

Cubic

6. SCANNING TABLES

 Laue class $O_h - m\bar{3}m$

 Centring type F

Orientation orbit (hkl)	Conventional basis of the scanning group			Auxiliary basis of the scanning group		
	\mathbf{a}'	\mathbf{b}'	\mathbf{d}	$\hat{\mathbf{a}}$	$\hat{\mathbf{b}}$	$\hat{\mathbf{c}}$
($hk0$)	\mathbf{c}	$n\hat{\mathbf{a}} - m\hat{\mathbf{b}}$	$p\hat{\mathbf{a}} + q\hat{\mathbf{b}}$	$(\mathbf{a} - \mathbf{b})/2$	$(\mathbf{a} + \mathbf{b})/2$	\mathbf{c}
($\bar{h}k0$)	\mathbf{c}	$n\hat{\mathbf{a}} + m\hat{\mathbf{b}}$	$-p\hat{\mathbf{a}} + q\hat{\mathbf{b}}$			
($0hk$)	\mathbf{a}	$n\hat{\mathbf{a}} - m\hat{\mathbf{b}}$	$p\hat{\mathbf{a}} + q\hat{\mathbf{b}}$	$(\mathbf{b} - \mathbf{c})/2$	$(\mathbf{b} + \mathbf{c})/2$	\mathbf{a}
($0\bar{h}k$)	\mathbf{a}	$n\hat{\mathbf{a}} + m\hat{\mathbf{b}}$	$-p\hat{\mathbf{a}} + q\hat{\mathbf{b}}$			
($k0h$)	\mathbf{b}	$n\hat{\mathbf{a}} - m\hat{\mathbf{b}}$	$p\hat{\mathbf{a}} + q\hat{\mathbf{b}}$	$(\mathbf{c} - \mathbf{a})/2$	$(\mathbf{c} + \mathbf{a})/2$	\mathbf{b}
($k0\bar{h}$)	\mathbf{b}	$n\hat{\mathbf{a}} + m\hat{\mathbf{b}}$	$-p\hat{\mathbf{a}} + q\hat{\mathbf{b}}$			

h even, k odd or h odd, k even $\Rightarrow n = h + k, m = h - k$
 h, k odd $\Rightarrow n = (h + k)/2, m = (h - k)/2$

 Arithmetic classes $23F$ and $m\bar{3}F$

Serial No. Group type Group	196 T^2 $F23$	202 T_h^3 $Fm\bar{3}$	203 T_h^4 $Fd\bar{3}$	
			Origin 1	Origin 2
($hk0$)	$I112$	$I112/m$	$I112/b$	$I112/b$
($\bar{h}k0$)			$(\mathbf{a} + \mathbf{b} + \mathbf{c})/8$	
($0hk$)				
($0\bar{h}k$)				
($k0h$)				
($k0\bar{h}$)				

 Laue class $O_h - m\bar{3}m$

 Geometric class $O - 432$

 No. 207 $P432$
 $\mathcal{G} = P432$
 O^1

Orientation orbit (hkl)	Conventional basis of the scanning group			Scanning group \mathcal{H}	Linear orbit $s\mathbf{d}$	Sectional layer group $\mathcal{L}(s\mathbf{d})$
	\mathbf{a}'	\mathbf{b}'	\mathbf{d}			
(001)	\mathbf{a}	\mathbf{b}	\mathbf{c}	$P432$	$0\mathbf{d}, \frac{1}{2}\mathbf{d}$	$p422$ L53
(100)	\mathbf{b}	\mathbf{c}	\mathbf{a}		$[s\mathbf{d}, -s\mathbf{d}]$	$p4$ L49
(010)	\mathbf{c}	\mathbf{a}	\mathbf{b}			
(110)	\mathbf{c}	$\mathbf{a} - \mathbf{b}$	$\mathbf{a} + \mathbf{b}$	$A232$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}]$	$p222$ L19
($\bar{1}\bar{1}0$)	\mathbf{c}	$\mathbf{a} + \mathbf{b}$	$\mathbf{b} - \mathbf{a}$		$[\frac{1}{4}\mathbf{d}, \frac{3}{4}\mathbf{d}]$	$p22_12$ L20
(011)	\mathbf{a}	$\mathbf{b} - \mathbf{c}$	$\mathbf{b} + \mathbf{c}$		$[\pm s\mathbf{d}, (\pm s + \frac{1}{2})\mathbf{d}]$	$p112$ L03
($0\bar{1}\bar{1}$)	\mathbf{a}	$\mathbf{b} + \mathbf{c}$	$\mathbf{c} - \mathbf{b}$			
(101)	\mathbf{b}	$\mathbf{c} - \mathbf{a}$	$\mathbf{c} + \mathbf{a}$			
($\bar{1}0\bar{1}$)	\mathbf{b}	$\mathbf{c} + \mathbf{a}$	$\mathbf{a} - \mathbf{c}$			
(111)	$\mathbf{a} - \mathbf{b}$	$\mathbf{b} - \mathbf{c}$	$\boldsymbol{\tau}$	$R32$	$[0\mathbf{d}, \frac{1}{2}\mathbf{d}, \frac{1}{3}\mathbf{d}, \frac{2}{3}\mathbf{d}]$	$p321$ L68
($\bar{1}\bar{1}\bar{1}$)	$\mathbf{b} - \mathbf{a}$	$-\mathbf{b} - \mathbf{c}$	$\boldsymbol{\tau}_3$		$[\frac{1}{3}\mathbf{d}, \frac{2}{3}\mathbf{d}, \frac{1}{6}\mathbf{d}, \frac{5}{6}\mathbf{d}]$	$p321 [(2\mathbf{a}' + \mathbf{b}')/3]$ L68
($1\bar{1}\bar{1}$)	$\mathbf{a} + \mathbf{b}$	$\mathbf{c} - \mathbf{b}$	$\boldsymbol{\tau}_1$		$[\frac{2}{3}\mathbf{d}, \frac{1}{6}\mathbf{d}]$	$p321 [(\mathbf{a}' + 2\mathbf{b}')/3]$ L68
($\bar{1}\bar{1}1$)	$-\mathbf{a} - \mathbf{b}$	$\mathbf{b} + \mathbf{c}$	$\boldsymbol{\tau}_2$		$[\pm s\mathbf{d}, (\pm s + \frac{1}{3})\mathbf{d}, (\pm s + \frac{2}{3})\mathbf{d}]$	$p3$ L65

Auxiliary tables for Laue class $O_h - m\bar{3}m$

Centring type P

Orientation orbit (<i>hkl</i>)	Conventional basis of the scanning group			Auxiliary basis of the scanning group		
	a'	b'	d	\hat{a}	\hat{b}	\hat{c}
(<i>mn0</i>)	c	<i>na - mb</i>	<i>pa + qb</i>	a	b	c
($\bar{1}\bar{1}n0$)	c	<i>na + mb</i>	<i>-pa + qb</i>			
(<i>nm0</i>)	c	<i>ma - nb</i>	<i>qa + pb</i>			
($\bar{1}\bar{1}m0$)	c	<i>ma + nb</i>	<i>-qa + pb</i>			
(<i>0mn</i>)	a	<i>nb - mc</i>	<i>pb + qc</i>	b	c	a
($0\bar{m}\bar{n}$)	a	<i>nb + mc</i>	<i>-pb + qc</i>			
(<i>0nm</i>)	a	<i>mb - nc</i>	<i>qb + pc</i>			
($0\bar{m}m$)	a	<i>mb + nc</i>	<i>-qb + pc</i>			
(<i>n0m</i>)	b	<i>nc - ma</i>	<i>pc + qa</i>	c	a	b
(<i>n0\bar{m}</i>)	b	<i>nc + ma</i>	<i>-pc + qa</i>			
(<i>m0n</i>)	b	<i>mc - na</i>	<i>qc + pa</i>			
(<i>m0\bar{n}</i>)	b	<i>mc + na</i>	<i>-qc + pa</i>			
(<i>hhl</i>)	a - b	<i>n(a + b) - mc</i>	<i>p(a + b) + qc</i>	a + b	c	a - b
($\bar{h}\bar{h}l$)	a - b	<i>n(a + b) + mc</i>	<i>-p(a + b) + qc</i>			
(<i>h$\bar{h}l$</i>)	a + b	<i>n(b - a) - mc</i>	<i>p(b - a) + qc</i>	b - a	c	a + b
($\bar{h}hl$)	a + b	<i>n(b - a) + mc</i>	<i>-p(b - a) + qc</i>			
(<i>lhh</i>)	b - c	<i>n(b + c) - ma</i>	<i>p(b + c) + qa</i>	b + c	a	b - c
($\bar{l}\bar{h}\bar{h}$)	b - c	<i>n(b + c) + ma</i>	<i>-p(b + c) + qa</i>			
(<i>lh\bar{h}</i>)	b + c	<i>n(c - b) - ma</i>	<i>p(c - b) + qa</i>	c - b	a	b + c
($\bar{l}h\bar{h}$)	b + c	<i>n(c - b) + ma</i>	<i>-p(c - b) + qa</i>			
(<i>hlh</i>)	c - a	<i>n(c + a) - mb</i>	<i>p(c + a) + qb</i>	c + a	b	c - a
($\bar{h}\bar{l}\bar{h}$)	c - a	<i>n(c + a) + mb</i>	<i>-p(c + a) + qb</i>			
($\bar{h}l\bar{h}$)	c + a	<i>n(a - c) - mb</i>	<i>p(a - c) + qb</i>	a - c	b	c + a
(<i>hl\bar{h}</i>)	c + a	<i>n(a - c) + mb</i>	<i>-p(a - c) + qb</i>			

l odd $\Rightarrow n = l, m = 2h; l$ even $\Rightarrow n = l/2, m = h$

Arithmetic classes $432P$ and $\bar{4}3mP$

Serial No. Group type Group	207 O^1 $P432$	208 O^2 $P4_232$	212 O^6 $P4_332$	213 O^7 $P4_132$	215 T_d^1 $P\bar{4}3m$	218 T_d^4 $P\bar{4}3n$
$(mn0)$ $(\bar{m}n0)$ $(nm0)$ $(\bar{n}m0)$ $(0mn)$ $(0\bar{m}n)$ $(0nm)$ $(0\bar{n}m)$ $(n0m)$ $(n0\bar{m})$ $(m0n)$ $(m0\bar{n})$	$P112$	$P112$	$P112_1$ $(a/4)$	$P112_1$ $(a/4)$	$P112$	$P112$
			$P112_1$ $(b/4)$	$P112_1$ $(b/4)$		
			$P112_1$ $(c/4)$	$P112_1$ $(c/4)$		
(hhl) $(\bar{h}hl)$ $(h\bar{h}l)$ $(\bar{h}\bar{h}l)$ (lhh) $(\bar{l}h\bar{h})$ $(lh\bar{h})$ $(\bar{l}h\bar{h})$ (hlh) $(\bar{h}l\bar{h})$ $(\bar{h}lh)$ $(hl\bar{h})$	$A112$	$A112$ $(a+c)/4$	$A112$ $(a+c)/8$	$A112$ $3(a+c)/8$	$A11m$	$A11a$
			$A112$ $3(b+c)/8$	$A112$ $(b+c)/8$		
		$A112$ $(b+a)/4$	$A112$ $(b+a)/8$	$A112$ $3(b+a)/8$		
			$A112$ $3(c+a)/8$	$A112$ $(c+a)/8$		
		$A112$ $(c+b)/4$	$A112$ $(c+b)/8$	$A112$ $3(c+b)/8$		
			$A112$ $3(a+b)/8$	$A112$ $(a+b)/8$		