

$P4_2/nnm$

No. 134

 $P4_2/n2/n2/m$ D_{4h}^{12}

Axes	Coordinates		Wyckoff positions							
	origin 1	origin 2	2a	2b	4c 8i	4d 8j	4e 8k	4f 8l	4g 8m	8h 16n
I Maximal translationengleiche subgroups										
[2] $P\bar{4}n2$ (118)		$x+\frac{1}{4}, y-\frac{1}{4}, z+\frac{1}{4}$	2a	2b	4h 8i	2c; 2d 8j	4f 8k	4g 8l	4e 8m	$2 \times 4h$ $2 \times 8i$
[2] $P\bar{4}2m$ (111)		$x+\frac{1}{4}, y-\frac{1}{4}, z+\frac{1}{4}$	1a; 1b	1c; 1d	2e; 2f 4i; 4j	4m 4k; 4l	4n 8o	4n 8o	2g; 2h $2 \times 4n$	$2 \times 4m$ $2 \times 8o$
[2] $P4_2nm$ (102)		$x+\frac{1}{4}, y-\frac{1}{4}, z$	2a	2a	4b 8d	4b 8d	4c 8d	4c 8d	$2 \times 2a$ $2 \times 4c$	$2 \times 4b$ $2 \times 8d$
[2] $P4_222$ (93)	$x, y+\frac{1}{2}, z$	$x+\frac{1}{4}, y+\frac{1}{4}, z+\frac{1}{4}$	2c	2d	2a; 2b 4l; 4m	2e; 2f 4j; 4k	4o $2 \times 4n$	4n $2 \times 4o$	4i 8p	$4g; 4h$ $2 \times 8p$
[2] $P4_2/n$ (86)		$x, y+\frac{1}{2}, z$	2a	2b	4e 8g	4e 8g	4c 8g	4d 8g	4f 8g	$2 \times 4e$ $2 \times 8g$
[2] $Pnnn$ (48)			2a(d*)	2c(b*)	2b(a*); 2d(c*) 4g(h*); 4i	4l(k*) 4h(g*); 4j	4e 8m	4f 8m	4k(l*) 8m	$2 \times 4l(k^*)$ $2 \times 8m$
[2] $Cmme$ (67)	$\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, \mathbf{c}$	$\frac{1}{2}(x+y), \frac{1}{2}(x+y), \frac{1}{2}(-x+y)+\frac{1}{4}, z-\frac{1}{4}$	4g	4g	8l 16o	4a; 4b 16o	4d; 4e 8h; 8k	4c; 4f 8i; 8j	$2 \times 4g$ $2 \times 8l$	$2 \times 8l$ $2 \times 16o$

II Maximal klassengleiche subgroups

Enlarged unit cell, non-isomorphic

[2] $I4_1/acd$ (142)	$\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, 2\mathbf{c}$	$\frac{1}{2}(x+y), \frac{1}{2}(-x+y), \frac{1}{2}z; + (0, 0, \frac{1}{2})$	8a	8b	16f 32g	16e $2 \times 16f$	16e 32g	16c $2 \times 16e$	16d 32g	$32g$ $2 \times 32g$
[2] $I4_1/acd$ (142)	$\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, 2\mathbf{c}$	$\frac{1}{2}(x+y), \frac{1}{2}(-x+y), \frac{1}{2}z+\frac{1}{4}; + (0, 0, \frac{1}{2})$	8b	8a	16f $2 \times 16f$	16e 32g	16c $2 \times 16e$	16e 32g	16d $2 \times 32g$	$32g$ $2 \times 32g$
[2] $I4_1/acd$ (142)	$\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, 2\mathbf{c}$	$\frac{1}{2}(x+y)+\frac{1}{2}, \frac{1}{2}(-x+y), \frac{1}{2}z; + (0, 0, \frac{1}{2})$	8b	8a	16f $2 \times 16f$	16e 32g	16e $2 \times 16e$	16c 32g	16d $2 \times 32g$	$32g$ $2 \times 32g$
[2] $I4_1/acd$ (142)	$\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, 2\mathbf{c}$	$\frac{1}{2}(x+y)+\frac{1}{2}, \frac{1}{2}(-x+y), \frac{1}{2}z+\frac{1}{4}; + (0, 0, \frac{1}{2})$	8a	8b	16f 32g	16e $2 \times 16f$	16c 32g	16e 32g	16d $2 \times 32g$	$32g$ $2 \times 32g$
[2] $I4_1/amd$ (141)	$\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, 2\mathbf{c}$	$\frac{1}{2}(x+y), \frac{1}{2}(-x+y), \frac{1}{2}z; + (0, 0, \frac{1}{2})$	4a; 4b	8e	16g $2 \times 16g$	16f 32i	16h $2 \times 16f$	8c; 8d 32i	$2 \times 8e$ $2 \times 16h$	$32i$ $2 \times 32i$
[2] $I4_1/amd$ (141)	$\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, 2\mathbf{c}$	$\frac{1}{2}(x+y), \frac{1}{2}(-x+y), \frac{1}{2}z+\frac{1}{4}; + (0, 0, \frac{1}{2})$	8e	4a; 4b	16g 32i	16f $2 \times 16g$	8c; 8d 32i	16h $2 \times 16f$	$2 \times 8e$ $2 \times 16h$	$32i$ $2 \times 32i$
[2] $I4_1/amd$ (141)	$\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, 2\mathbf{c}$	$\frac{1}{2}(x+y)+\frac{1}{2}, \frac{1}{2}(-x+y), \frac{1}{2}z; + (0, 0, \frac{1}{2})$	8e	4a; 4b	16g 32i	16f $2 \times 16g$	16h 32i	8c; 8d $2 \times 16f$	$2 \times 8e$ $2 \times 16h$	$32i$ $2 \times 32i$
[2] $I4_1/amd$ (141)	$\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, 2\mathbf{c}$	$\frac{1}{2}(x+y)+\frac{1}{2}, \frac{1}{2}(-x+y), \frac{1}{2}z+\frac{1}{4}; + (0, 0, \frac{1}{2})$	8e	4a; 4b	16g $2 \times 16g$	16f 32i	16h 32i	8c; 8d $2 \times 16f$	$2 \times 8e$ $2 \times 16h$	$32i$ $2 \times 32i$
[2] $I4_1/amd$ (141)	$\mathbf{a}+\mathbf{b}, -\mathbf{a}+\mathbf{b}, 2\mathbf{c}$	$\frac{1}{2}(x+y)+\frac{1}{2}, \frac{1}{2}(-x+y), \frac{1}{2}z; + (0, 0, \frac{1}{2})$	4a; 4b	8e	16g 32i	16f 32i	16h 32i	8c; 8d $2 \times 16f$	$2 \times 8e$ $2 \times 16h$	$32i$ $2 \times 32i$

* origin 2

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 $P4_2/n\bar{2}/n\bar{2}/m$

No. 134

 $P4_2/nnm$

Axes	Coordinates		Wyckoff positions					
	origin 1	origin 2	2a 4f	2b 4g 8k	4c 8h 8l	4d 8i 8m	4e 8j 16n	
Enlarged unit cell, isomorphic								
[3] $P4_2/nnm$	a, b, 3c	$x, y, \frac{1}{3}z; \pm(0, 0, \frac{1}{3})$	$x, y, \frac{1}{3}z; \pm(0, 0, \frac{1}{3})$	$2a(b^*); 4g$ $4e(f^*); 8m$	$2b(a^*); 4g$ $3 \times 4g$ $8l(k^*); 16n$	$4c; 8h$ $3 \times 8h$ $8k(l^*); 16n$	$4d; 8h$ $8i(j^*); 16n$ $3 \times 8m$	$4f(e^*); 8m$ $8j(i^*); 16n$ $3 \times 16n$
[p] $P4_2/nnm$	a, b, pc	$x, y, \frac{1}{p}z; +\left(0, 0, \frac{u}{p}\right)$	$x, y, \frac{1}{p}z; +\left(0, 0, \frac{u}{p}\right)$	$2a(b^\dagger); \frac{p-1}{2} \times 4g$ $4f(e^\ddagger); \frac{p-1}{2} \times 8m$	$2b(a^\dagger); \frac{p-1}{2} \times 4g$ $p \times 4g$ $8k(l^\ddagger); \frac{p-1}{2} \times 16n$	$4c; \frac{p-1}{2} \times 8h$ $p \times 8h$ $8l(k^\ddagger); \frac{p-1}{2} \times 16n$	$4d; \frac{p-1}{2} \times 8h$ $8i(j^\dagger); \frac{p-1}{2} \times 16n$ $p \times 8m$	$4e(f^\ddagger); \frac{p-1}{2} \times 8m$ $8j(i^\dagger); \frac{p-1}{2} \times 16n$ $p \times 16n$
		$p = \text{prime} > 2;$						
		$u = 1, \dots, p-1$						
[9] $P4_2/nnm$	3a, 3b, c	$\underbrace{\frac{1}{3}x, \frac{1}{3}y, z; \pm(\frac{1}{3}, 0, 0)}_{\pm(\frac{1}{3}, 0, 0); \pm(0, \frac{1}{3}, 0)}$	$\underbrace{\frac{1}{3}x, \frac{1}{3}y, z; \pm(\frac{1}{3}, \frac{1}{3}, 0)}_{\pm(\frac{1}{3}, \frac{1}{3}, 0); \pm(\frac{1}{3}, \frac{2}{3}, 0)}$	$2a(b^*); 8i(j^*); 8m$ $4f; 8k; 8m; 16n$	$2b(a^*); 8j(i^*); 8m$ $4g; 2 \times 8m; 16n$ $3 \times 8k; 3 \times 16n$	$4c; 8i; 8j; 16n$ $8h; 4 \times 16n$ $3 \times 8l; 3 \times 16n$	$4d; 8k; 8l; 16n$ $3 \times 8i(j^*); 3 \times 16n$ $3 \times 8m; 3 \times 16n$	$4e; 8l; 8m; 16n$ $3 \times 8j(i^*); 3 \times 16n$ $9 \times 16n$
[p^2] $P4_2/nnm$	p a, p b, c	$\frac{1}{p}x, \frac{1}{p}y, z; +\left(\frac{u}{p}, \frac{v}{p}, 0\right)$	$\frac{1}{p}x, \frac{1}{p}y, z; +\left(\frac{u}{p}, \frac{v}{p}, 0\right)$	$2a(b^\dagger); \frac{p-1}{2} \times 8i(j^\dagger); \frac{p-1}{2} \times 8m; \frac{(p-1)(p-3)}{8} \times 16n$ $p = \text{prime} > 2;$ $u, v = 1, \dots, p-1$	$2b(a^\dagger); \frac{p-1}{2} \times 8j(i^\dagger); \frac{p-1}{2} \times 8m; \frac{(p-1)(p-3)}{8} \times 16n$	$4c; \frac{p-1}{2} \times 8i; \frac{p-1}{2} \times 8j; \frac{(p-1)^2}{4} \times 16n$	$4d; \frac{p-1}{2} \times 8k; \frac{p-1}{2} \times 8l; \frac{(p-1)^2}{4} \times 16n$	$4e; \frac{p-1}{2} \times 8l; \frac{p-1}{2} \times 8m; \frac{(p-1)^2}{4} \times 16n$
				$4f; \frac{p-1}{2} \times 8k; \frac{p-1}{2} \times 8m; \frac{(p-1)^2}{4} \times 16n$	$4g; (p-1) \times 8m; \frac{(p-1)^2}{4} \times 16n$	$8h; \frac{p^2-1}{2} \times 16n$	$p \times 8i(j^\dagger); \frac{p(p-1)}{2} \times 16n$	$p \times 8j(i^\dagger); \frac{p(p-1)}{2} \times 16n$
					$p \times 8k; \frac{p(p-1)}{2} \times 16n$	$p \times 8l; \frac{p(p-1)}{2} \times 16n$	$p \times 8m; \frac{p(p-1)}{2} \times 16n$	$p^2 \times 16n$

* origin 2

† origin 2 and $p = 4n-1$ ‡ origin 1 and $p = 4n-1$