b}	\mathbf{c}	$2\mathbf{a} + \mathbf{b}$
$(\overline{h}2h\overline{h}\overline{l})$	$-(2\mathbf{a} + \mathbf{b})$	$n\mathbf{b} + m\mathbf{c}$	$p\mathbf{b} - q\mathbf{c}$			
$(\overline{hh}2hl)$	$\mathbf{b} - \mathbf{a}$	$-n(\mathbf{a} + \mathbf{b}) - m\mathbf{c}$	$-p(\mathbf{a} + \mathbf{b}) + q\mathbf{c}$	$-(\mathbf{a} + \mathbf{b})$	\mathbf{c}	$\mathbf{b} - \mathbf{a}$
$(\overline{hh}2h\overline{l})$	$\mathbf{a} - \mathbf{b}$	$-n(\mathbf{a} + \mathbf{b}) + m\mathbf{c}$	$-p(\mathbf{a} + \mathbf{b}) - q\mathbf{c}$			
$(2h\overline{hhl})$	$-(\mathbf{a} + 2\mathbf{b})$	$n\mathbf{a} - m\mathbf{c}$	$p\mathbf{a} + q\mathbf{c}$	\mathbf{a}	\mathbf{c}	$-\mathbf{a} + 2\mathbf{b}$
$(2h\overline{h}\overline{hl})$	$\mathbf{a} + 2\mathbf{b}$	$n\mathbf{a} + m\mathbf{c}$	$p\mathbf{a} - q\mathbf{c}$			
$l \text{ odd} \Rightarrow n = l, m = 2h; l \text{ even} \Rightarrow n = l/2, m = h$						

Arithmetic class 622P

Serial No.	177	178	179	180	181	182
Group type	D_6^1	D_6^2	D_6^3	D_6^4	D_6^5	D_6^6
Group	$P6_{22}$	$P6_{122}$	$P6_{522}$	$P6_{22}$	$P6_{422}$	$P6_{322}$
$(\overline{mnm} + n0)$	$P112$	$P112_1$	$P112_1$	$P112$	$P112$	$P112_1$
$(\overline{m} + \overline{nmn}0)$						
$(\overline{nm} + \overline{nm}0)$						
$(\overline{nmn} + n0)$						
$(\overline{m} + \overline{nm}0)$						
$(\overline{mm} + \overline{nn}0)$						
Reference group $B112$ with respect to origin at:						
$(0h\overline{hl})$	P	P	P	P	P	P
$(0h\overline{h}\overline{l})$						
$(\overline{h}0hl)$		$P + \mathbf{c}/3$	$P + \mathbf{c}/6$	$P + \mathbf{c}/6$	$P + \mathbf{c}/3$	
$(\overline{h}0h\overline{l})$						
$(h\overline{h}0l)$		$P + \mathbf{c}/6$	$P + \mathbf{c}/3$	$P + \mathbf{c}/3$	$P + \mathbf{c}/6$	
$(h\overline{h}0\overline{l})$						
$(\overline{h}2h\overline{hl})$	P	$P + \mathbf{c}/12$	$P + 5\mathbf{c}/12$	$P + \mathbf{c}/6$	$P + \mathbf{c}/3$	$P + \mathbf{c}/4$
$(\overline{h}2h\overline{h}\overline{l})$						
$(\overline{hh}2hl)$		$P + 5\mathbf{c}/12$	$P + \mathbf{c}/12$	$P + \mathbf{c}/3$	$P + \mathbf{c}/6$	
$(\overline{hh}2h\overline{l})$						
$(2h\overline{hhl})$		$P + \mathbf{c}/4$	$P + \mathbf{c}/4$	P	P	
$(2h\overline{h}\overline{hl})$						

Arithmetic class $6mmP$

Serial No.	183	184	185	186
Group type	C_{6v}^1	C_{6v}^2	C_{6v}^3	C_{6v}^4
Group	$P6mm$	$P6cc$	$P6_3cm$	$P6_3mc$
$(\overline{mnm} + n0)$	$P112$	$P112$	$P112_1$	$P112_1$
$(\overline{m} + nmn0)$				
$(\overline{nm} + nm0)$				
$(\overline{mmm} + n0)$				
$(\overline{m} + nmn0)$				
$(\overline{mm} + nn0)$				
$(0h\overline{hl})$	$B11m$	$B11b$	$B11b$	$B11m$
$(0h\overline{h\overline{l}})$				
$(\overline{h}0hl)$				
$(\overline{h}0h\overline{l})$				
$(h\overline{h}0l)$				
$(h\overline{h}0\overline{l})$				
$(\overline{h}2h\overline{hl})$	$B11m$	$B11b$	$B11m$	$B11b$
$(\overline{h}2h\overline{h\overline{l}})$				
$(\overline{h\overline{h}}2hl)$				
$(\overline{h\overline{h}}2h\overline{l})$				
$(2h\overline{h\overline{hl}})$				
$(2h\overline{h\overline{h\overline{l}}})$				

Arithmetic classes $\overline{6}m2P$ and $\overline{6}2mP$

Serial No.	187	188	189	190
Group type	D_{3h}^1	D_{3h}^2	D_{3h}^3	D_{3h}^4
Group	$P\overline{6}m2$	$P\overline{6}c2$	$P\overline{6}2m$	$P\overline{6}2c$
$(\overline{mnm} + n0)$	$P11m$	$P11m$	$P11m$	$P11m$
$(\overline{m} + nmn0)$		$(c/4)$		$(c/4)$
$(\overline{nm} + nm0)$				
$(\overline{mmm} + n0)$				
$(\overline{m} + nmn0)$				
$(\overline{mm} + nn0)$				
$(0h\overline{hl})$	$B11m$	$B11b$	$B112$	$B112$
$(0h\overline{h\overline{l}})$				
$(\overline{h}0hl)$				
$(\overline{h}0h\overline{l})$				
$(h\overline{h}0l)$				
$(h\overline{h}0\overline{l})$				
$(\overline{h}2h\overline{hl})$	$B112$	$B112$	$B11m$	$B11b$
$(\overline{h}2h\overline{h\overline{l}})$				
$(\overline{h\overline{h}}2hl)$				
$(\overline{h\overline{h}}2h\overline{l})$				
$(2h\overline{h\overline{hl}})$				
$(2h\overline{h\overline{h\overline{l}}})$				