

$I\bar{m}\bar{3}m$

No. 229

 $I4/m\bar{3}2/m$ O_h^9

Axes	Coordinates	2a	6b	8c 24h	12d 48i	12e 48j	16f 48k	24g 96l
I Maximal translationengleiche subgroups								
[2] $I\bar{4}3m$ (217)		2a	6b	8c 24g	12d 48h	12e 48h	$2\times 8c$ $2\times 24g$	$24f$ $2\times 48h$
[2] $I432$ (211)		2a	6b	8c 24h	12d $2\times 24i$	12e 48j	16f 48j	$24g$ $2\times 48j$
[2] $Im\bar{3}$ (204)		2a	6b	8c 24g	12e 48h	12d $2\times 24g$	16f 48h	$2\times 12e$ $2\times 48h$
[4] $R\bar{3}m$ (166)	$\frac{1}{2}(-\mathbf{a}+\mathbf{b}+\mathbf{c})$, $y+z, x+z, x+y$ $\frac{1}{2}(\mathbf{a}-\mathbf{b}+\mathbf{c})$, (rhombohedral $\frac{1}{2}(\mathbf{a}+\mathbf{b}-\mathbf{c})$ axes) $-\mathbf{a}+\mathbf{b}, -\mathbf{b}+\mathbf{c}$, $\frac{1}{3}(-2x+y+z), \frac{1}{3}(-x-y+2z)$, $\frac{1}{2}(\mathbf{a}+\mathbf{b}+\mathbf{c})$ $\frac{2}{3}(x+y+z)$ (hexagonal axes)	1a	3e	1b; 3d 6f; 6h	6g $2\times 6g; 12i$	6h $2\times 12i$	$2c; 6h$ $2\times 6h; 12i$	$12i$ $4\times 12i$
conjugate: $\mathbf{a}+\mathbf{b}, -\mathbf{b}-\mathbf{c}$, $\frac{1}{3}(2x+y-z), \frac{1}{3}(x-y-2z)$, $\frac{1}{2}(-\mathbf{a}+\mathbf{b}-\mathbf{c})$ $\frac{2}{3}(-x+y-z)$ (hexagonal axes)			3a	9e	3b; 9d 18f; 18h	18g $2\times 18g; 36i$	18h $2\times 36i$	$36i$ $4\times 36i$
conjugate: $-\mathbf{a}-\mathbf{b}, \mathbf{b}-\mathbf{c}$, $\frac{1}{3}(-2x-y-z), \frac{1}{3}(-x+y-2z)$, $\frac{1}{2}(\mathbf{a}-\mathbf{b}-\mathbf{c})$ $\frac{2}{3}(x-y-z)$ (hexagonal axes)								
conjugate: $\mathbf{a}-\mathbf{b}, \mathbf{b}+\mathbf{c}$, $\frac{1}{3}(2x-y+z), \frac{1}{3}(x+y+2z)$, $\frac{1}{2}(-\mathbf{a}-\mathbf{b}+\mathbf{c})$ $\frac{2}{3}(-x-y+z)$ (hexagonal axes)								
[3] $I4/mmm$ (139)		2a	2b; 4c	8f 8h; 16n	4d; 8j 16k; 32o	4e; 8i 16l; $2\times 16n$	16m 16m; 32o	$8g; 2\times 8j$ $3\times 32o$
conjugate: $\mathbf{b}, \mathbf{c}, \mathbf{a}$	y, z, x							
conjugate: $\mathbf{c}, \mathbf{a}, \mathbf{b}$	z, x, y							

II Maximal klassengleiche subgroups**Loss of centring translations**

[2] $Pn\bar{3}m$ (224)	origin 1: x, y, z origin 2: $x+\frac{1}{4}, y+\frac{1}{4}, z+\frac{1}{4}$	2a	6d	4b; 4c 24k	12f 24i; 24j	12g 48l	$2\times 8e$ $2\times 24k$	$24h$ $2\times 48l$
[2] $Pm\bar{3}n$ (223)		2a	6b	8e 24k	6c; 6d $2\times 24j$	12f $2\times 24k$	16i 48l	$12g; 12h$ $2\times 48l$
[2] $Pn\bar{3}n$ (222)	origin 1: x, y, z origin 2: $x+\frac{1}{4}, y+\frac{1}{4}, z+\frac{1}{4}$	2a	6b	8c 24h	12d 48i	12e 48i	16f 48i	$24g$ $2\times 48i$
[2] $Pm\bar{3}m$ (221)		1a; 1b	3c; 3d	8g 12i; 12j	12h 48n	6e; 6f 24k; 24l	$2\times 8g$ $2\times 24m$	$2\times 12h$ $2\times 48n$

Enlarged unit cell, isomorphic

[27] $Im\bar{3}m$	3a, 3b, 3c	$\frac{1}{3}x, \frac{1}{3}y, \frac{1}{3}z; \pm(\frac{1}{3}, 0, 0);$ $\pm(0, \frac{1}{3}, 0); \pm(0, 0, \frac{1}{3});$ $\pm(0, \frac{1}{3}, \frac{1}{3}); \pm(\frac{1}{3}, 0, \frac{1}{3});$ $\pm(\frac{1}{3}, \frac{1}{3}, 0); \pm(\frac{1}{3}, 0, \frac{2}{3});$ $\pm(\frac{1}{3}, \frac{2}{3}, 0); \pm(0, \frac{1}{3}, \frac{2}{3});$ $\pm(\frac{1}{3}, \frac{1}{3}, \frac{1}{3}); \pm(\frac{2}{3}, \frac{1}{3}, \frac{1}{3});$ $\pm(\frac{1}{3}, \frac{2}{3}, \frac{1}{3}); \pm(\frac{1}{3}, \frac{1}{3}, \frac{2}{3})$	2a; 12e; 16f; 24h	6b; 12e; 24g; 24h; 48j; 48k	8c; 16f; 48i; 3×48k	12d; 24g; 48i 3×48j; 96l	3×12e; 3×48j;	3×16f; 6×48k; 96l	3×24g; 6×48j; 3×96l
					3×24h; 3×48j; 3×48k; 3×96l	9×48j; 12×96l	9×48k; 9×96l	27×96l 9×96l	

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No. 229

 $Im\bar{3}m$

Axes	Coordinates	Wyckoff positions					
	$2a$ $24g$	$6b$ $24h$	$8c$ $48i$	$12d$ $48j$	$12e$ $48k$	$16f$ $96l$	
$[p^3] Im\bar{3}m$ $p\mathbf{a}, p\mathbf{b}, p\mathbf{c}$ $\frac{1}{p}x, \frac{1}{p}y, \frac{1}{p}z;$ $+(\frac{u}{p}, \frac{v}{p}, \frac{w}{p})$ $p = \text{prime} > 2;$ $u, v, w = 1, \dots, p-1$	$\frac{1}{p}x, \frac{1}{p}y, \frac{1}{p}z;$ $+(\frac{u}{p}, \frac{v}{p}, \frac{w}{p})$ $p = \text{prime} > 2;$ $u, v, w = 1, \dots, p-1$	$2a; \frac{p-1}{2} \times 12e;$ $\frac{p-1}{2} \times 16f;$ $\frac{p-1}{2} \times 24h;$ $\frac{(p-1)(p-3)}{8} \times 48j;$ $\frac{(p-1)(p-3)}{4} \times 48k;$ $\frac{(p-1)(p-3)(p-5)}{48} \times 96l$	$6b; \frac{p-1}{2} \times 12e;$ $\frac{p-1}{2} \times 24g;$ $\frac{p-1}{2} \times 24h;$ $\frac{(p-1)(3p-5)}{8} \times 48j;$ $\frac{(p-1)^2}{4} \times 48k;$ $\frac{(p-1)^2(p-3)}{16} \times 96l$	$8c; \frac{p-1}{2} \times 16f;$ $\frac{p(p-1)}{2} \times 48i;$ $\frac{(p^2-1)(p-3)}{12} \times 96l$	$12d; \frac{p-1}{2} \times 24g;$ $\frac{p(p-1)}{2} \times 48i;$ $\frac{(p^2-1)(p-2)}{8} \times 96l$	$p \times 12e;$ $\frac{p(p-1)}{2} \times 48j;$ $\frac{p(p-1)(p-2)}{6} \times 96l$	$p \times 16f;$ $\frac{p(p-1)}{2} \times 48k;$ $\frac{p(p-1)(p-3)}{8} \times 96l$