

Laue class $D_{6h} - 6/mmm$

6. SCANNING TABLES

Hexagonal

 No. 189 $P\bar{6}2m$

$$\mathcal{G} = P\bar{6}2m$$

 D_{3h}^3

Orientation orbit (<i>hkl</i>)	Conventional basis of the scanning group			Scanning group \mathcal{H}	Linear orbit \mathbf{sd}	Sectional layer group $\mathcal{L}(\mathbf{sd})$	
	\mathbf{a}'	\mathbf{b}'	\mathbf{d}				
(0001)	\mathbf{a}	\mathbf{b}	\mathbf{c}	$P\bar{6}2m$	$0\mathbf{d}, \frac{1}{2}\mathbf{d}$ $[\mathbf{sd}, -\mathbf{sd}]$	$p\bar{6}2m$ $p31m$	L79 L70
(01 $\bar{1}$ 0)	\mathbf{c}	\mathbf{a}	$\mathbf{a} + 2\mathbf{b}$	$Am2m$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pm2m$ $pm2_1b$ $pm11$	L27 L28 L11
($\bar{1}$ 010)	\mathbf{c}	\mathbf{b}	$-(2\mathbf{a} + \mathbf{b})$				
(1 $\bar{1}$ 00)	\mathbf{c}	$-(\mathbf{a} + \mathbf{b})$	$(\mathbf{a} - \mathbf{b})$				
($\bar{1}$ 2 $\bar{1}$ 0)	\mathbf{c}	$2\mathbf{a} + \mathbf{b}$	\mathbf{b}	$Amm2$	$[\mathbf{sd}, (s + \frac{1}{2})\mathbf{d}]$	$pmm2$	L23
($\bar{1}$ 120)	\mathbf{c}	$(\mathbf{b} - \mathbf{a})$	$-(\mathbf{a} + \mathbf{b})$				
(2 $\bar{1}$ 10)	\mathbf{c}	$-(\mathbf{a} + 2\mathbf{b})$	\mathbf{a}				

 No. 190 $P\bar{6}2c$

$$\mathcal{G} = P\bar{6}2c$$

 D_{3h}^4

Orientation orbit (<i>hkl</i>)	Conventional basis of the scanning group			Scanning group \mathcal{H}	Linear orbit \mathbf{sd}	Sectional layer group $\mathcal{L}(\mathbf{sd})$	
	\mathbf{a}'	\mathbf{b}'	\mathbf{d}				
(0001)	\mathbf{a}	\mathbf{b}	\mathbf{c}	$P\bar{6}2c$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$	$p321$ $p\bar{6}$ $p3$	L68 L74 L65
(01 $\bar{1}$ 0)	\mathbf{c}	\mathbf{a}	$\mathbf{a} + 2\mathbf{b}$	$Am2a$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pm2a$ $pm2_1n (\mathbf{a}'/4)$ $pm11 (\mathbf{a}'/4)$	L31 L32 L11
($\bar{1}$ 010)	\mathbf{c}	\mathbf{b}	$-(2\mathbf{a} + \mathbf{b})$				
(1 $\bar{1}$ 00)	\mathbf{c}	$-(\mathbf{a} + \mathbf{b})$	$(\mathbf{a} - \mathbf{b})$				
($\bar{1}$ 2 $\bar{1}$ 0)	\mathbf{c}	$2\mathbf{a} + \mathbf{b}$	\mathbf{b}	$Ama2$	$[\mathbf{sd}, (s + \frac{1}{2})\mathbf{d}]$	$pma2$	L24
($\bar{1}$ 120)	\mathbf{c}	$(\mathbf{b} - \mathbf{a})$	$-(\mathbf{a} + \mathbf{b})$				
(2 $\bar{1}$ 10)	\mathbf{c}	$-(\mathbf{a} + 2\mathbf{b})$	\mathbf{a}				

Geometric class $D_{6h} - 6/mmm$

 No. 191 $P6/mmm$

$$\mathcal{G} = P6\frac{6}{m}\frac{2}{m}\frac{2}{m}$$

 D_{6h}^1

Orientation orbit (<i>hkl</i>)	Conventional basis of the scanning group			Scanning group \mathcal{H}	Linear orbit \mathbf{sd}	Sectional layer group $\mathcal{L}(\mathbf{sd})$	
	\mathbf{a}'	\mathbf{b}'	\mathbf{d}				
(0001)	\mathbf{a}	\mathbf{b}	\mathbf{c}	$P6/mmm$	$0\mathbf{d}, \frac{1}{2}\mathbf{d}$ $[\mathbf{sd}, -\mathbf{sd}]$	$p6/mmm$ $p6mm$	L80 L77
(01 $\bar{1}$ 0)	\mathbf{c}	\mathbf{a}	$\mathbf{a} + 2\mathbf{b}$	$Ammm$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pmmm$ $pmm\mathbf{b} (\mathbf{b}'/4)$ $pmm2$	L37 L41 L23
($\bar{1}$ 010)	\mathbf{c}	\mathbf{b}	$-(2\mathbf{a} + \mathbf{b})$				
(1 $\bar{1}$ 00)	\mathbf{c}	$-(\mathbf{a} + \mathbf{b})$	$(\mathbf{a} - \mathbf{b})$				
($\bar{1}$ 2 $\bar{1}$ 0)	\mathbf{c}	$2\mathbf{a} + \mathbf{b}$	\mathbf{b}	$Ammm$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm\mathbf{sd}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pmmm$ $pmm\mathbf{b} (\mathbf{b}'/4)$ $pmm2$	L37 L41 L23
($\bar{1}$ 120)	\mathbf{c}	$(\mathbf{b} - \mathbf{a})$	$-(\mathbf{a} + \mathbf{b})$				
(2 $\bar{1}$ 10)	\mathbf{c}	$-(\mathbf{a} + 2\mathbf{b})$	\mathbf{a}				

Auxiliary tables for Laue class $D_{6h} - 6/mmm$

Centring type P

Orientation orbit ($hkil$)	Conventional basis of the scanning group			Auxiliary basis of the scanning group		
	\mathbf{a}'	\mathbf{b}'	\mathbf{d}	$\hat{\mathbf{a}}$	$\hat{\mathbf{b}}$	$\hat{\mathbf{c}}$
$(\overline{mnm} + n0)$	\mathbf{c}	$n\mathbf{a} - m\mathbf{b}$	$p\mathbf{a} + q\mathbf{b}$	\mathbf{a}	\mathbf{b}	\mathbf{c}
$(\overline{m} + \overline{nmn}0)$	\mathbf{c}	$m\mathbf{a} + (m+n)\mathbf{b}$	$-q\mathbf{a} + (p-q)\mathbf{b}$	\mathbf{b}	$-(\mathbf{a} + \mathbf{b})$	\mathbf{c}
$(\overline{nm} + \overline{nm}0)$	\mathbf{c}	$-(m+n)\mathbf{a} - n\mathbf{b}$	$(q-p)\mathbf{a} - p\mathbf{b}$	$-(\mathbf{a} + \mathbf{b})$	\mathbf{a}	\mathbf{c}
$(\overline{nmn} + n0)$	$-\mathbf{c}$	$m\mathbf{a} - n\mathbf{b}$	$-q\mathbf{a} - p\mathbf{b}$	$-\mathbf{b}$	$-\mathbf{a}$	$-\mathbf{c}$
$(\overline{m} + \overline{nm}0)$	\mathbf{c}	$n\mathbf{a} + (m+n)\mathbf{b}$	$p\mathbf{a} + (p-q)\mathbf{b}$	$\mathbf{a} + \mathbf{b}$	$-\mathbf{b}$	$-\mathbf{c}$
$(\overline{mm} + \overline{nn}0)$	$-\mathbf{c}$	$-(m+n)\mathbf{a} - m\mathbf{b}$	$(q-p)\mathbf{a} + q\mathbf{b}$	$-\mathbf{a}$	$\mathbf{a} + \mathbf{b}$	$-\mathbf{c}$
$(0h\overline{hl})$	\mathbf{a}	$n(\mathbf{a} + 2\mathbf{b}) - m\mathbf{c}$	$p(\mathbf{a} + 2\mathbf{b}) + q\mathbf{c}$	$\mathbf{a} + 2\mathbf{b}$	\mathbf{c}	\mathbf{a}
$(0h\overline{h}\overline{l})$	$-\mathbf{a}$	$n(\mathbf{a} + 2\mathbf{b}) + m\mathbf{c}$	$p(\mathbf{a} + 2\mathbf{b}) - q\mathbf{c}$			
$(\overline{h}0hl)$	\mathbf{b}	$-n(2\mathbf{a} + \mathbf{b}) - m\mathbf{c}$	$-p(2\mathbf{a} + \mathbf{b}) + q\mathbf{c}$	$-(2\mathbf{a} + \mathbf{b})$	\mathbf{c}	\mathbf{b}
$(\overline{h}0h\overline{l})$	$-\mathbf{b}$	$-n(2\mathbf{a} + \mathbf{b}) + m\mathbf{c}$	$-p(2\mathbf{a} + \mathbf{b}) - q\mathbf{c}$			
$(h\overline{h}0l)$	$-(\mathbf{a} + \mathbf{b})$	$n(\mathbf{a} - \mathbf{b}) - m\mathbf{c}$	$p(\mathbf{a} - \mathbf{b}) + q\mathbf{c}$	$\mathbf{a} - \mathbf{b}$	\mathbf{c}	$-(\mathbf{a} + \mathbf{b})$
$(h\overline{h}0\overline{l})$	$(\mathbf{a} + \mathbf{b})$	$n(\mathbf{a} - \mathbf{b}) + m\mathbf{c}$	$p(\mathbf{a} - \mathbf{b}) - q\mathbf{c}$			
$l \text{ odd} \Rightarrow n = l, m = 2h; l \text{ even} \Rightarrow n = l/2, m = h$						
$(\overline{h}2h\overline{hl})$	$2\mathbf{a} + \mathbf{b}$	$n\mathbf{b} - m\mathbf{c}$	$p\mathbf{b} + q\mathbf{c}$	\mathbf{b}	\mathbf{c}	$2\mathbf{a} + \mathbf{b}$
$(\overline{h}2h\overline{h}\overline{l})$	$-(2\mathbf{a} + \mathbf{b})$	$n\mathbf{b} + m\mathbf{c}$	$p\mathbf{b} - q\mathbf{c}$			
$(\overline{hh}2hl)$	$\mathbf{b} - \mathbf{a}$	$-n(\mathbf{a} + \mathbf{b}) - m\mathbf{c}$	$-p(\mathbf{a} + \mathbf{b}) + q\mathbf{c}$	$-(\mathbf{a} + \mathbf{b})$	\mathbf{c}	$\mathbf{b} - \mathbf{a}$
$(\overline{hh}2h\overline{l})$	$\mathbf{a} - \mathbf{b}$	$-n(\mathbf{a} + \mathbf{b}) + m\mathbf{c}$	$-p(\mathbf{a} + \mathbf{b}) - q\mathbf{c}$			
$(2h\overline{h}hl)$	$-(\mathbf{a} + 2\mathbf{b})$	$n\mathbf{a} - m\mathbf{c}$	$p\mathbf{a} + q\mathbf{c}$	\mathbf{a}	\mathbf{c}	$-\mathbf{a} + 2\mathbf{b}$
$(2h\overline{h}\overline{h}\overline{l})$	$\mathbf{a} + 2\mathbf{b}$	$n\mathbf{a} + m\mathbf{c}$	$p\mathbf{a} - q\mathbf{c}$			
$l \text{ odd} \Rightarrow n = l, m = 2h; l \text{ even} \Rightarrow n = l/2, m = h$						

Arithmetic class 622P

Serial No.	177	178	179	180	181	182
Group type	D_6^1	D_6^2	D_6^3	D_6^4	D_6^5	D_6^6
Group	$P6_{22}$	$P6_122$	$P6_522$	$P6_222$	$P6_422$	$P6_322$
$(\overline{mnm} + n0)$	$P112$	$P112_1$	$P112_1$	$P112$	$P112$	$P112_1$
$(\overline{m} + \overline{nmn}0)$						
$(\overline{nm} + \overline{nm}0)$						
$(\overline{nmn} + n0)$						
$(\overline{m} + \overline{nm}0)$						
$(\overline{mm} + \overline{nn}0)$						
Reference group $B112$ with respect to origin at:						
$(0h\overline{hl})$	P	P	P	P	P	P
$(0h\overline{h}\overline{l})$						
$(\overline{h}0hl)$		$P + \mathbf{c}/3$	$P + \mathbf{c}/6$	$P + \mathbf{c}/6$	$P + \mathbf{c}/3$	
$(\overline{h}0h\overline{l})$						
$(h\overline{h}0l)$		$P + \mathbf{c}/6$	$P + \mathbf{c}/3$	$P + \mathbf{c}/3$	$P + \mathbf{c}/6$	
$(h\overline{h}0\overline{l})$						
$(\overline{h}2h\overline{hl})$	P	$P + \mathbf{c}/12$	$P + 5\mathbf{c}/12$	$P + \mathbf{c}/6$	$P + \mathbf{c}/3$	$P + \mathbf{c}/4$
$(\overline{h}2h\overline{h}\overline{l})$						
$(\overline{hh}2hl)$		$P + 5\mathbf{c}/12$	$P + \mathbf{c}/12$	$P + \mathbf{c}/3$	$P + \mathbf{c}/6$	
$(\overline{hh}2h\overline{l})$						
$(2h\overline{h}hl)$		$P + \mathbf{c}/4$	$P + \mathbf{c}/4$	P	P	
$(2h\overline{h}\overline{h}\overline{l})$						

Arithmetic class $6mmP$

Serial No.	183	184	185	186
Group type	C_{6v}^1	C_{6v}^2	C_{6v}^3	C_{6v}^4
Group	$P6mm$	$P6cc$	$P6_3cm$	$P6_3mc$
$(\overline{mnm} + n0)$	$P112$	$P112$	$P112_1$	$P112_1$
$(\overline{m} + nmn0)$				
$(\overline{nm} + nm0)$				
$(\overline{mmm} + n0)$				
$(\overline{m} + nmn0)$				
$(\overline{mm} + nn0)$				
$(0h\overline{hl})$	$B11m$	$B11b$	$B11b$	$B11m$
$(0h\overline{h\overline{l}})$				
$(\overline{h}0hl)$				
$(\overline{h}0h\overline{l})$				
$(h\overline{h}0l)$				
$(h\overline{h}0\overline{l})$				
$(\overline{h}2h\overline{hl})$	$B11m$	$B11b$	$B11m$	$B11b$
$(\overline{h}2h\overline{h\overline{l}})$				
$(\overline{h\overline{h}}2hl)$				
$(\overline{h\overline{h}}2h\overline{l})$				
$(2h\overline{h\overline{hl}})$				
$(2h\overline{h\overline{h\overline{l}}})$				

Arithmetic classes $\overline{6}m2P$ and $\overline{6}2mP$

Serial No.	187	188	189	190
Group type	D_{3h}^1	D_{3h}^2	D_{3h}^3	D_{3h}^4
Group	$P\overline{6}m2$	$P\overline{6}c2$	$P\overline{6}2m$	$P\overline{6}2c$
$(\overline{mnm} + n0)$	$P11m$	$P11m$	$P11m$	$P11m$
$(\overline{m} + nmn0)$		$(c/4)$		$(c/4)$
$(\overline{nm} + nm0)$				
$(\overline{mmm} + n0)$				
$(\overline{m} + nmn0)$				
$(\overline{mm} + nn0)$				
$(0h\overline{hl})$	$B11m$	$B11b$	$B112$	$B112$
$(0h\overline{h\overline{l}})$				
$(\overline{h}0hl)$				
$(\overline{h}0h\overline{l})$				
$(h\overline{h}0l)$				
$(h\overline{h}0\overline{l})$				
$(\overline{h}2h\overline{hl})$	$B112$	$B112$	$B11m$	$B11b$
$(\overline{h}2h\overline{h\overline{l}})$				
$(\overline{h\overline{h}}2hl)$				
$(\overline{h\overline{h}}2h\overline{l})$				
$(2h\overline{h\overline{hl}})$				
$(2h\overline{h\overline{h\overline{l}}})$				