International Tables for Crystallography (2006). Vol. C, Figure 9.2.1.7, p. 755.

layers in the slab can be written as $A\beta\beta A$ or $A\gamma\gamma A$. There are thus six possible sequences for the unit slab. These unit slabs can be stacked in the manner described for equal spheres. Thus, for example, the $2H$ structure can have three different layer stackings: $/A\beta\beta A\,B\gamma\gamma B/\ldots$, $/A\beta\beta A\,B\alpha\alpha B/\ldots$ and $/A\beta\beta A\,C\beta\beta C/$. Periodicities containing up to 21 unit slabs have been reported for GaSe (see Terhell, 1983). The bonding between the layers of a slab is predominantly covalent while that between two adjacent slabs is of the van der Waals type, which imparts cleavage characteristics to this material.

9.2.1.3. *Symmetry of close-packed layer stackings of equal spheres*

It can be seen from Fig. 9.2.1.2(*a*) that a stacking of two or more layers in the close-packed manner still possesses all three symmetry planes but the twofold axes disappear while the sixfold axes coincide with the threefold axes (Verma & Krishna, 1966). The lowest symmetry of a completely arbitrary periodic stacking sequence of close-packed layers is shown in Fig. 9.2.1.2(*b*). Structures resulting from such stackings therefore belong to the trigonal system. Even though a pure sixfold axis of rotation is not possible, close-packed structures belonging to the hexagonal system can result by virtue of at least one of the three symmetry axes parallel to [00.1] being a 6_3 axis (Verma & Krishna, 1966). This is possible if the layers in the unit cell are stacked in special ways. For example, a $6H$ stacking sequence $/ABCACB/\ldots$ has a 6_3 axis through 0, 0. It follows that, for an nH structure belonging to the hexagonal system, n must be even. A packing nH/nR with n odd will therefore necessarily belong to the trigonal system and can have either a hexagonal or a rhombohedral lattice (Verma & Krishna, 1966).

Other symmetries that can arise by restricting the arbitrariness of the stacking sequence in the identity period are: (i) a centre of symmetry at the centre of either the spheres or the octahedral voids; and (ii) a mirror plane perpendicular to [00.1]. Since there must be two centres of symmetry in the unit cell, the centrosymmetric arrangements may possess both centres either at sphere centres/octahedral void centres or one centre each at the centres of spheres and octahedral voids (Patterson & Kasper, 1959).

9.2.1.4. *Possible lattice types*

Close packings of equal spheres can belong to the trigonal, hexagonal, or cubic crystal systems. Structures belonging to the hexagonal system necessarily have a hexagonal lattice, *i.e.* a lattice in which we can choose a primitive unit cell with $a = b \neq c$, $\alpha = \beta = 90^\circ$, and $\gamma = 120^\circ$. In the primitive unit cell of the hexagonal close-packed structure $/AB/\ldots$ shown in Fig. 9.2.1.6, there are two spheres associated with each lattice point, one at 0, 0, 0 and the other at $\frac{1}{3}, \frac{2}{3}, \frac{1}{2}$. Structures belonging to the trigonal system can have either a hexagonal or a rhombohedral lattice. By a rhombohedral lattice is meant a lattice in which we can choose a primitive unit cell with $a = b = c$, $\alpha = \beta = \gamma \neq 90^\circ$. Both types of lattice can be referred to either hexagonal or rhombohedral axes, the unit cell being non-primitive when a hexagonal lattice is referred to rhombohedral axes and *vice versa* (Buerger, 1953). In close-packed structures, it is generally convenient to refer both hexagonal and rhombohedral lattices to hexagonal axes. Fig. 9.2.1.7 shows a rhombohedral lattice in which the primitive cell is defined by the rhombohedral axes a_1, a_2, a_3; but a non-primitive hexagonal unit cell can be chosen by adopting the axes A_1, A_2, C. The latter has lattice points at $0, 0, 0$; $\frac{2}{3}, \frac{1}{3}, \frac{1}{3}$; and $\frac{1}{3}, \frac{2}{3}, \frac{2}{3}$. If this rhombohedral lattice is rotated through 60° around [00.1], the hexagonal unit cell will then be centred at $\frac{1}{3}, \frac{2}{3}, \frac{1}{3}$ and $\frac{2}{3}, \frac{1}{3}, \frac{2}{3}$. These two settings are crystallographically equivalent for close packing of equal spheres. They represent twin arrangements when both occur in the same crystal. The hexagonal unit cell of an nR structure is made up of three elementary stacking sequences of $n/3$ layers that are related to each other either by an anticyclic shift of layers $A \to C \to B \to A$ (obverse setting) or by a cyclic shift of layers $A \to B \to C \to A$ (reverse setting) in the direction of z increasing (Verma & Krishna, 1966). Evidently, n must be a multiple of 3 for nR structures.

In the special case of the close packing $/ABC/\ldots$ [with the ideal axial ratio of $\sqrt{(2/3)}$], the primitive rhombohedral unit cell has $\alpha = \beta = \gamma = 60^\circ$, which enhances the symmetry and enables the choice of a face-centred cubic unit cell. The relationship between the face-centred cubic and the rhombohedral unit cell is shown in Fig. 9.2.1.8. The threefold axis of the rhombohedral unit cell coincides with one of the $\langle 111 \rangle$ directions of the cubic unit cell. The close-packed layers are thus parallel to the $\{111\}$ planes in the cubic close packing.

9.2.1.5. *Possible space groups*

It was shown by Belov (1947) that consistent combinations of the possible symmetry elements in close packing of equal spheres can give rise to eight possible space groups: $P3m1$, $P\bar{3}m1$,

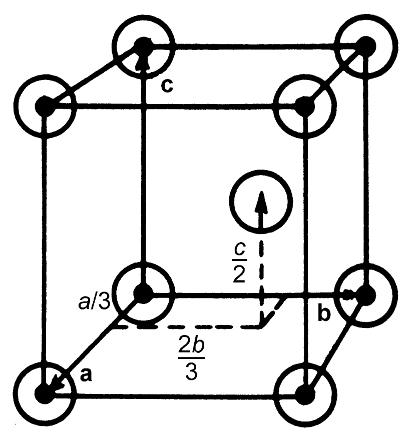

Fig. 9.2.1.6. The primitive unit cell of the $2H$ close packing.

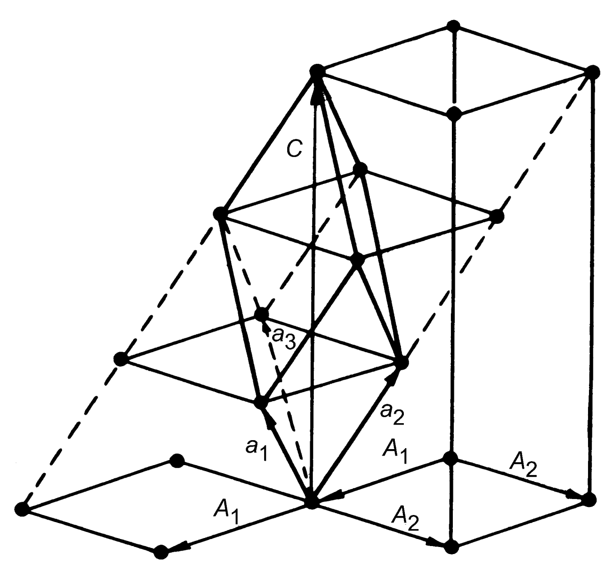

Fig. 9.2.1.7. A rhombohedral lattice (a_1, a_2, a_3) referred to hexagonal axes (A_1, A_2, C) (after Buerger, 1953).

references