

Hexagonal

6. SCANNING TABLES

Laue class $D_{6h} - 6/mmm$ No. 192 $P6/mcc$

$$\mathcal{G} = P6_{m\ c\ c}^{\underline{6}\ \underline{2}\ \underline{2}}$$

 D_{6h}^2

Orientation orbit ($hkil$)	Conventional basis of the scanning group \mathbf{a}' \mathbf{b}' \mathbf{d}	Scanning group \mathcal{H}	Linear orbit $s\mathbf{d}$	Sectional layer group $\mathcal{L}(s\mathbf{d})$	
(0001)	\mathbf{a} \mathbf{b} \mathbf{c}	$P6/mcc$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$p6/m$ $p622$ $p6$	L75 L76 L73
(0110)	\mathbf{c} \mathbf{a} $\mathbf{a} + 2\mathbf{b}$	<i>Amaa</i>	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$	$pmaa$	L38
(1010)	\mathbf{c} \mathbf{b} $-(2\mathbf{a} + \mathbf{b})$		$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$	$pman(\mathbf{b}'/4)$	L42
(1100)	\mathbf{c} $-(\mathbf{a} + \mathbf{b})$ $(\mathbf{a} - \mathbf{b})$		$[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pma2(\mathbf{a}'/4)$	L24
(1210)	\mathbf{c} $2\mathbf{a} + \mathbf{b}$ \mathbf{b}	<i>Amaa</i>	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$	$pmaa$	L38
(1120)	\mathbf{c} $(\mathbf{b} - \mathbf{a})$ $-(\mathbf{a} + \mathbf{b})$		$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$	$pman(\mathbf{b}'/4)$	L42
(2110)	\mathbf{c} $-(\mathbf{a} + 2\mathbf{b})$ \mathbf{a}		$[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pma2(\mathbf{a}'/4)$	L24

No. 193 $P6_3/mcm$

$$\mathcal{G} = P6_{m\ c\ m}^{\underline{6}_3\ \underline{2}\ \underline{2}}$$

 D_{6h}^3

Orientation orbit ($hkil$)	Conventional basis of the scanning group \mathbf{a}' \mathbf{b}' \mathbf{d}	Scanning group \mathcal{H}	Linear orbit $s\mathbf{d}$	Sectional layer group $\mathcal{L}(s\mathbf{d})$	
(0001)	\mathbf{a} \mathbf{b} \mathbf{c}	$P6_3/mcm$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$p\bar{3}1m$ $p\bar{6}2m$ $p31m$	L71 L79 L70
(0110)	\mathbf{c} \mathbf{a} $\mathbf{a} + 2\mathbf{b}$	<i>Amam</i>	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$	$pmam$	L40
(1010)	\mathbf{c} \mathbf{b} $-(2\mathbf{a} + \mathbf{b})$		$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$	$pmab(\mathbf{b}'/4)$	L45
(1100)	\mathbf{c} $-(\mathbf{a} + \mathbf{b})$ $(\mathbf{a} - \mathbf{b})$		$[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pma2$	L24
(1210)	\mathbf{c} $2\mathbf{a} + \mathbf{b}$ \mathbf{b}	<i>Amma</i>	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$	$pmma$	L41
(1120)	\mathbf{c} $(\mathbf{b} - \mathbf{a})$ $-(\mathbf{a} + \mathbf{b})$		$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$	$pmmn(\mathbf{b}'/4)$	L46
(2110)	\mathbf{c} $-(\mathbf{a} + 2\mathbf{b})$ \mathbf{a}		$[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pmm2(\mathbf{a}'/4)$	L23

No. 194 $P6_3/mmc$

$$\mathcal{G} = P6_{m\ m\ c}^{\underline{6}_3\ \underline{2}\ \underline{2}}$$

 D_{6h}^4

Orientation orbit ($hkil$)	Conventional basis of the scanning group \mathbf{a}' \mathbf{b}' \mathbf{d}	Scanning group \mathcal{H}	Linear orbit $s\mathbf{d}$	Sectional layer group $\mathcal{L}(s\mathbf{d})$	
(0001)	\mathbf{a} \mathbf{b} \mathbf{c}	$P6_3/mmc$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$ $[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$ $[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$p\bar{3}m1$ $p\bar{6}m2$ $p3m1$	L72 L78 L69
(0110)	\mathbf{c} \mathbf{a} $\mathbf{a} + 2\mathbf{b}$	<i>Amma</i>	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$	$pmma$	L41
(1010)	\mathbf{c} \mathbf{b} $-(2\mathbf{a} + \mathbf{b})$		$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$	$pmmn(\mathbf{b}'/4)$	L46
(1100)	\mathbf{c} $-(\mathbf{a} + \mathbf{b})$ $(\mathbf{a} - \mathbf{b})$		$[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pmm2(\mathbf{a}'/4)$	L23
(1210)	\mathbf{c} $2\mathbf{a} + \mathbf{b}$ \mathbf{b}	<i>Amam</i>	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$	$pmam$	L40
(1120)	\mathbf{c} $(\mathbf{b} - \mathbf{a})$ $-(\mathbf{a} + \mathbf{b})$		$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$	$pmab(\mathbf{b}'/4)$	L45
(2110)	\mathbf{c} $-(\mathbf{a} + 2\mathbf{b})$ \mathbf{a}		$[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$pma2$	L24

Auxiliary tables for Laue class $D_{6h} - 6/mmm$

Centring type P

Orientation orbit ($hkil$)	Conventional basis of the scanning group			Auxiliary basis of the scanning group		
	\mathbf{a}'	\mathbf{b}'	\mathbf{d}	$\widehat{\mathbf{a}}$	$\widehat{\mathbf{b}}$	$\widehat{\mathbf{c}}$
$(nnm + \bar{n}0)$	\mathbf{c}	$n\mathbf{a} - m\mathbf{b}$	$p\mathbf{a} + q\mathbf{b}$	\mathbf{a}	\mathbf{b}	\mathbf{c}
$(\bar{m} + nmn0)$	\mathbf{c}	$m\mathbf{a} + (m+n)\mathbf{b}$	$-q\mathbf{a} + (p-q)\mathbf{b}$	\mathbf{b}	$-(\mathbf{a} + \mathbf{b})$	\mathbf{c}
$(\bar{n}m + nm0)$	\mathbf{c}	$-(m+n)\mathbf{a} - n\mathbf{b}$	$(q-p)\mathbf{a} - p\mathbf{b}$	$-(\mathbf{a} + \mathbf{b})$	\mathbf{a}	\mathbf{c}
$(nmm + \bar{n}0)$	$-\mathbf{c}$	$m\mathbf{a} - n\mathbf{b}$	$-q\mathbf{a} - p\mathbf{b}$	$-\mathbf{b}$	$-\mathbf{a}$	$-\mathbf{c}$
$(\bar{m} + nnm0)$	\mathbf{c}	$n\mathbf{a} + (m+n)\mathbf{b}$	$p\mathbf{a} + (p-q)\mathbf{b}$	$\mathbf{a} + \mathbf{b}$	$-\mathbf{b}$	$-\mathbf{c}$
$(\bar{m}m + nn0)$	$-\mathbf{c}$	$-(m+n)\mathbf{a} - mb$	$(q-p)\mathbf{a} + qb$	$-\mathbf{a}$	$\mathbf{a} + \mathbf{b}$	$-\mathbf{c}$
$(0hh\bar{l})$	\mathbf{a}	$n(\mathbf{a} + 2\mathbf{b}) - mc$	$p(\mathbf{a} + 2\mathbf{b}) + qc$	$\mathbf{a} + 2\mathbf{b}$	\mathbf{c}	\mathbf{a}
$(0\bar{h}\bar{h}\bar{l})$	$-\mathbf{a}$	$n(\mathbf{a} + 2\mathbf{b}) + mc$	$p(\mathbf{a} + 2\mathbf{b}) - qc$			
$(\bar{h}0h\bar{l})$	\mathbf{b}	$-n(2\mathbf{a} + \mathbf{b}) - mc$	$-p(2\mathbf{a} + \mathbf{b}) + qc$	$-(2\mathbf{a} + \mathbf{b})$	\mathbf{c}	\mathbf{b}
$(\bar{h}0\bar{h}\bar{l})$	$-\mathbf{b}$	$-n(2\mathbf{a} + \mathbf{b}) + mc$	$-p(2\mathbf{a} + \mathbf{b}) - qc$			
$(h\bar{h}0l)$	$-(\mathbf{a} + \mathbf{b})$	$n(\mathbf{a} - \mathbf{b}) - mc$	$p(\mathbf{a} - \mathbf{b}) + qc$	$\mathbf{a} - \mathbf{b}$	\mathbf{c}	$-(\mathbf{a} + \mathbf{b})$
$(h\bar{h}0\bar{l})$	$(\mathbf{a} + \mathbf{b})$	$n(\mathbf{a} - \mathbf{b}) + mc$	$p(\mathbf{a} - \mathbf{b}) - qc$			
l odd $\Rightarrow n = l, m = 2h; l$ even $\Rightarrow n = l/2, m = h$						
$(\bar{h}2h\bar{h}\bar{l})$	$2\mathbf{a} + \mathbf{b}$	$n\mathbf{b} - mc$	$p\mathbf{b} + qc$	\mathbf{b}	\mathbf{c}	$2\mathbf{a} + \mathbf{b}$
$(\bar{h}2h\bar{h}l)$	$-(2\mathbf{a} + \mathbf{b})$	$n\mathbf{b} + mc$	$p\mathbf{b} - qc$			
$(\bar{h}h2\bar{h}l)$	$\mathbf{b} - \mathbf{a}$	$-n(\mathbf{a} + \mathbf{b}) - mc$	$-p(\mathbf{a} + \mathbf{b}) + qc$	$-(\mathbf{a} + \mathbf{b})$	\mathbf{c}	$\mathbf{b} - \mathbf{a}$
$(\bar{h}h2\bar{h}\bar{l})$	$\mathbf{a} - \mathbf{b}$	$-n(\mathbf{a} + \mathbf{b}) + mc$	$-p(\mathbf{a} + \mathbf{b}) - qc$			
$(2\bar{h}h\bar{h}l)$	$-(\mathbf{a} + 2\mathbf{b})$	$n\mathbf{a} - mc$	$p\mathbf{a} + qc$	\mathbf{a}	\mathbf{c}	$-\mathbf{a} + 2\mathbf{b}$
$(2\bar{h}h\bar{h}\bar{l})$	$\mathbf{a} + 2\mathbf{b}$	$n\mathbf{a} + mc$	$p\mathbf{a} - qc$			
l odd $\Rightarrow n = l, m = 2h; l$ even $\Rightarrow n = l/2, m = h$						

Arithmetic class $622P$

Serial No.	177	178	179	180	181	182	
Group type	D_6^1	D_6^2	D_6^3	D_6^4	D_6^5	D_6^6	
Group	$P622$	$P6_122$	$P6_522$	$P6_222$	$P6_422$	$P6_322$	
$(nnm + \bar{n}0)$	$P112$	$P112_1$	$P112_1$	$P112$	$P112$	$P112_1$	
$(\bar{m} + nmn0)$							
$(\bar{n}m + nm0)$							
$(\bar{n}nm + \bar{n}0)$							
$(m + nnm0)$							
$(\bar{m}m + nn0)$							
Reference group $B112$ with respect to origin at:							
$(0h\bar{h}l)$	P	P	P	P	P	P	
$(0\bar{h}\bar{h}\bar{l})$		$P + \mathbf{c}/3$	$P + \mathbf{c}/6$	$P + \mathbf{c}/6$	$P + \mathbf{c}/3$		
$(\bar{h}0h\bar{l})$		$P + \mathbf{c}/6$	$P + \mathbf{c}/3$	$P + \mathbf{c}/3$	$P + \mathbf{c}/6$		
$(\bar{h}\bar{h}0l)$							
$(\bar{h}\bar{h}0\bar{l})$							
$(\bar{h}2h\bar{h}\bar{l})$	P	$P + \mathbf{c}/12$	$P + 5\mathbf{c}/12$	$P + \mathbf{c}/6$	$P + \mathbf{c}/3$	$P + \mathbf{c}/4$	
$(\bar{h}2h\bar{h}l)$		$P + 5\mathbf{c}/12$	$P + \mathbf{c}/12$	$P + \mathbf{c}/3$	$P + \mathbf{c}/6$		
$(\bar{h}h2\bar{h}l)$		$P + \mathbf{c}/4$	$P + \mathbf{c}/4$	P	P		
$(\bar{h}h2\bar{h}\bar{l})$							
$(2\bar{h}h\bar{h}l)$							
$(2\bar{h}h\bar{h}\bar{l})$							

Arithmetic class $6/mmmP$

Serial No.	191 D_{6h}^1 $P6/mmm$	192 D_{6h}^2 $P6/mcc$	193 D_{6h}^3 $P6_3/mcm$	194 D_{6h}^4 $P6_3/mmc$
$(mnm + \bar{n}0)$	$P112/m$	$P112/m$	$P112_1/m$	$P112_1/m$
$(\bar{m} + nm\bar{n}0)$				
$(\bar{nm} + nm0)$				
$(nmm + \bar{n}0)$				
$(m + nnm\bar{n}0)$				
$(\bar{mm} + \bar{nn}0)$				
$(0h\bar{h}l)$	$B112/m$	$B112/b$	$B112/b$	$B112/m$
$(0h\bar{h}\bar{l})$				
$(\bar{h}0h\bar{l})$				
$(\bar{h}0\bar{h}\bar{l})$				
$(h\bar{h}0l)$				
$(h\bar{h}0\bar{l})$				
$(\bar{h}2h\bar{h}l)$	$B112/m$	$B112/b$	$B112/m$	$B112/b$
$(\bar{h}2h\bar{h}\bar{l})$				
$(\bar{h}\bar{h}2h\bar{l})$				
$(\bar{h}\bar{h}2\bar{h}\bar{l})$				
$(2h\bar{h}h\bar{l})$				
$(2h\bar{h}h\bar{l})$				