

9. BASIC STRUCTURAL FEATURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups

The number labelling the superspace group is denoted by $n.m$, where n is the number attached to the three-dimensional basic space group and m numbers the various superspace groups having the same basic space group. The symbol of the basic space group, the symbol for the four-dimensional point group K_s , the number of the four-dimensional Bravais class to which the superspace group belongs (Table 9.8.3.2a), and the superspace-group symbol are also given. The superspace-group symbol is indicated in the short notation, *i.e.* for the basic group one uses the short symbol from *International Tables for Crystallography*, Volume A, and then the values of τ are given for each of the generators in this symbol, unless all these values are zero. Then, instead of writing a number of zeros, one omits them all. Finally, the special reflection conditions due to non-primitive translations are given, for $hklm$ if $q^r = 0$ and for $HKLm$ otherwise. Recall the $HKLm$ are the indices with respect to a conventional basis a_c^*, b_c^*, c_c^*, q^i as in Table 9.8.3.2(a). The reflection conditions due to centring translations are given in Table 9.8.3.6.

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions
1.1	$P1$	$(1, 1)$	1	$P1(\alpha\beta\gamma)$	
2.1	$P\bar{1}$	$(\bar{1}, \bar{1})$	1	$P\bar{1}(\alpha\beta\gamma)$	
3.1	$P2$	$(2, \bar{1})$	2	$P2(\alpha\beta 0)$	$00lm: m = 2n$
3.2		$(2, \bar{1})$	3	$P2(\alpha\beta \frac{1}{2})$	
3.3		$(2, 1)$	5	$P2(00\gamma)$	
3.4		$(2, 1)$	5	$P2(00\gamma)s$	
3.5		$(2, 1)$	6	$P2(\frac{1}{2}0\gamma)$	
4.1	$P2_1$	$(2, \bar{1})$	2	$P2_1(\alpha\beta 0)$	$00l0: l = 2n$
4.2		$(2, 1)$	5	$P2_1(00\gamma)$	$00lm: l = 2n$
4.3		$(2, 1)$	6	$P2_1(\frac{1}{2}0\gamma)$	$00Lm: L = 2n$
5.1	$B2$	$(2, \bar{1})$	4	$B2(\alpha\beta 0)$	$00lm: m = 2n$
5.2		$(2, 1)$	7	$B2(00\gamma)$	
5.3		$(2, 1)$	7	$B2(00\gamma)s$	
5.4	Pm	$(2, 1)$	8	$B2(0\frac{1}{2}\gamma)$	$hk0m: m = 2n$
6.1		$(m, 1)$	2	$Pm(\alpha\beta 0)$	
6.2		$(m, 1)$	2	$Pm(\alpha\beta 0)s$	
6.3		$(m, 1)$	3	$Pm(\alpha\beta \frac{1}{2})$	
6.4		$(m, \bar{1})$	5	$Pm(00\gamma)$	
6.5	$(m, \bar{1})$	6	$Pm(\frac{1}{2}0\gamma)$	$hk0m: k = 2n$ $HK0m: K = 2n$ $hk00: k = 2n$ $HK00: K = 2n$	
7.1	Pb	$(m, 1)$	2		$Pb(\alpha\beta 0)$
7.2		$(m, 1)$	3		$Pb(\alpha\beta \frac{1}{2})$
7.3		$(m, \bar{1})$	5		$Pb(00\gamma)$
7.4		$(m, \bar{1})$	6		$Pb(\frac{1}{2}0\gamma)$
8.1	Bm	$(m, 1)$	4	$Bm(\alpha\beta 0)$	$hk0m: m = 2n$
8.2		$(m, 1)$	4	$Bm(\alpha\beta 0)s$	
8.3		$(m, \bar{1})$	7	$Bm(00\gamma)$	
8.4		$(m, \bar{1})$	8	$Bm(0\frac{1}{2}\gamma)$	
9.1	Bb	$(m, 1)$	4	$Bb(\alpha\beta 0)$	$hk0m: k = 2n$
9.2		$(m, \bar{1})$	7	$Bb(00\gamma)$	$hk00: k = 2n$
10.1	$P2/m$	$(2/m, \bar{1}\bar{1})$	2	$P2/m(\alpha\beta 0)$	$hk0m: m = 2n$
10.2		$(2/m, \bar{1}\bar{1})$	2	$P2/m(\alpha\beta 0)s$	
10.3		$(2/m, \bar{1}\bar{1})$	3	$P2/m(\alpha\beta \frac{1}{2})$	
10.4		$(2/m, \bar{1}\bar{1})$	5	$P2/m(00\gamma)$	
10.5		$(2/m, \bar{1}\bar{1})$	5	$P2/m(00\gamma)s0$	
10.6	$P2_1/m$	$(2/m, \bar{1}\bar{1})$	6	$P2/m(\frac{1}{2}0\gamma)$	$00lm: m = 2n$
11.1		$(2/m, \bar{1}\bar{1})$	2	$P2_1/m(\alpha\beta 0)$	
11.2		$(2/m, \bar{1}\bar{1})$	2	$P2_1/m(\alpha\beta 0)s$	
11.3		$(2/m, \bar{1}\bar{1})$	5	$P2_1/m(00\gamma)$	
11.4		$(2/m, \bar{1}\bar{1})$	6	$P2_1/m(\frac{1}{2}0\gamma)$	
12.1	$B2/m$	$(2/m, \bar{1}\bar{1})$	4	$B2/m(\alpha\beta 0)$	$00l0: l = 2n$ $00l0: l = 2n; hk0m: m = 2n$ $00lm: l = 2n$ $00Lm: L = 2n$
12.2		$(2/m, \bar{1}\bar{1})$	4	$B2/m(\alpha\beta 0)s$	
12.3		$(2/m, \bar{1}\bar{1})$	7	$B2/m(00\gamma)$	
12.4		$(2/m, \bar{1}\bar{1})$	7	$B2/m(00\gamma)s0$	
12.5		$(2/m, \bar{1}\bar{1})$	8	$B2/m(\frac{1}{2}0\gamma)$	
13.1	$P2/b$	$(2/m, \bar{1}\bar{1})$	2	$P2/b(\alpha\beta 0)$	$hk0m: k = 2n$ $HK0m: m = 2n$ $hk00: k = 2n$ $00lm: m = 2n; hk00: k = 2n$ $HK00: K = 2n$
13.2		$(2/m, \bar{1}\bar{1})$	3	$P2/b(\alpha\beta \frac{1}{2})$	
13.3		$(2/m, \bar{1}\bar{1})$	5	$P2/b(00\gamma)$	
13.4		$(2/m, \bar{1}\bar{1})$	5	$P2/b(00\gamma)s0$	
13.5		$(2/m, \bar{1}\bar{1})$	6	$P2/b(\frac{1}{2}0\gamma)$	
14.1	$P2_1/b$	$(2/m, \bar{1}\bar{1})$	2	$P2_1/b(\alpha\beta 0)$	$00l0: l = 2n; hk0m: k = 2n$ $00lm: l = 2n; hk00: k = 2n$ $00Lm: L = 2n; HK00: K = 2n$
14.2		$(2/m, \bar{1}\bar{1})$	5	$P2_1/b(00\gamma)$	
14.3		$(2/m, \bar{1}\bar{1})$	6	$P2_1/b(\frac{1}{2}0\gamma)$	
15.1	$B2/b$	$(2/m, \bar{1}\bar{1})$	4	$B2/b(\alpha\beta 0)$	$hk0m: k = 2n$ $hk00: k = 2n$ $00lm: m = 2n; hk00: k = 2n$
15.2		$(2/m, \bar{1}\bar{1})$	7	$B2/b(00\gamma)$	
15.3		$(2/m, \bar{1}\bar{1})$	7	$B2/b(00\gamma)s0$	

9. BASIC STRUCTURAL FEATURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions		
28.3		$(m2m, \bar{1}\bar{1}\bar{1})$	9	$Pma2(00\gamma)ss0$	$0klm: m = 2n; h0lm: h + m = 2n$		
28.4			9	$Pma2(00\gamma)0ss$	$h0lm: h + m = 2n$		
28.5			10	$Pma2(0\frac{1}{2}\gamma)$	$H0Lm: H = 2n$		
28.6			10	$Pma2(0\frac{1}{2}\gamma)s0s$	$0Klm: m = 2n; H0Lm: H = 2n$		
28.7			10	$Pm2a(0\frac{1}{2}\gamma)$	$HK00: H = 2n$		
28.8			10	$Pm2a(0\frac{1}{2}\gamma)s00$	$0Klm: m = 2n; HK00: H = 2n$		
28.9			10	$Pc2m(0\frac{1}{2}\gamma)$	$0Klm: L = 2n$		
28.10			$(2mm, \bar{1}\bar{1}\bar{1})$	9	$P2cm(00\gamma)$	$h0lm: l = 2n$	
28.11				9	$P2mb(00\gamma)$	$hk00: k = 2n$	
28.12				$(mm2, 111)$	9	$P2mb(00\gamma)0s0$	$h0lm: m = 2n; hk00: k = 2n$
28.13					10	$P2cm(0\frac{1}{2}\gamma)$	$H0Lm: L = 2n$
28.14					11	$P2cm(\frac{1}{2}\frac{1}{2}\gamma)$	$H0Lm: L = 2n$
29.1	$Pca2_1$	$(mm2, 111)$			9	$Pca2_1(00\gamma)$	$0klm: l = 2n; h0lm: h = 2n$
29.2					9	$Pca2_1(00\gamma)0ss$	$0klm: l = 2n; h0lm: h + m = 2n$
29.3			10	$Pca2_1(0\frac{1}{2}\gamma)$	$0Klm: L = 2n; H0Lm: H = 2n$		
29.4			$(2mm, \bar{1}\bar{1}\bar{1})$	9	$P2_1ca(00\gamma)$	$hk00: h = 2n; h0lm: l = 2n$	
29.5				9	$P2_1ab(00\gamma)$	$h0lm: h = 2n; hk00: k = 2n$	
29.6			$Pcn2$	$(mm2, 111)$	9	$P2_1ab(00\gamma)0s0$	$h0lm: h + m = 2n; hk00: k = 2n$
29.7					10	$P2_1ca(0\frac{1}{2}\gamma)$	$H0Lm: L = 2n; HK00: H = 2n$
30.1	9	$Pcn2(00\gamma)$			$0klm: l = 2n; h0lm: h + l = 2n$		
30.2		$(2mm, \bar{1}\bar{1}\bar{1})$	9	$Pcn2(00\gamma)s0s$	$0klm: l + m = 2n; h0lm: h + l = 2n$		
30.3			10	$Pcn2(0\frac{1}{2}\gamma)$	$0Klm: L = 2n; H0Lm: H + L = 2n$		
30.4			9	$P2na(00\gamma)$	$h0lm: h + l = 2n; hk00: h = 2n$		
30.5			9	$P2an(00\gamma)$	$h0lm: h = 2n; hk00: h + k = 2n$		
30.6			9	$P2an(00\gamma)0s0$	$h0lm: h + m = 2n; hk00: h + k = 2n$		
30.7			10	$P2na(0\frac{1}{2}\gamma)$	$H0Lm: H + L = 2n; HK00: H = 2n$		
30.8			11	$P2an(\frac{1}{2}\frac{1}{2}\gamma)0q0$	$H0Lm: 2H + m = 4n; HK00: H + K = 2n$		
31.1	$Pmn2_1$	$(mm2, 111)$	9	$Pmn2_1(00\gamma)$	$h0lm: h + l = 2n$		
31.2			9	$Pmn2_1(00\gamma)s0s$	$0klm: m = 2n; h0lm: h + l = 2n$		
31.3			10	$Pmn2_1(0\frac{1}{2}\gamma)$	$H0Lm: H + L = 2n$		
31.4			10	$Pmn2_1(0\frac{1}{2}\gamma)s0s$	$0Klm: m = 2n; H0Lm: H + L = 2n$		
31.5			$(2mm, \bar{1}\bar{1}\bar{1})$	9	$P2_1nm(00\gamma)$	$h0lm: h + l = 2n$	
31.6	9	$P2_1mn(00\gamma)$		$hk00: h + k = 2n$			
31.7	9	$P2_1mn(00\gamma)0s0$		$hk00: h + k = 2n; h0lm: m = 2n$			
31.8	$Pba2$	$(mm2, 111)$	10	$P2_1nm(0\frac{1}{2}\gamma)$	$H0Lm: H + L = 2n$		
32.1			9	$Pba2(00\gamma)$	$0klm: k = 2n; h0lm: h = 2n$		
32.2			9	$Pba2(00\gamma)s0s$	$0klm: k + m = 2n; h0lm: h = 2n$		
32.3			9	$Pba2(00\gamma)ss0$	$0klm: k + m = 2n; h0lm: h + m = 2n$		
32.4		$(m2m, \bar{1}\bar{1}\bar{1})$	11	$Pba2(\frac{1}{2}\frac{1}{2}\gamma)qq0$	$0Klm: 2K + m = 4n; H0Lm: 2H + m = 4n$		
32.5			10	$Pc2a(0\frac{1}{2}\gamma)$	$0Klm: L = 2n; HK00: H = 2n$		
32.6			9	$P2cb(00\gamma)$	$h0lm: l = 2n; hk00: k = 2n$		
33.1	$Pbn2_1$	$(mm2, 111)$	9	$Pbn2_1(00\gamma)$	$0klm: k = 2n; h0lm: h + l = 2n$		
33.2			9	$Pbn2_1(00\gamma)s0s$	$0klm: k + m = 2n; h0lm: h + l = 2n$		
33.3			11	$Pbn2_1(\frac{1}{2}\frac{1}{2}\gamma)qq0$	$0Klm: 2K + m = 4n; H0Lm: 2H + 2L + m = 4n$		
33.4			$(2mm, \bar{1}\bar{1}\bar{1})$	9	$P2_1nb(00\gamma)$	$h0lm: h + l = 2n; hk00: k = 2n$	
33.5	9	$P2_1cn(00\gamma)$		$h0lm: l = 2n; hk00: h + k = 2n$			
34.1	$Pnn2$	$(mm2, 111)$	9	$Pnn2(00\gamma)$	$0klm: k + l = 2n; h0lm: h + l = 2n$		
34.2			9	$Pnn2(00\gamma)s0s$	$0klm: k + l + m = 2n; h0lm: h + l = 2n$		
34.3			11	$Pnn2(\frac{1}{2}\frac{1}{2}\gamma)qq0$	$0Klm: 2K + 2L + m = 4n; H0Lm: 2H + 2L + m = 4n$		
34.4	$(2mm, \bar{1}\bar{1}\bar{1})$		9	$P2nn(00\gamma)$	$h0lm: h + l = 2n; hk00: h + k = 2n$		
34.5			11	$P2nn(\frac{1}{2}\frac{1}{2}\gamma)0q0$	$H0Lm: 2H + 2L + m = 4n; HK00: H + K = 2n$		
35.1	$Cmm2$	$(mm2, 111)$	13	$Cmm2(00\gamma)$			
35.2			13	$Cmm2(00\gamma)s0s$	$0klm: m = 2n$		
35.3			13	$Cmm2(00\gamma)ss0$	$0klm: m = 2n; h0lm: m = 2n$		
35.4			14	$Cmm2(10\gamma)$			
35.5			14	$Cmm2(10\gamma)s0s$	$0Klm: m = 2n$		
35.6			14	$Cmm2(10\gamma)ss0$	$0Klm: m = 2n; H0Lm: m = 2n$		
35.7			$(2mm, \bar{1}\bar{1}\bar{1})$	15	$A2mm(00\gamma)$		
35.8	15	$A2mm(00\gamma)0s0$		$h0lm: m = 2n$			
35.9	$Cmc2_1$	$(mm2, 111)$	16	$A2mm(\frac{1}{2}0\gamma)$			
35.10			16	$A2mm(\frac{1}{2}0\gamma)0s0$	$H0Lm: m = 2n$		
36.1			13	$Cmc2_1(00\gamma)$			
36.2			13	$Cmc2_1(00\gamma)s0s$	$0klm: m = 2n; h0lm: l = 2n$		
36.3	$(2mm, \bar{1}\bar{1}\bar{1})$		14	$Cmc2_1(10\gamma)$	$H0Lm: L = 2n$		
36.4			14	$Cmc2_1(10\gamma)s0s$	$0Klm: m = 2n; H0Lm: L = 2n$		
36.5			15	$A2_1am(00\gamma)$	$h0lm: h = 2n$		

9.8. INCOMMENSURATE AND COMMENSURATE MODULATED STRUCTURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions		
36.6	Ccc2	(mm2, 111)	15	$A2_1am(00\gamma)0s0$	$h0lm: h + m = 2n$		
36.7			15	$A2_1ma(00\gamma)$	$hk00: h = 2n$		
36.8			15	$A2_1ma(00\gamma)0s0$	$h0lm: m = 2n; hk00: h = 2n$		
37.1			13	$Ccc2(00\gamma)$	$0klm: l = 2n; h0lm: l = 2n$		
37.2			13	$Ccc2(00\gamma)s0s$	$0klm: l + m = 2n; h0lm: l = 2n$		
37.3			14	$Ccc2(10\gamma)$	$0Klm: L = 2n; H0Lm: L = 2n$		
37.4			14	$Ccc2(10\gamma)s0s$	$0Klm: L + m = 2n; H0Lm: L = 2n$		
37.5			(2mm, $\bar{1}1\bar{1}$)	15	$A2aa(00\gamma)$	$h0lm: h = 2n; hk00: h = 2n$	
37.6				15	$A2aa(00\gamma)0s0$	$h0lm: h + m = 2n; hk00: h = 2n$	
38.1			C2mm	(2mm, $\bar{1}1\bar{1}$)	13	$C2mm(00\gamma)$	$h0lm: m = 2n$
38.2					13	$C2mm(00\gamma)0s0$	
38.3					14	$C2mm(10\gamma)$	
38.4					14	$C2mm(10\gamma)0s0$	$H0Lm: m = 2n$
38.5	(mm2, 111)	15			$Amm2(00\gamma)$		
38.6		15			$Amm2(00\gamma)s0s$	$0klm: m = 2n$	
38.7		15			$Amm2(00\gamma)ss0$	$0klm: m = 2n; h0lm: m = 2n$	
38.8		15			$Amm2(00\gamma)0ss$	$h0lm: m = 2n$	
38.9		16			$Amm2(\frac{1}{2}0\gamma)$		
38.10		16			$Amm2(\frac{1}{2}0\gamma)0ss$	$H0Lm: m = 2n$	
38.11	(m2m, $1\bar{1}\bar{1}$)	15	$Am2m(00\gamma)$				
38.12		15	$Am2m(00\gamma)s00$	$0klm: m = 2n$			
38.13		16	$Am2m(\frac{1}{2}0\gamma)$				
39.1		C2mb	(2mm, $\bar{1}1\bar{1}$)	13	$C2mb(00\gamma)$	$hk00: k = 2n$	
39.2	13			$C2mb(00\gamma)0s0$	$h0lm: m = 2n; hk00: k = 2n$		
39.3	14			$C2mb(10\gamma)$	$HK00: K = 2n$		
39.4	14			$C2mb(10\gamma)0s0$	$H0Lm: m = 2n; HK00: K = 2n$		
39.5	(mm2, 111)			15	$Abm2(00\gamma)$	$0klm: k = 2n$	
39.6				15	$Abm2(00\gamma)s0s$	$0klm: k + m = 2n$	
39.7				15	$Abm2(00\gamma)ss0$	$0klm: k + m = 2n; h0lm: m = 2n$	
39.8				15	$Abm2(00\gamma)0ss$	$0klm: k = 2n; h0lm: m = 2n$	
39.9				16	$Abm2(\frac{1}{2}0\gamma)$	$0Klm: K = 2n$	
39.10				16	$Abm2(\frac{1}{2}0\gamma)0ss$	$0Klm: K + m = 2n$	
39.11	(m2m, $1\bar{1}\bar{1}$)			15	$Ac2m(00\gamma)$	$0klm: l = 2n$	
39.12				15	$Ac2m(00\gamma)s00$	$0klm: l + m = 2n$	
39.13		16	$Ac2m(\frac{1}{2}0\gamma)$	$0Klm: L = 2n$			
40.1		C2cm	(2mm, $\bar{1}1\bar{1}$)	13	$C2cm(00\gamma)$	$h0lm: l = 2n$	
40.2	14			$C2cm(10\gamma)$	$H0Lm: L = 2n$		
40.3	(mm2, 111)			15	$Ama2(00\gamma)$	$h0lm: h = 2n$	
40.4				15	$Ama2(00\gamma)s0s$	$0klm: m = 2n; h0lm: h = 2n$	
40.5				15	$Ama2(00\gamma)ss0$	$0klm: m = 2n; h0lm: h + m = 2n$	
40.6				15	$Ama2(00\gamma)0ss$	$h0lm: h + m = 2n$	
40.7	(m2m, $1\bar{1}\bar{1}$)			15	$Am2a(00\gamma)$	$hk00: h = 2n$	
40.8				15	$Am2a(00\gamma)s00$	$0klm: m = 2n; hk00: h = 2n$	
41.1		C2cb	(2mm, $\bar{1}1\bar{1}$)	13	$C2cb(00\gamma)$	$h0lm: l = 2n; hk00: k = 2n$	
41.2				14	$C2cb(10\gamma)$	$H0Lm: L = 2n; HK00: K = 2n$	
41.3	(mm2, 111)			15	$Aba2(00\gamma)$	$0klm: k = 2n; h0lm: h = 2n$	
41.4				15	$Aba2(00\gamma)s0s$	$0klm: k + m = 2n; h0lm: h = 2n$	
41.5				15	$Aba2(00\gamma)ss0$	$0klm: k + m = 2n; h0lm: h + m = 2n$	
41.6	(m2m, $1\bar{1}\bar{1}$)			15	$Aba2(00\gamma)0ss$	$0klm: k = 2n; h0lm: h + m = 2n$	
41.7		15	$Ac2a(00\gamma)$	$0klm: l = 2n; hk00: h = 2n$			
41.8		15	$Ac2a(00\gamma)s00$	$0klm: l + m = 2n; hk00: h = 2n$			
42.1	Fmm2	(mm2, 111)	17	$Fmm2(00\gamma)$			
42.2			17	$Fmm2(00\gamma)s0s$	$0klm: m = 2n$		
42.3			17	$Fmm2(00\gamma)ss0$	$0klm: m = 2n; h0lm: m = 2n$		
42.4			18	$Fmm2(10\gamma)$			
42.5			18	$Fmm2(10\gamma)s0s$	$0Klm: m = 2n$		
42.6			18	$Fmm2(10\gamma)ss0$	$0Klm: m = 2n; H0Lm: m = 2n$		
42.7			(2mm, $\bar{1}1\bar{1}$)	17	$F2mm(00\gamma)$		
42.8				17	$F2mm(00\gamma)0s0$	$h0lm: m = 2n$	
42.9				18	$F2mm(10\gamma)$		
42.10				18	$F2mm(10\gamma)0s0$	$H0Lm: m = 2n$	
43.1	Fdd2	(mm2, 111)	17	$Fdd2(00\gamma)$	$0klm: k + l = 4n$		
43.2			17	$Fdd2(00\gamma)s0s$	$0klm: k + l + 2m = 4n; h0lm: h + l = 4n$		
43.3			(2mm, $\bar{1}1\bar{1}$)	17	$F2dd(00\gamma)$	$h0lm: h + l = 4n$	
44.1	Imm2	(mm2, 111)	12	$Imm2(00\gamma)$			
44.2			12	$Imm2(00\gamma)s0s$	$0klm: m = 2n$		

9. BASIC STRUCTURAL FEATURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions	
44.3	<i>Iba2</i>	$(2mm, \bar{1}1\bar{1})$	12	<i>Imm2</i> (00 γ) <i>ss0</i>	<i>Oklm</i> : $m = 2n$; <i>h0lm</i> : $m = 2n$	
44.4			12	<i>I2mm</i> (00 γ)		
44.5			12	<i>I2mm</i> (00 γ) <i>0s0</i>	<i>h0lm</i> : $m = 2n$	
45.1			$(mm2, 111)$	12	<i>Iba2</i> (00 γ)	<i>Oklm</i> : $k = 2n$; <i>h0lm</i> : $h = 2n$
45.2			12	<i>Iba2</i> (00 γ) <i>s0s</i>	<i>Oklm</i> : $k + m = 2n$; <i>h0lm</i> : $h = 2n$	
45.3			12	<i>Iba2</i> (00 γ) <i>ss0</i>	<i>Oklm</i> : $k + m = 2n$; <i>h0lm</i> : $h + m = 2n$	
45.4		$(2mm, \bar{1}1\bar{1})$	12	<i>I2cb</i> (00 γ)	<i>h0lm</i> : $l = 2n$; <i>hk00</i> : $k = 2n$	
45.5		12	<i>I2cb</i> (00 γ) <i>0s0</i>	<i>h0lm</i> : $l + m = 2n$; <i>hk00</i> : $k = 2n$		
46.1		<i>Ima2</i>	$(mm2, 111)$	12	<i>Ima2</i> (00 γ)	<i>h0lm</i> : $h = 2n$
46.2				12	<i>Ima2</i> (00 γ) <i>s0s</i>	<i>Oklm</i> : $m = 2n$; <i>h0lm</i> : $h = 2n$
46.3				12	<i>Ima2</i> (00 γ) <i>ss0</i>	<i>Oklm</i> : $m = 2n$; <i>h0lm</i> : $h + m = 2n$
46.4				12	<i>Ima2</i> (00 γ) <i>0ss</i>	<i>h0lm</i> : $h + m = 2n$
46.5	$(2mm, \bar{1}1\bar{1})$			12	<i>I2mb</i> (00 γ)	<i>hk00</i> : $k = 2n$
46.6	12			<i>I2mb</i> (00 γ) <i>0s0</i>	<i>h0lm</i> : $m = 2n$; <i>hk00</i> : $k = 2n$	
46.7	12	<i>I2cm</i> (00 γ)	<i>h0lm</i> : $l = 2n$			
46.8	12	<i>I2cm</i> (00 γ) <i>0s0</i>	<i>h0lm</i> : $l + m = 2n$			
47.1	<i>Pmmm</i>	$(mmm, 11\bar{1})$	9	<i>Pmmm</i> (00 γ)		
47.2			9	<i>Pmmm</i> (00 γ) <i>s00</i>	<i>Oklm</i> : $m = 2n$	
47.3			9	<i>Pmmm</i> (00 γ) <i>ss0</i>	<i>Oklm</i> : $m = 2n$; <i>h0lm</i> : $m = 2n$	
47.4			10	<i>Pmmm</i> (0 $\frac{1}{2}$ γ)		
47.5			10	<i>Pmmm</i> (0 $\frac{1}{2}$ γ) <i>s00</i>	<i>OKLm</i> : $m = 2n$	
47.6			11	<i>Pmmm</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)		
48.1	<i>Pnnn</i>	$(mmm, 11\bar{1})$	9	<i>Pnnn</i> (00 γ)	<i>Oklm</i> : $k + l = 2n$; <i>h0lm</i> : $h + l = 2n$; <i>hk00</i> : $h + k = 2n$	
48.2			9	<i>Pnnn</i> (00 γ) <i>s00</i>	<i>Oklm</i> : $k + l + m = 2n$; <i>h0lm</i> : $h + l = 2n$; <i>hk00</i> : $h + k = 2n$	
48.3			11	<i>Pnnn</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ) <i>qq0</i>	<i>OKLm</i> : $2K + 2L + m = 4n$; <i>H0Lm</i> : $2H + 2L + m = 2n$; <i>HK00</i> : $H + K = 2n$	
49.1	<i>Pccm</i>	$(mmm, 11\bar{1})$	9	<i>Pccm</i> (00 γ)	<i>Oklm</i> : $l = 2n$; <i>h0lm</i> : $l = 2n$	
49.2			9	<i>Pccm</i> (00 γ) <i>s00</i>	<i>Oklm</i> : $l + m = 2n$; <i>h0lm</i> : $l = 2n$	
49.3			9	<i>Pmaa</i> (00 γ)	<i>h0lm</i> : $h = 2n$; <i>hk00</i> : $h = 2n$	
49.4			9	<i>Pmaa</i> (00 γ) <i>s00</i>	<i>Oklm</i> : $m = 2n$; <i>h0lm</i> : $h = 2n$; <i>hk00</i> : $h = 2n$	
49.5			9	<i>Pmaa</i> (00 γ) <i>ss0</i>	<i>Oklm</i> : $m = 2n$; <i>h0lm</i> : $h + m = 2n$; <i>hk00</i> : $h = 2n$	
49.6			9	<i>Pmaa</i> (00 γ) <i>0s0</i>	<i>h0lm</i> : $h + m = 2n$; <i>hk00</i> : $h = 2n$	
49.7			10	<i>Pccm</i> (0 $\frac{1}{2}$ γ)	<i>OKLm</i> : $L = 2n$; <i>H0Lm</i> : $L = 2n$	
49.8			10	<i>Pmaa</i> (0 $\frac{1}{2}$ γ)	<i>H0Lm</i> : $H = 2n$; <i>HK00</i> : $H = 2n$	
49.9			10	<i>Pmaa</i> (0 $\frac{1}{2}$ γ) <i>s00</i>	<i>OKLm</i> : $m = 2n$; <i>H0Lm</i> : $H = 2n$; <i>HK00</i> : $H = 2n$	
49.10			11	<i>Pccm</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)	<i>OKLm</i> : $L = 2n$; <i>H0Lm</i> : $L = 2n$	
50.1			<i>Pban</i>	$(mmm, 11\bar{1})$	9	<i>Pban</i> (00 γ)
50.2	9	<i>Pban</i> (00 γ) <i>s00</i>			<i>Oklm</i> : $k + m = 2n$; <i>h0lm</i> : $h = 2n$	
50.3	9	<i>Pban</i> (00 γ) <i>ss0</i>			<i>Oklm</i> : $k + m = 2n$; <i>h0lm</i> : $h + m = 2n$	
50.4	9	<i>Pcna</i> (00 γ)			<i>Oklm</i> : $l = 2n$; <i>h0lm</i> : $h + l = 2n$; <i>hk00</i> : $h = 2n$	
50.5	9	<i>Pcna</i> (00 γ) <i>s00</i>			<i>Oklm</i> : $l + m = 2n$; <i>h0lm</i> : $h + l = 2n$; <i>hk00</i> : $h = 2n$	
50.6	10	<i>Pcna</i> (0 $\frac{1}{2}$ γ)			<i>OKLm</i> : $L = 2n$; <i>H0Lm</i> : $H + L = 2n$; <i>HK00</i> : $H = 2n$	
50.7	11	<i>Pban</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ) <i>qq0</i>			<i>OKLm</i> : $2K + m = 4n$; <i>H0Lm</i> : $2H + m = 4n$; <i>HK00</i> : $H + K = 2n$	
51.1	<i>Pmma</i>	$(mmm, 11\bar{1})$	9	<i>Pmma</i> (00 γ)	<i>hk00</i> : $h = 2n$	
51.2			9	<i>Pmma</i> (00 γ) <i>s00</i>	<i>Oklm</i> : $m = 2n$; <i>hk00</i> : $h = 2n$	
51.3			9	<i>Pmma</i> (00 γ) <i>ss0</i>	<i>Oklm</i> : $m = 2n$; <i>h0lm</i> : $m = 2n$; <i>hk00</i> : $h = 2n$	
51.4			9	<i>Pmma</i> (00 γ) <i>0s0</i>	<i>h0lm</i> : $m = 2n$; <i>hk00</i> : $h = 2n$	
51.5			9	<i>Pmam</i> (00 γ)	<i>h0lm</i> : $h = 2n$	
51.6			9	<i>Pmam</i> (00 γ) <i>s00</i>	<i>Oklm</i> : $m = 2n$; <i>h0lm</i> : $h = 2n$	
51.7			9	<i>Pmam</i> (00 γ) <i>ss0</i>	<i>Oklm</i> : $m = 2n$; <i>h0lm</i> : $h + m = 2n$	
51.8			9	<i>Pmam</i> (00 γ) <i>0s0</i>	<i>h0lm</i> : $h + m = 2n$	
51.9			9	<i>Pmcm</i> (00 γ)	<i>h0lm</i> : $l = 2n$	
51.10			9	<i>Pmcm</i> (00 γ) <i>s00</i>	<i>Oklm</i> : $m = 2n$; <i>h0lm</i> : $l = 2n$	
51.11			10	<i>Pmma</i> (0 $\frac{1}{2}$ γ)	<i>HK00</i> : $H = 2n$	
51.12			10	<i>Pmma</i> (0 $\frac{1}{2}$ γ) <i>s00</i>	<i>OKLm</i> : $m = 2n$; <i>HK00</i> : $H = 2n$	
51.13			10	<i>Pmam</i> (0 $\frac{1}{2}$ γ)	<i>H0Lm</i> : $H = 2n$	
51.14			10	<i>Pmam</i> (0 $\frac{1}{2}$ γ) <i>s00</i>	<i>OKLm</i> : $m = 2n$; <i>H0Lm</i> : $H = 2n$	
51.15			10	<i>Pmcm</i> (0 $\frac{1}{2}$ γ)	<i>H0Lm</i> : $L = 2n$	
51.16			10	<i>Pmcm</i> (0 $\frac{1}{2}$ γ) <i>s00</i>	<i>OKLm</i> : $m = 2n$; <i>H0Lm</i> : $L = 2n$	
51.17			10	<i>Pcmm</i> (0 $\frac{1}{2}$ γ)	<i>OKLm</i> : $L = 2n$	
51.18			11	<i>Pcmm</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)	<i>OKLm</i> : $L = 2n$	
52.1	<i>Pnna</i>	$(mmm, 11\bar{1})$	9	<i>Pnna</i> (00 γ)	<i>Oklm</i> : $k + l = 2n$; <i>h0lm</i> : $h + l = 2n$; <i>hk00</i> : $h = 2n$	
52.2			9	<i>Pnna</i> (00 γ) <i>s00</i>	<i>Oklm</i> : $k + l + m = 2n$; <i>h0lm</i> : $h + l = 2n$; <i>hk00</i> : $h = 2n$	
52.3			9	<i>Pbnn</i> (00 γ)	<i>Oklm</i> : $k = 2n$; <i>h0lm</i> : $h + l = 2n$; <i>hk00</i> : $h + k = 2n$	

9.8. INCOMMENSURATE AND COMMENSURATE MODULATED STRUCTURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions		
52.4			9	$Pbnn(00\gamma)s00$	$0klm: k+m=2n; h0lm: h+l=2n; hk00: h+k=2n$		
52.5			9	$Pcnn(00\gamma)$	$0klm: l=2n; h0lm: h+l=2n; hk00: h+k=2n$		
52.6			9	$Pcnn(00\gamma)s00$	$0klm: l+m=2n; h0lm: h+l=2n; hk00: h+k=2n$		
52.7			11	$Pbnn(\frac{1}{2}2\gamma)qq0$	$0KLM: 2K+m=4n; H0Lm: 2H+2L+m=4n; HK00: H+K=2n$		
53.1	$Pmna$	$(mmm, 11\bar{1})$	9	$Pmna(00\gamma)$	$h0lm: h+l=2n; hk00: h=2n$		
53.2			9	$Pmna(00\gamma)s00$	$0klm: m=2n; h0lm: h+l=2n; hk00: h=2n$		
53.3			9	$Pcnm(00\gamma)$	$0klm: l=2n; h0lm: h+l=2n$		
53.4			9	$Pcnm(00\gamma)s00$	$0klm: l+m=2n; h0lm: h+l=2n$		
53.5			9	$Pbmn(00\gamma)$	$0klm: k=2n; hk00: h+k=2n$		
53.6			9	$Pbmn(00\gamma)s00$	$0klm: k+m=2n; hk00: h+k=2n$		
53.7			9	$Pbmn(00\gamma)ss0$	$0klm: k+m=2n; h0lm: m=2n; hk00: h+k=2n$		
53.8			9	$Pbmn(00\gamma)0s0$	$0klm: k=2m; h0lm: m=2n; hk00: h+k=2n$		
53.9			10	$Pmna(0\frac{1}{2}\gamma)$	$H0Lm: H+L=2n; HK00: H=2n$		
53.10			10	$Pmna(0\frac{1}{2}\gamma)s00$	$0KLM: m=2n; H0Lm: H+L=2n; HK00: H=2n$		
53.11	$Pcca$	$(mmm, 11\bar{1})$	10	$Pcnn(0\frac{1}{2}\gamma)$	$0KLM: L=2n; H0Lm: H+L=2n$		
54.1			9	$Pcca(00\gamma)$	$0klm: l=2n; h0lm: l=2n; hk00: h=2n$		
54.2			9	$Pcca(00\gamma)s00$	$0klm: l+m=2n; h0lm: l=2n; hk00: h=2n$		
54.3			9	$Pcaa(00\gamma)$	$0klm: l=2n; h0lm: h=2n; hk00: h=2n$		
54.4			9	$Pcaa(00\gamma)0s0$	$0klm: l=2n; h0lm: h+m=2n; hk00: h=2n$		
54.5			9	$Pbab(00\gamma)$	$0klm: k=2n; h0lm: h=2n; hk00: k=2n$		
54.6			9	$Pbab(00\gamma)s00$	$0klm: k+m=2n; h0lm: h=2n; hk00: k=2n$		
54.7			9	$Pbab(00\gamma)ss0$	$0klm: k+m=2n; h0lm: h+m=2n; hk00: k=2n$		
54.8			9	$Pbab(00\gamma)0s0$	$0klm: k=2n; h0lm: h+m=2n; hk00: k=2n$		
54.9			10	$Pcca(0\frac{1}{2}\gamma)$	$0KLM: L=2n; H0Lm: L=2n; HK00: H=2n$		
54.10	10	$Pcaa(0\frac{1}{2}\gamma)$	$0KLM: L=2n; H0Lm: H=2n; HK00: H=2n$				
55.1	$Pbam$	$(mmm, 11\bar{1})$	9	$Pbam(00\gamma)$	$0klm: k=2n; h0lm: h=2n$		
55.2			9	$Pbam(00\gamma)s00$	$0klm: k+m=2n; h0lm: h=2n$		
55.3			9	$Pbam(00\gamma)ss0$	$0klm: k+m=2n; h0lm: h+m=2n$		
55.4			9	$Pcma(00\gamma)$	$0klm: l=2n; hk00: h=2n$		
55.5	9	$Pcma(00\gamma)0s0$	$0klm: l=2n; h0lm: m=2n; hk00: h=2n$				
55.6	10	$Pcma(0\frac{1}{2}\gamma)$	$0KLM: L=2n; HK00: H=2n$				
56.1	$Pccn$	$(mmm, 11\bar{1})$	9	$Pccn(00\gamma)$	$0klm: l=2n; h0lm: l=2n; hk00: h+k=2n$		
56.2			9	$Pccn(00\gamma)s00$	$0klm: l+m=2n; h0lm: l=2n; hk00: h+k=2n$		
56.3			9	$Pbnb(00\gamma)$	$0klm: k=2n; h0lm: h+l=2n; hk00: k=2n$		
56.4			9	$Pbnb(00\gamma)s00$	$0klm: k+m=2n; h0lm: h+l=2n; hk00: k=2n$		
57.1	$Pcam$	$(mmm, 11\bar{1})$	9	$Pcam(00\gamma)$	$0klm: l=2n; h0lm: h=2n$		
57.2			9	$Pcam(00\gamma)0s0$	$0klm: l=2n; h0lm: h+m=2n$		
57.3			9	$Pmca(00\gamma)$	$h0lm: l=2n; hk00: h=2n$		
57.4			9	$Pmca(00\gamma)s00$	$0klm: m=2n; h0lm: l=2n; hk00: h=2n$		
57.5			9	$Pbma(00\gamma)$	$0klm: k=2n; hk00: h=2n$		
57.6			9	$Pbma(00\gamma)s00$	$0klm: k+m=2n; hk00: h=2n$		
57.7			9	$Pbma(00\gamma)ss0$	$0klm: k+m=2n; h0lm: m=2n; hk00: h=2n$		
57.8			9	$Pbma(00\gamma)0s0$	$0klm: k=2n; h0lm: m=2n; hk00: h=2n$		
57.9			10	$Pcam(0\frac{1}{2}\gamma)$	$0KLM: L=2n; H0Lm: H=2n$		
57.10			10	$Pmca(0\frac{1}{2}\gamma)$	$H0Lm: L=2n; HK00: H=2n$		
57.11	$Pnnm$	$(mmm, 11\bar{1})$	10	$Pmca(0\frac{1}{2}\gamma)s00$	$0KLM: m=2n; H0Lm: L=2n; HK00: H=2n$		
58.1			9	$Pnnm(00\gamma)$	$0klm: k+l=2n; h0lm: h+l=2n$		
58.2			9	$Pnnm(00\gamma)s00$	$0klm: k+l+m=2n; h0lm: h+l=2n$		
58.3			9	$Pmnn(00\gamma)$	$h0lm: h+l=2n; hk00: h+k=2n$		
58.4	$Pmnn$	$(mmm, 11\bar{1})$	9	$Pmnn(00\gamma)s00$	$0klm: m=2n; h0lm: h+l=2n; hk00: h+k=2n$		
59.1			9	$Pmnn(00\gamma)$	$hk00: h+k=2n$		
59.2			9	$Pmnn(00\gamma)s00$	$0klm: m=2n; hk00: h+k=2n$		
59.3			9	$Pmnn(00\gamma)ss0$	$0klm: m=2n; h0lm: m=2n; hk00: h+k=2n$		
59.4			9	$Pnmm(00\gamma)$	$h0lm: h+l=2n$		
59.5			9	$Pnmm(00\gamma)s00$	$0klm: m=2n; h0lm: h+l=2n$		
59.6			10	$Pnmm(0\frac{1}{2}\gamma)$	$H0Lm: H+L=2n$		
59.7			10	$Pnmm(0\frac{1}{2}\gamma)s00$	$0KLM: m=2n; H0Lm: H+L=2n$		
60.1			$Pbcn$	$(mmm, 11\bar{1})$	9	$Pbcn(00\gamma)$	$0klm: k=2n; h0lm: l=2n; hk00: h+k=2n$
60.2					9	$Pbcn(00\gamma)s00$	$0klm: k+m=2n; h0lm: l=2n; hk00: h+k=2n$
60.3	9	$Pnca(00\gamma)$			$0klm: k+l=2n; h0lm: l=2n; hk00: h=2n$		
60.4	9	$Pnca(00\gamma)s00$			$0klm: k+l+m=2n; h0lm: l=2n; hk00: h=2n$		
60.5	9	$Pbna(00\gamma)$	$0klm: k=2n; h0lm: h+l=2n; hk00: h=2n$				
60.6	$Pbca$	$(mmm, 11\bar{1})$	9	$Pbna(00\gamma)s00$	$0klm: k+m=2n; h0lm: h+l=2n; hk00: h=2n$		
61.1			9	$Pbca(00\gamma)$	$0klm: k=2n; h0lm: l=2n; hk00: h=2n$		
61.2			9	$Pbca(00\gamma)s00$	$0klm: k+m=2n; h0lm: l=2n; hk00: h=2n$		

9. BASIC STRUCTURAL FEATURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions
62.1	<i>Pnma</i>	$(mmm, 11\bar{1})$	9	<i>Pnma</i> (00 γ)	0klm: $k+l=2n$; hk00: $h=2n$
62.2			9	<i>Pnma</i> (00 γ)0s0	0klm: $k+l=2n$; h0lm: $m=2n$; hk00: $h=2n$
62.3			9	<i>Pbnm</i> (00 γ)	0klm: $k=2n$; h0lm: $h+l=2n$
62.4			9	<i>Pbnm</i> (00 γ)s00	0klm: $k+m=2n$; h0lm: $h+l=2n$
62.5			9	<i>Pmcn</i> (00 γ)	h0lm: $l=2n$; hk00: $h+k=2n$
62.6	<i>Cmcm</i>	$(mmm, 11\bar{1})$	9	<i>Pmcn</i> (00 γ)s00	0klm: $m=2n$; h0lm: $l=2n$; hk00: $h+k=2n$
63.1			13	<i>Cmcm</i> (00 γ)	h0lm: $l=2n$
63.2			13	<i>Cmcm</i> (00 γ)s00	0klm: $m=2n$; h0lm: $l=2n$
63.3			14	<i>Cmcm</i> (10 γ)	H0Lm: $L=2n$
63.4			14	<i>Cmcm</i> (10 γ)s00	0KLm: $m=2n$; H0Lm: $L=2n$
63.5			15	<i>Amam</i> (00 γ)	h0lm: $h=2n$
63.6			15	<i>Amam</i> (00 γ)s00	0klm: $m=2n$; h0lm: $h=2n$
63.7			15	<i>Amam</i> (00 γ)ss0	0klm: $m=2n$; h0lm: $h+m=2n$
63.8			15	<i>Amam</i> (00 γ)0s0	h0lm: $h+m=2n$
63.9			15	<i>Amma</i> (00 γ)	hk00: $h=2n$
63.10			15	<i>Amma</i> (00 γ)s00	0klm: $m=2n$; hk00: $h=2n$
63.11	<i>Cmca</i>	$(mmm, 11\bar{1})$	15	<i>Amma</i> (00 γ)ss0	0klm: $m=2n$; h0lm: $m=2n$; hk00: $h=2n$
63.12			15	<i>Amma</i> (00 γ)0s0	h0lm: $m=2n$; hk00: $h=2n$
64.1			13	<i>Cmca</i> (00 γ)	h0lm: $l=2n$; hk00: $h=2n$
64.2			13	<i>Cmca</i> (00 γ)s00	0klm: $m=2n$; h0lm: $l=2n$; hk00: $h=2n$
64.3			14	<i>Cmca</i> (10 γ)	H0Lm: $L=2n$; HK00: $H=2n$
64.4			14	<i>Cmca</i> (10 γ)s00	0KLm: $m=2n$; H0Lm: $L=2n$; HK00: $H=2n$
64.5			15	<i>Abma</i> (00 γ)	0klm: $k=2n$; hk00: $h=2n$
64.6			15	<i>Abma</i> (00 γ)s00	0klm: $k+m=2n$; hk00: $h=2n$
64.7			15	<i>Abma</i> (00 γ)ss0	0klm: $k+m=2n$; h0lm: $m=2n$; hk00: $h=2n$
64.8			15	<i>Abma</i> (00 γ)0s0	0klm: $k=2n$; h0lm: $m=2n$; hk00: $h=2n$
64.9			15	<i>Acam</i> (00 γ)	0klm: $l=2n$; h0lm: $h=2n$
64.10	<i>Cmmm</i>	$(mmm, 11\bar{1})$	15	<i>Acam</i> (00 γ)s00	0klm: $l+m=2n$; h0lm: $h=2n$
64.11			15	<i>Acam</i> (00 γ)ss0	0klm: $l+m=2n$; h0lm: $h+m=2n$
64.12			15	<i>Acam</i> (00 γ)0s0	0klm: $l=2n$; h0lm: $h+m=2n$
65.1			13	<i>Cmmm</i> (00 γ)	
65.2			13	<i>Cmmm</i> (00 γ)s00	0klm: $m=2n$
65.3			13	<i>Cmmm</i> (00 γ)ss0	0klm: $m=2n$; h0lm: $m=2n$
65.4			14	<i>Cmmm</i> (10 γ)	
65.5			14	<i>Cmmm</i> (10 γ)s00	0KLm: $m=2n$
65.6			14	<i>Cmmm</i> (10 γ)ss0	0KLm: $m=2n$; H0Lm: $m=2n$
65.7			15	<i>Ammm</i> (00 γ)	
65.8			15	<i>Ammm</i> (00 γ)s00	0klm: $m=2n$
65.9	15	<i>Ammm</i> (00 γ)ss0	0klm: $m=2n$; h0lm: $m=2n$		
65.10	15	<i>Ammm</i> (00 γ)0s0	h0lm: $m=2n$		
65.11	<i>Cccm</i>	$(mmm, 11\bar{1})$	16	<i>Ammm</i> ($\frac{1}{2}$ 0 γ)	
65.12			16	<i>Ammm</i> ($\frac{1}{2}$ 0 γ)0s0	H0Lm: $m=2n$
66.1			13	<i>Cccm</i> (00 γ)	0klm: $l=2n$; h0lm: $l=2n$
66.2			13	<i>Cccm</i> (00 γ)s00	0klm: $l+m=2n$; h0lm: $l=2n$
66.3			14	<i>Cccm</i> (10 γ)	0KLm: $L=2n$; H0Lm: $L=2n$
66.4			14	<i>Cccm</i> (10 γ)s00	0KLm: $L+m=2n$; H0Lm: $L=2n$
66.5			15	<i>Amaa</i> (00 γ)	h0lm: $h=2n$; hk00: $h=2n$
66.6			15	<i>Amaa</i> (00 γ)s00	0klm: $m=2n$; h0lm: $h=2n$; hk00: $h=2n$
66.7			15	<i>Amaa</i> (00 γ)ss0	0klm: $m=2n$; h0lm: $h+m=2n$; hk00: $h=2n$
66.8			15	<i>Amaa</i> (00 γ)0s0	h0lm: $h+m=2n$; hk00: $h=2n$
67.1			<i>Cmma</i>	$(mmm, 11\bar{1})$	13
67.2	13	<i>Cmma</i> (00 γ)s00			0klm: $m=2n$; hk00: $h=2n$
67.3	13	<i>Cmma</i> (00 γ)ss0			0klm: $m=2n$; h0lm: $m=2n$; hk00: $h=2n$
67.4	14	<i>Cmma</i> (10 γ)			HK00: $H=2n$
67.5	14	<i>Cmma</i> (10 γ)s00			0KLm: $m=2n$; HK00: $H=2n$
67.6	14	<i>Cmma</i> (10 γ)ss0			0KLm: $m=2n$; H0Lm: $m=2n$; HK00: $H=2n$
67.7	15	<i>Acmm</i> (00 γ)			0klm: $l=2n$
67.8	15	<i>Acmm</i> (00 γ)s00			0klm: $l+m=2n$
67.9	15	<i>Acmm</i> (00 γ)ss0			0klm: $l+m=2n$; h0lm: $m=2n$
67.10	15	<i>Acmm</i> (00 γ)0s0			0klm: $l=2n$; h0lm: $m=2n$
67.11	16	<i>Acmm</i> ($\frac{1}{2}$ 0 γ)			0KLm: $L=2n$
67.12	16	<i>Acmm</i> ($\frac{1}{2}$ 0 γ)0s0	0KLm: $L=2n$; H0Lm: $m=2n$		
68.1	<i>Ccca</i>	$(mmm, 11\bar{1})$	13	<i>Ccca</i> (00 γ)	0klm: $l=2n$; h0lm: $l=2n$; hk00: $h=2n$
68.2			13	<i>Ccca</i> (00 γ)s00	0klm: $l+m=2n$; h0lm: $l=2n$; hk00: $h=2n$
68.3			14	<i>Ccca</i> (10 γ)	0KLm: $L=2n$; H0Lm: $L=2n$; HK00: $H=2n$
68.4			14	<i>Ccca</i> (10 γ)s00	0KLm: $L+m=2n$; H0Lm: $L=2n$; HK00: $H=2n$

9.8. INCOMMENSURATE AND COMMENSURATE MODULATED STRUCTURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions		
68.5	<i>Fmmm</i>	$(mmm, 11\bar{1})$	15	<i>Acaa</i> (00 γ)	0 klm : $l = 2n$; h0 lm : $h = 2n$; hk00: $h = 2n$		
68.6			15	<i>Acaa</i> (00 γ)s00	0 klm : $l + m = 2n$; h0 lm : $h = 2n$; hk00: $h = 2n$		
68.7			15	<i>Acaa</i> (00 γ)ss0	0 klm : $l + m = 2n$; h0 lm : $h + m = 2n$; hk00: $h = 2n$		
68.8			15	<i>Acaa</i> (00 γ)0s0	0 klm : $l = 2n$; h0 lm : $h + m = 2n$; hk00: $h = 2n$		
69.1			17	<i>Fmmm</i> (00 γ)	0 klm : $m = 2n$		
69.2			17	<i>Fmmm</i> (00 γ)s00	0 klm : $m = 2n$; h0 lm : $m = 2n$		
69.3			17	<i>Fmmm</i> (00 γ)ss0			
69.4			18	<i>Fmmm</i> (10 γ)	0 KLm : $m = 2n$		
69.5			18	<i>Fmmm</i> (10 γ)s00	0 KLm : $m = 2n$; H0 Lm : $m = 2n$		
69.6			18	<i>Fmmm</i> (10 γ)ss0	0 klm : $k + l = 4n$; h0 lm : $h + l = 4n$; hk00: $h + k = 4n$		
70.1	<i>Fddd</i>	$(mmm, 11\bar{1})$	17	<i>Fddd</i> (00 γ)	0 klm : $k + l + 2m = 4n$; h0 lm : $h + l = 4n$;		
70.2			17	<i>Fddd</i> (00 γ)s00	hk00: $h + k = 4n$		
71.1	<i>Immm</i>	$(mmm, 11\bar{1})$	12	<i>Immm</i> (00 γ)	0 klm : $m = 2n$		
71.2			12	<i>Immm</i> (00 γ)s00	0 klm : $m = 2n$; h0 lm : $m = 2n$		
71.3	<i>Ibam</i>	$(mmm, 11\bar{1})$	12	<i>Ibam</i> (00 γ)	0 klm : $k = 2n$; h0 lm : $h = 2n$		
72.1			12	<i>Ibam</i> (00 γ)s00	0 klm : $k + m = 2n$; h0 lm : $h = 2n$		
72.2			12	<i>Ibam</i> (00 γ)ss0	0 klm : $k + m = 2n$; h0 lm : $h = 2n$		
72.3			12	<i>Ibam</i> (00 γ)0s0	0 klm : $k + m = 2n$; h0 lm : $h + m = 2n$		
72.4			12	<i>Imcb</i> (00 γ)	h0 lm : $l = 2n$; hk00: $k = 2n$		
72.5			12	<i>Imcb</i> (00 γ)s00	0 klm : $m = 2n$; h0 lm : $l = 2n$; hk00: $k = 2n$		
72.6			12	<i>Imcb</i> (00 γ)ss0	0 klm : $m = 2n$; h0 lm : $l + m = 2n$; hk00: $k = 2n$		
72.7			12	<i>Imcb</i> (00 γ)0s0	h0 lm : $l + m = 2n$; hk00: $k = 2n$		
73.1			<i>Ibca</i>	$(mmm, 11\bar{1})$	12	<i>Ibca</i> (00 γ)	0 klm : $k = 2n$; h0 lm : $l = 2n$; hk00: $h = 2n$
73.2					12	<i>Ibca</i> (00 γ)s00	0 klm : $k + m = 2n$; h0 lm : $l = 2n$; hk00: $h = 2n$
73.3	<i>Imma</i>	$(mmm, 11\bar{1})$	12	<i>Ibca</i> (00 γ)ss0	0 klm : $k + m = 2n$; h0 lm : $l + m = 2n$; hk00: $h = 2n$		
74.1			12	<i>Imma</i> (00 γ)	hk00: $h = 2n$		
74.2			12	<i>Imma</i> (00 γ)s00	0 klm : $m = 2n$; hk00: $h = 2n$		
74.3			12	<i>Imma</i> (00 γ)ss0	0 klm : $m = 2n$; h0 lm : $m = 2n$; hk00: $h = 2n$		
74.4			12	<i>Icmm</i> (00 γ)	0 klm : $l = 2n$		
74.5			12	<i>Icmm</i> (00 γ)s00	0 klm : $l + m = 2n$		
74.6			12	<i>Icmm</i> (00 γ)ss0	0 klm : $l + m = 2n$; h0 lm : $m = 2n$		
74.7	12	<i>Icmm</i> (00 γ)0s0	0 klm : $l = 2n$; h0 lm : $m = 2n$				
75.1	<i>P4</i>	(4, 1)	19	<i>P4</i> (00 γ)	00 lm : $m = 4n$		
75.2			19	<i>P4</i> (00 γ)q	00 lm : $m = 2n$		
75.3	<i>P4₁</i>	(4, 1)	19	<i>P4</i> (00 γ)s			
75.4			20	<i>P4</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)	00 Lm : $m = 4n$		
75.5			20	<i>P4</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)q	00 lm : $l = 4n$		
76.1			19	<i>P4₁</i> (00 γ)	00 Lm : $L = 4n$		
76.2			20	<i>P4₁</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)	00 lm : $l = 2n$		
77.1			<i>P4₂</i>	(4, 1)	19	<i>P4₂</i> (00 γ)	00 lm : $2l + m = 4n$
77.2					19	<i>P4₂</i> (00 γ)q	00 lm : $l = 2n$
77.3			<i>P4₃</i>	(4, 1)	20	<i>P4₂</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)	00 Lm : $L = 2n$
77.4					20	<i>P4₂</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)q	00 Lm : $2L + m = 4n$
78.1					19	<i>P4₃</i> (00 γ)	00 lm : $l = 4n$
78.2	20	<i>P4₃</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)			00 Lm : $L = 4n$		
79.1	<i>I4</i>	(4, 1)	21	<i>I4</i> (00 γ)			
79.2			21	<i>I4</i> (00 γ)q	00 lm : $m = 4n$		
79.3			21	<i>I4</i> (00 γ)s	00 lm : $m = 2n$		
80.1	<i>I4₁</i>	(4, 1)	21	<i>I4₁</i> (00 γ)	00 lm : $l = 4n$		
80.2			21	<i>I4₁</i> (00 γ)q	00 lm : $l + m = 4n$		
81.1	<i>P$\bar{4}$</i>	$(\bar{4}, \bar{1})$	19	<i>P$\bar{4}$</i> (00 γ)			
81.2			20	<i>P$\bar{4}$</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)			
82.1	<i>I$\bar{4}$</i>	$(\bar{4}, \bar{1})$	21	<i>I$\bar{4}$</i> (00 γ)			
83.1			<i>P4/m</i>	(4/ m , $1\bar{1}$)	19	<i>P4/m</i> (00 γ)	
83.2	19	<i>P4/m</i> (00 γ)s0			00 lm : $m = 2n$		
83.3	<i>P4₂/m</i>	(4/ m , $1\bar{1}$)	20	<i>P4/m</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)			
84.1			19	<i>P4₂/m</i> (00 γ)	00 lm : $l = 2n$		
84.2			20	<i>P4₂/m</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)	00 Lm : $L = 2n$		
85.1			<i>P4/n</i>	(4/ m , $1\bar{1}$)	19	<i>P4/n</i> (00 γ)	hk00: $h + k = 2n$
85.2	19	<i>P4/n</i> (00 γ)s0			00 lm : $m = 2n$; hk00: $h + k = 2n$		
85.3	<i>P4₂/n</i>	(4/ m , $1\bar{1}$)	20	<i>P4/n</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)q0	00 Lm : $m = 4n$; HK00: $H = 2n$, $K = 2n$		
86.1			19	<i>P4₂/n</i> (00 γ)	00 lm : $l = 2n$; hk00: $h + k = 2n$		
86.2	<i>I4/m</i>	(4/ m , $1\bar{1}$)	20	<i>P4₂/n</i> ($\frac{1}{2}$ $\frac{1}{2}$ γ)q0	00 Lm : $2L + m = 4n$; HK00: $H = 2n$, $K = 2n$		
87.1			21	<i>I4/m</i> (00 γ)			

9. BASIC STRUCTURAL FEATURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions
87.2			21	$I4/m(00\gamma)s0$	$00lm: m = 2n$
88.1	$I4_1/a$	$(4/m, \bar{1}\bar{1})$	21	$I4_1/a(00\gamma)$	$00lm: l = 4n; hk00: h = 2n$
89.1	$P422$	$(422, \bar{1}\bar{1}\bar{1})$	19	$P422(00\gamma)$	
89.2			19	$P422(00\gamma)q00$	$00lm: m = 4n$
89.3			19	$P422(00\gamma)s00$	$00lm: m = 2n$
89.4			20	$P422(\frac{1}{2}\frac{1}{2}\gamma)$	
89.5			20	$P422(\frac{1}{2}\frac{1}{2}\gamma)q00$	$00Lm: m = 4n$
90.1	$P4_22$	$(422, \bar{1}\bar{1}\bar{1})$	19	$P4_22(00\gamma)$	$h000: h = 2n$
90.2			19	$P4_22(00\gamma)q00$	$00lm: m = 4n; h000: h = 2n$
90.3			19	$P4_22(00\gamma)s00$	$00lm: m = 2n; h000: h = 2n$
91.1	$P4_122$	$(422, \bar{1}\bar{1}\bar{1})$	19	$P4_122(00\gamma)$	$00lm: l = 4n$
91.2			20	$P4_122(\frac{1}{2}\frac{1}{2}\gamma)$	$00Lm: L = 4n$
92.1	$P4_12_12$	$(422, \bar{1}\bar{1}\bar{1})$	19	$P4_12_12(00\gamma)$	$00lm: l = 4n; h000: h = 2n$
93.1	$P4_222$	$(422, \bar{1}\bar{1}\bar{1})$	19	$P4_222(00\gamma)$	$00lm: l = 2n$
93.2			19	$P4_222(00\gamma)q00$	$00lm: 2l + m = 4n$
93.3			20	$P4_222(\frac{1}{2}\frac{1}{2}\gamma)$	$00Lm: L = 2n$
93.4			20	$P4_222(\frac{1}{2}\frac{1}{2}\gamma)q00$	$00Lm: 2L + m = 4n$
94.1	$P4_22_12$	$(422, \bar{1}\bar{1}\bar{1})$	19	$P4_22_12(00\gamma)$	$00lm: l = 2n; h000: h = 2n$
94.2			19	$P4_22_12(00\gamma)q00$	$00lm: 2l + m = 4n; h000: h = 2n$
95.1	$P4_322$	$(422, \bar{1}\bar{1}\bar{1})$	19	$P4_322(00\gamma)$	$00lm: l = 4n$
95.2			20	$P4_322(\frac{1}{2}\frac{1}{2}\gamma)$	$00Lm: L = 4n$
96.1	$P4_32_12$	$(422, \bar{1}\bar{1}\bar{1})$	19	$P4_32_12(00\gamma)$	$00lm: l = 4n; h000: h = 2n$
97.1	$I422$	$(422, \bar{1}\bar{1}\bar{1})$	21	$I422(00\gamma)$	
97.2			21	$I422(00\gamma)q00$	$00lm: m = 4n$
97.3			21	$I422(00\gamma)s00$	$00lm: m = 2n$
98.1	$I4_122$	$(422, \bar{1}\bar{1}\bar{1})$	21	$I4_122(00\gamma)$	$00lm: l = 4n$
98.2			21	$I4_122(00\gamma)q00$	$00lm: l + m = 4n$
99.1	$P4mm$	$(4mm, 111)$	19	$P4mm(00\gamma)$	
99.2			19	$P4mm(00\gamma)ss0$	$00lm: m = 2n; 0klm: m = 2n$
99.3			19	$P4mm(00\gamma)0ss$	$0klm: m = 2n; hhlm: m = 2n$
99.4			19	$P4mm(00\gamma)s0s$	$00lm: m = 2n; hhlm: m = 2n$
99.5			20	$P4mm(\frac{1}{2}\frac{1}{2}\gamma)$	
99.6			20	$P4mm(\frac{1}{2}\frac{1}{2}\gamma)0ss$	$0KLM: m = 2n; HHLm: m = 2n$
100.1	$P4bm$	$(4mm, 111)$	19	$P4bm(00\gamma)$	$0klm: k = 2n$
100.2			19	$P4bm(00\gamma)ss0$	$00lm: m = 2n; 0klm: m = 2n$
100.3			19	$P4bm(00\gamma)0ss$	$0klm: k + m = 2n; hhlm: m = 2n$
100.4			19	$P4bm(00\gamma)s0s$	$00lm: m = 2n; 0klm: k = 2n; hhlm: m = 2n$
100.5			20	$P4bm(\frac{1}{2}\frac{1}{2}\gamma)qq0$	$00Lm: m = 4n; KKLm: 2K + m = 4n$
100.6			20	$P4bm(\frac{1}{2}\frac{1}{2}\gamma)qqs$	$00Lm: m = 4n; KKLm: 2K + m = 4n;$ $HOLm: m = 2n$
101.1	$P4_2cm$	$(4mm, 111)$	19	$P4_2cm(00\gamma)$	$00lm: l = 2n; 0klm: l = 2n$
101.2			19	$P4_2cm(00\gamma)0ss$	$00lm: l = 2n; 0klm: l + m = 2n; hhlm: m = 2n$
101.3			20	$P4_2cm(\frac{1}{2}\frac{1}{2}\gamma)$	$00Lm: L = 2n; HHLm: L = 2n$
101.4			20	$P4_2cm(\frac{1}{2}\frac{1}{2}\gamma)0ss$	$00Lm: L = 2n; HHLm: L + m = 2n; HOLm: m = 2n$
102.1	$P4_2nm$	$(4mm, 111)$	19	$P4_2nm(00\gamma)$	$00lm: l = 2n; 0klm: k + l = 2n$
102.2			19	$P4_2nm(00\gamma)0ss$	$00lm: l = 2n; 0klm: k + l + m = 2n; hhlm: m = 2n$
102.3			20	$P4_2nm(\frac{1}{2}\frac{1}{2}\gamma)qq0$	$00Lm: 2L + m = 4n; HHLm: 2H + 2L + m = 4n$
102.4			20	$P4_2nm(\frac{1}{2}\frac{1}{2}\gamma)qqs$	$00Lm: 2L + m = 4n; HHLm: 2H + 2L + m = 4n;$ $HOLm: m = 2n$
103.1	$P4cc$	$(4mm, 111)$	19	$P4cc(00\gamma)$	$0klm: l = 2n; hhlm: l = 2n$
103.2			19	$P4cc(00\gamma)ss0$	$00lm: m = 2n; 0klm: l + m = 2n; hhlm: l = 2n$
103.3			20	$P4cc(\frac{1}{2}\frac{1}{2}\gamma)$	$HHLm: L = 2n; HOLm: L = 2n$
104.1	$P4nc$	$(4mm, 111)$	19	$P4nc(00\gamma)$	$0klm: k + l = 2n; hhlm: l = 2n$
104.2			19	$P4nc(00\gamma)ss0$	$00lm: m = 2n; 0klm: k + l + m = 2n; hhlm: l = 2n$
104.3			20	$P4nc(\frac{1}{2}\frac{1}{2}\gamma)qq0$	$00Lm: m = 4n; HHLm: 2H + 2L + m = 4n;$ $HOLm: L = 2n$
105.1	$P4_2mc$	$(4mm, 111)$	19	$P4_2mc(00\gamma)$	$00lm: l = 2n; hhlm: l = 2n$
105.2			19	$P4_2mc(00\gamma)ss0$	$00lm: l + m = 2n; 0klm: m = 2n; hhlm: l = 2n$
105.3			20	$P4_2mc(\frac{1}{2}\frac{1}{2}\gamma)$	$00Lm: L = 2n; HOLm: L = 2n$
106.1	$P4_2bc$	$(4mm, 111)$	19	$P4_2bc(00\gamma)$	$00lm: l = 2n; 0klm: k = 2n; hhlm: l = 2n$
106.2			19	$P4_2bc(00\gamma)ss0$	$00lm: l + m = 2n; 0klm: k + m = 2n; hhlm: l = 2n$
106.3			20	$P4_2bc(\frac{1}{2}\frac{1}{2}\gamma)qq0$	$00Lm: 2L + m = 4n; HHLm: 2H + m = 4n;$ $HOLm: L = 2n$
107.1	$I4mm$	$(4mm, 111)$	21	$I4mm(00\gamma)$	
107.2			21	$I4mm(00\gamma)ss0$	$00lm: m = 2n; 0klm: m = 2n$
107.3			21	$I4mm(00\gamma)0ss$	$0klm: m = 2n; hhlm: m = 2n$

9.8. INCOMMENSURATE AND COMMENSURATE MODULATED STRUCTURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions				
107.4	$I4cm$	$(4mm, 111)$	21	$I4mm(00\gamma)s0s$	$00lm: m = 2n; hhl m: m = 2n$				
108.1			21	$I4cm(00\gamma)$	$0klm: l = 2n$				
108.2			21	$I4cm(00\gamma)ss0$	$00lm: m = 2n; 0klm: l + m = 2n$				
108.3			21	$I4cm(00\gamma)0ss$	$0klm: l + m = 2n; hhl m: m = 2n$				
108.4	$I4_1md$	$(4mm, 111)$	21	$I4cm(00\gamma)s0s$	$00lm: m = 2n; 0klm: l = 2n; hhl m: m = 2n$				
109.1			21	$I4_1md(00\gamma)$	$00lm: l = 4n; hhl m: 2h + l = 4n$				
109.2	$I4_1cd$	$(4mm, 111)$	21	$I4_1md(00\gamma)ss0$	$00lm: l + 2m = 4n; 0klm: m = 2n; hhl m: 2h + l = 4n$				
110.1			21	$I4_1cd(00\gamma)$	$00lm: l = 4n; 0klm: l = 2n; hhl m: 2h + l = 4n$				
110.2			21	$I4_1cd(00\gamma)ss0$	$00lm: l + 2m = 4n; 0klm: l + m = 2n; hhl m: 2h + l = 4n$				
111.1	$P\bar{4}2m$	$(\bar{4}2m, \bar{1}\bar{1}1)$	19	$P\bar{4}2m(00\gamma)$	$hhl m: m = 2n$				
111.2			19	$P\bar{4}2m(00\gamma)00s$					
111.3	$P\bar{4}2c$	$(\bar{4}2m, \bar{1}\bar{1}1)$	20	$P\bar{4}2m(\frac{1}{2}\gamma)$	$HOLm: m = 2n$				
111.4			20	$P\bar{4}2m(\frac{1}{2}\gamma)00s$					
112.1			19	$P\bar{4}2c(00\gamma)$		$hhl m: l = 2n$			
112.2			20	$P\bar{4}2c(\frac{1}{2}\gamma)$		$HOLm: L = 2n$			
113.1	$P\bar{4}2_1m$	$(\bar{4}2m, \bar{1}\bar{1}1)$	19	$P\bar{4}2_1m(00\gamma)$	$h000: h = 2n$				
113.2			19	$P\bar{4}2_1m(00\gamma)00s$	$h000: h = 2n; hhl m: m = 2n$				
114.1	$P\bar{4}2_1c$	$(\bar{4}2m, \bar{1}\bar{1}1)$	19	$P\bar{4}2_1c(00\gamma)$	$h000: h = 2n; hhl m: l = 2n$				
115.1	$P\bar{4}m2$	$(\bar{4}m2, \bar{1}\bar{1}1)$	19	$P\bar{4}m2(00\gamma)$	$0klm: m = 2n$				
115.2			19	$P\bar{4}m2(00\gamma)0s0$					
115.3	$P\bar{4}c2$	$(\bar{4}m2, \bar{1}\bar{1}1)$	20	$P\bar{4}m2(\frac{1}{2}\gamma)$	$0klm: l = 2n$				
116.1			19	$P\bar{4}c2(00\gamma)$					
116.2			20	$P\bar{4}c2(\frac{1}{2}\gamma)$		$HHLm: L = 2n$			
117.1			19	$P\bar{4}b2(00\gamma)$		$0klm: k = 2n$			
117.2	$P\bar{4}b2$	$(\bar{4}m2, \bar{1}\bar{1}1)$	19	$P\bar{4}b2(00\gamma)0s0$	$0klm: k + m = 2n$				
117.3			20	$P\bar{4}b2(\frac{1}{2}\gamma)0q0$	$HHLm: 2H + m = 4n$				
118.1	$P\bar{4}n2$	$(\bar{4}m2, \bar{1}\bar{1}1)$	19	$P\bar{4}n2(00\gamma)$	$0klm: k + l = 2n$				
118.2			20	$P\bar{4}n2(\frac{1}{2}\gamma)0q0$	$HHLm: 2H + 2L + m = 4n$				
119.1	$I\bar{4}m2$	$(\bar{4}m2, \bar{1}\bar{1}1)$	21	$I\bar{4}m2(00\gamma)$	$0klm: m = 2n$				
119.2			21	$I\bar{4}m2(00\gamma)0s0$					
120.1	$I\bar{4}c2$	$(\bar{4}m2, \bar{1}\bar{1}1)$	21	$I\bar{4}c2(00\gamma)$	$0klm: l = 2n$				
120.2			21	$I\bar{4}c2(00\gamma)0s0$	$0klm: l + m = 2n$				
121.1	$I\bar{4}2m$	$(\bar{4}2m, \bar{1}\bar{1}1)$	21	$I\bar{4}2m(00\gamma)$	$hhl m: m = 2n$				
121.2			21	$I\bar{4}2m(00\gamma)00s$					
122.1	$I\bar{4}2d$	$(\bar{4}2m, \bar{1}\bar{1}1)$	21	$I\bar{4}2d(00\gamma)$	$hhl m: 2h + l = 4n$				
123.1	$P4/mmm$	$(4/mmm, \bar{1}\bar{1}\bar{1}1)$	19	$P4/mmm(00\gamma)$	$00lm: m = 2n; 0klm: m = 2n$				
123.2			19	$P4/mmm(00\gamma)s0s0$		$0klm: m = 2n; hhl m: m = 2n$			
123.3			19	$P4/mmm(00\gamma)00ss$		$00lm: m = 2n; hhl m: m = 2n$			
123.4			19	$P4/mmm(00\gamma)s00s$		$00lm: m = 2n; hhl m: m = 2n$			
123.5			20	$P4/mmm(\frac{1}{2}\gamma)$		$HHLm: m = 2n; HOLm: m = 2n$			
123.6			20	$P4/mmm(\frac{1}{2}\gamma)00ss$					
124.1			$P4/mcc$	$(4/mmm, \bar{1}\bar{1}\bar{1}1)$			19	$P4/mcc(00\gamma)$	$0klm: l = 2n; hhl m: l = 2n$
124.2							19	$P4/mcc(00\gamma)s0s0$	$00lm: m = 2n; 0klm: l + m = 2n; hhl m: l = 2n$
124.3			$P4/nbm$	$(4/mmm, \bar{1}\bar{1}\bar{1}1)$			20	$P4/mcc(\frac{1}{2}\gamma)$	$HHLm: L = 2n; HOLm: L = 2n$
125.1							19	$P4/nbm(00\gamma)$	$hk00: h + k = 2n; 0klm: k = 2n$
125.2							19	$P4/nbm(00\gamma)s0s0$	$00lm: m = 2n; hk00: h + k = 2n; 0klm: k + m = 2n$
125.3			$P4/nbm$	$(4/mmm, \bar{1}\bar{1}\bar{1}1)$			19	$P4/nbm(00\gamma)00ss$	$hk00: h + k = 2n; 0klm: k + m = 2n; hhl m: m = 2n$
125.4	19	$P4/nbm(00\gamma)s00s$			$00lm: m = 2n; hk00: h + k = 2n; 0klm: k = 2n; hhl m: m = 2n$				
125.5	$P4/nbm$	$(4/mmm, \bar{1}\bar{1}\bar{1}1)$	20	$P4/nbm(\frac{1}{2}\gamma)q0q0$	$00Lm: m = 4n; HK00: H = 2n, K = 2n; HHLm: 2H + m = 4n$				
125.6			20	$P4/nbm(\frac{1}{2}\gamma)q0qs$	$00Lm: m = 4n; HK00: H = 2n, K = 2n; HHLm: 2H + m = 4n; HOLm: m = 2n$				
126.1	$P4/nnc$	$(4/mmm, \bar{1}\bar{1}\bar{1}1)$	19	$P4/nnc(00\gamma)$	$hk00: h + k = 2n; h0lm: h + l = 2n; hhl m: l = 2n$				
126.2			19	$P4/nnc(00\gamma)s0s0$	$00lm: m = 2n; hk00: h + k = 2n; h0lm: h + l + m = 2n; hhl m: l = 2n$				
126.3	$P4/nbm$	$(4/mmm, \bar{1}\bar{1}\bar{1}1)$	20	$P4/nnc(\frac{1}{2}\gamma)q0q0$	$00Lm: m = 4n; HK00: H = 2n, K = 2n; HHLm: 2H + 2L + m = 4n; HOLm: L = 2n$				
127.1			19	$P4/nbm(00\gamma)$	$0klm: k = 2n$				
127.2			19	$P4/nbm(00\gamma)s0s0$	$00lm: m = 2n; 0klm: k + m = 2n$				
127.3	$P4/nmc$	$(4/mmm, \bar{1}\bar{1}\bar{1}1)$	19	$P4/nbm(00\gamma)00ss$	$0klm: k + m = 2n; hhl m: m = 2n$				
127.4			19	$P4/nbm(00\gamma)s00s$	$00lm: m = 2n; 0klm: k = 2n; hhl m: m = 2n$				
128.1	$P4/nmc$	$(4/mmm, \bar{1}\bar{1}\bar{1}1)$	19	$P4/nmc(00\gamma)$	$0klm: k + l = 2n; hhl m: l = 2n$				
128.2			19	$P4/nmc(00\gamma)s0s0$	$00lm: m = 2n; 0klm: k + l + m = 2n; hhl m: l = 2n$				
129.1	$P4/nmm$	$(4/mmm, \bar{1}\bar{1}\bar{1}1)$	19	$P4/nmm(00\gamma)$	$hk00: h + k = 2n$				

9. BASIC STRUCTURAL FEATURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions
129.2	$P4/ncc$	$(4/mmm, 1\bar{1}11)$	19	$P4/nmm(00\gamma)s0s0$	$00lm: m = 2n; hk00: h + k = 2n; Oklm: m = 2n$
129.3			19	$P4/nmm(00\gamma)00ss$	$hk00: h + k = 2n; Oklm: m = 2n; hhlml: m = 2n$
129.4			19	$P4/nmm(00\gamma)s00s$	$00lm: m = 2n; hk00: h + k = 2n; hhlml: m = 2n$
130.1			19	$P4/ncc(00\gamma)$	$hk00: h + k = 2n; Oklm: l = 2n; hhlml: l = 2n$
130.2			19	$P4/ncc(00\gamma)s0s0$	$00lm: m = 2n; hk00: h + k = 2n; Oklm: l + m = 2n; hhlml: l = 2n$
131.1	$P4_2/mmc$	$(4/mmm, 1\bar{1}11)$	19	$P4_2/mmc(00\gamma)$	$00lm: l = 2n; hhlml: l = 2n$
131.2			19	$P4_2/mmc(00\gamma)s0s0$	$00lm: l + m = 2n; Oklm: m = 2n; hhlml: l = 2n$
131.3	$P4_2/mcm$	$(4/mmm, 1\bar{1}11)$	20	$P4_2/mmc(\frac{1}{2}\gamma)$	$00Lm: L = 2n; HOLm: L = 2n$
132.1			19	$P4_2/mcm(00\gamma)$	$00lm: l = 2n; Oklm: l = 2n$
132.2			19	$P4_2/mcm(00\gamma)00ss$	$00lm: l = 2n; Oklm: l + m = 2n; hhlml: m = 2n$
132.3			20	$P4_2/mcm(\frac{1}{2}\gamma)$	$00Lm: L = 2n; HHLm: L = 2n$
132.4			20	$P4_2/mcm(\frac{1}{2}\gamma)00ss$	$00Lm: L = 2n; HHLm: L + m = 2n; HOLm: m = 2n$
133.1	$P4_2/nbc$	$(4/mmm, 1\bar{1}11)$	19	$P4_2/nbc(00\gamma)$	$00lm: l = 2n; hk00: h + k = 2n; Oklm: k = 2n; hhlml: l = 2n$
133.2			19	$P4_2/nbc(00\gamma)s0s0$	$00lm: l + m = 2n; hk00: h + k = 2n; Oklm: k + m = 2n; hhlml: l = 2n$
133.3	$P4_2/nnm$	$(4/mmm, 1\bar{1}11)$	20	$P4_2/nbc(\frac{1}{2}\gamma)q0q0$	$00Lm: 2L + m = 4n; HK00: H = 2n, K = 2n; HHLm: 2H + m = 4n; HOLm: L = 2n$
134.1			19	$P4_2/nnm(00\gamma)$	$00lm: l = 2n; hk00: h + k = 2n; Oklm: k + l = 2n$
134.2			19	$P4_2/nnm(00\gamma)00ss$	$00lm: l = 2n; hk00: h + k = 2n; Oklm: k + l + m = 2n; hhlml: m = 2n$
134.3			20	$P4_2/nnm(\frac{1}{2}\gamma)q0q0$	$00Lm: 2L + m = 4n; HK00: H = 2n, K = 2n; HHLm: 2H + 2L + m = 4n$
134.4	20	$P4_2/nnm(\frac{1}{2}\gamma)q0qs$	$00Lm: 2L + m = 4n; HK00: H + K = 2n; HHLm: 2H + 2L + m = 4n; HOLm: m = 2n$		
135.1	$P4_2/mbc$	$(4/mmm, 1\bar{1}11)$	19	$P4_2/mbc(00\gamma)$	$00lm: l = 2n; Oklm: k = 2n; hhlml: l = 2n$
135.2			19	$P4_2/mbc(00\gamma)s0s0$	$00lm: l + m = 2n; Oklm: k + m = 2n; hhlml: l = 2n$
136.1	$P4_2/mnm$	$(4/mmm, 1\bar{1}11)$	19	$P4_2/mnm(00\gamma)$	$00lm: l = 2n; Oklm: k + l = 2n$
136.2			19	$P4_2/mnm(00\gamma)00ss$	$00lm: l = 2n; Oklm: k + l + m = 2n; hhlml: m = 2n$
137.1	$P4_2/nmc$	$(4/mmm, 1\bar{1}11)$	19	$P4_2/nmc(00\gamma)$	$00lm: l = 2n; hk00: h + k = 2n; hhlml: l = 2n$
137.2			19	$P4_2/nmc(00\gamma)s0s0$	$00lm: l + m = 2n; hk00: h + k = 2n; Oklm: m = 2n; hhlml: l = 2n$
138.1	$P4_2/ncm$	$(4/mmm, 1\bar{1}11)$	19	$P4_2/ncm(00\gamma)$	$00lm: l = 2n; hk00: h + k = 2n; Oklm: l = 2n$
138.2			19	$P4_2/ncm(00\gamma)00ss$	$00lm: l = 2n; hk00: h + k = 2n; Oklm: l + m = 2n; hhlml: m = 2n$
139.1	$I4/mmm$	$(4/mmm, 1\bar{1}11)$	21	$I4/mmm(00\gamma)$	$00lm: m = 2n; Oklm: m = 2n$
139.2			21	$I4/mmm(00\gamma)s0s0$	$Oklm: m = 2n; hhlml: m = 2n$
139.3			21	$I4/mmm(00\gamma)00ss$	$00lm: m = 2n; hhlml: m = 2n$
139.4			21	$I4/mmm(00\gamma)s00s$	$Oklm: l = 2n$
140.1			$I4/mcm$	$(4/mmm, 1\bar{1}11)$	21
140.2	21	$I4/mcm(00\gamma)s0s0$			$Oklm: l + m = 2n; hhlml: m = 2n$
140.3	21	$I4/mcm(00\gamma)00ss$			$00lm: m = 2n; Oklm: l = 2n; hhlml: m = 2n$
140.4	21	$I4/mcm(00\gamma)s00s$			$00lm: l = 4n; hk00: h = 2n; hhlml: 2h + l = 4n$
141.1	$I4_1/amd$	$(4/mmm, 1\bar{1}11)$	21	$I4_1/amd(00\gamma)$	$00lm: l + 2m = 4n; hk00: h = 2n; Oklm: m = 2n; hhlml: 2h + l = 4n$
141.2			21	$I4_1/amd(00\gamma)s0s0$	$00lm: l + 2m = 4n; hk00: h = 2n; Oklm: m = 2n; hhlml: 2h + l = 4n$
142.1	$I4_1/acd$	$(4/mmm, 1\bar{1}11)$	21	$I4_1/acd(00\gamma)$	$00lm: l = 4n; hk00: h = 2n; Oklm: l = 2n; hhlml: 2h + l = 4n$
142.2			21	$I4_1/acd(00\gamma)s0s0$	$00lm: l + 2m = 4n; hk00: h = 2n; Oklm: l + m = 2n; hhlml: 2h + l = 4n$
143.1	$P3$	$(3, 1)$	23	$P3(\frac{1}{3}\gamma)$	$00lm: m = 3n$
143.2			24	$P3(00\gamma)$	$00Lm: L = 3n$
143.3	$P3_1$	$(3, 1)$	24	$P3(00\gamma)t$	$00lm: l = 3n$
144.1			23	$P3_1(\frac{1}{3}\gamma)$	$00Lm: L = 3n$
144.2	$P3_2$	$(3, 1)$	24	$P3_1(00\gamma)$	$00lm: l = 3n$
145.1			23	$P3_2(\frac{1}{3}\gamma)$	$00Lm: L = 3n$
145.2	$R3$	$(3, 1)$	24	$P3_2(00\gamma)$	$00lm: l = 3n$
146.1			22	$R3(00\gamma)$	
146.2	$P\bar{3}$	$(\bar{3}, \bar{1})$	22	$R3(00\gamma)t$	$00lm: m = 3n$
147.1			23	$P\bar{3}(\frac{1}{3}\gamma)$	
147.2	$R\bar{3}$	$(\bar{3}, \bar{1})$	24	$P\bar{3}(00\gamma)$	
148.1			22	$R\bar{3}(00\gamma)$	
149.1	$P312$	$(312, 11\bar{1})$	23	$P312(\frac{1}{3}\gamma)$	
149.2			24	$P312(00\gamma)$	

9.8. INCOMMENSURATE AND COMMENSURATE MODULATED STRUCTURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions
149.3			24	$P312(00\gamma)t00$	$00lm: m = 3n$
150.1	$P321$	$(321, \bar{1}\bar{1}\bar{1})$	24	$P321(00\gamma)$	
150.2			24	$P321(00\gamma)t00$	$00lm: m = 3n$
151.1	$P3_112$	$(312, 11\bar{1})$	23	$P3_112(\frac{1}{3}\gamma)$	$00Lm: L = 3n$
151.2			24	$P3_112(00\gamma)$	$00lm: l = 3n$
152.1	$P3_121$	$(321, \bar{1}\bar{1}\bar{1})$	24	$P3_121(00\gamma)$	$00lm: l = 3n$
153.1	$P3_212$	$(312, 11\bar{1})$	23	$P3_212(\frac{1}{3}\gamma)$	
153.2			24	$P3_212(00\gamma)$	$00lm: l = 3n$
154.1	$P3_221$	$(321, \bar{1}\bar{1}\bar{1})$	24	$P3_221(00\gamma)$	$00lm: l = 3n$
155.1	$R32$	$(32, \bar{1}\bar{1})$	22	$R32(00\gamma)$	
155.2			22	$R32(00\gamma)t0$	$00lm: m = 3n$
156.1	$P3m1$	$(3m1, 111)$	24	$P3m1(00\gamma)$	
156.2			24	$P3m1(00\gamma)0s0$	$0klm: m = 2n$
157.1	$P31m$	$(31m, 111)$	23	$P31m(\frac{1}{3}\gamma)$	
157.2			23	$P31m(\frac{1}{3}\gamma)00s$	$H\bar{H}Lm: m = 2n$
157.3			24	$P31m(00\gamma)$	
157.4			24	$P31m(00\gamma)00s$	$hhlm: m = 2n$
158.1	$P3c1$	$(3m1, 111)$	24	$P3c1(00\gamma)$	$0klm: l = 2n$
159.1	$P31c$	$(31m, 111)$	23	$P31c(\frac{1}{3}\gamma)$	$H\bar{H}Lm: L = 2n$
159.2			24	$P31c(00\gamma)$	$hhlm: l = 2n$
160.1	$R3m$	$(3m, 11)$	22	$R3m(00\gamma)$	
160.2			22	$R3m(00\gamma)0s$	$hhlm: m = 2n$
161.1	$R3c$	$(3m, 11)$	22	$R3c(00\gamma)$	$hhlm: l = 2n$
162.1	$P\bar{3}1m$	$(\bar{3}1m, \bar{1}\bar{1}\bar{1})$	23	$P\bar{3}1m(\frac{1}{3}\gamma)$	
162.2			23	$P\bar{3}1m(\frac{1}{3}\gamma)00s$	$H\bar{H}Lm: m = 2n$
162.3			24	$P\bar{3}1m(00\gamma)$	
162.4			24	$P\bar{3}1m(00\gamma)00s$	$hhlm: m = 2n$
163.1	$P\bar{3}1c$	$(\bar{3}1m, \bar{1}\bar{1}\bar{1})$	23	$P\bar{3}1c(\frac{1}{3}\gamma)$	$H\bar{H}Lm: L = 2n$
163.2			24	$P\bar{3}1c(00\gamma)$	$hhlm: l = 2n$
164.1	$P\bar{3}m1$	$(\bar{3}m1, \bar{1}\bar{1}\bar{1})$	24	$P\bar{3}m1(00\gamma)$	
164.2			24	$P\bar{3}m1(00\gamma)0s0$	$0klm: m = 2n$
165.1	$P\bar{3}c1$	$(\bar{3}m1, \bar{1}\bar{1}\bar{1})$	24	$P\bar{3}c1(00\gamma)$	$0klm: l = 2n$
166.1	$R\bar{3}m$	$(\bar{3}m, \bar{1}\bar{1})$	22	$R\bar{3}m(00\gamma)$	
166.2			22	$R\bar{3}m(00\gamma)0s$	$hhlm: m = 2n$
167.1	$R\bar{3}c$	$(\bar{3}m, \bar{1}\bar{1})$	22	$R\bar{3}c(00\gamma)$	$hhlm: l = 2n$
168.1	$P6$	$(6, 1)$	24	$P6(00\gamma)$	
168.2			24	$P6(00\gamma)h$	$00lm: m = 6n$
168.3			24	$P6(00\gamma)t$	$00lm: m = 3n$
168.4			24	$P6(00\gamma)s$	$00lm: m = 2n$
169.1	$P6_1$	$(6, 1)$	24	$P6_1(00\gamma)$	$00lm: l = 6n$
170.1	$P6_5$	$(6, 1)$	24	$P6_5(00\gamma)$	$00lm: l = 6n$
171.1	$P6_2$	$(6, 1)$	24	$P6_2(00\gamma)$	$00lm: l = 3n$
171.2			24	$P6_2(00\gamma)h$	$00lm: 2l + m = 6n$
172.1	$P6_4$	$(6, 1)$	24	$P6_4(00\gamma)$	$00lm: l = 3n$
172.2			24	$P6_4(00\gamma)h$	$00lm: 2l + m = 6n$
173.1	$P6_3$	$(6, 1)$	24	$P6_3(00\gamma)$	$00lm: l = 2n$
173.2			24	$P6_3(00\gamma)h$	$00lm: 3l + m = 6n$
174.1	$P\bar{6}$	$(\bar{6}, \bar{1})$	24	$P\bar{6}(00\gamma)$	
175.1	$P6/m$	$(6/m, \bar{1}\bar{1})$	24	$P6/m(00\gamma)$	
175.2			24	$P6/m(00\gamma)s0$	$00lm: m = 2n$
176.1	$P6_3/m$	$(6/m, \bar{1}\bar{1})$	24	$P6_3/m(00\gamma)$	$00lm: l = 2n$
177.1	$P622$	$(622, \bar{1}\bar{1}\bar{1})$	24	$P622(00\gamma)$	
177.2			24	$P622(00\gamma)h00$	$00lm: m = 6n$
177.3			24	$P622(00\gamma)t00$	$00lm: m = 3n$
177.4			24	$P622(00\gamma)s00$	$00lm: m = 2n$
178.1	$P6_122$	$(622, \bar{1}\bar{1}\bar{1})$	24	$P6_122(00\gamma)$	$00lm: l = 6n$
179.1	$P6_522$	$(622, \bar{1}\bar{1}\bar{1})$	24	$P6_522(00\gamma)$	$00lm: l = 6n$
180.1	$P6_222$	$(622, \bar{1}\bar{1}\bar{1})$	24	$P6_222(00\gamma)$	$00lm: l = 3n$
180.2			24	$P6_222(00\gamma)h00$	$00lm: 2l + m = 6n$
181.1	$P6_422$	$(622, \bar{1}\bar{1}\bar{1})$	24	$P6_422(00\gamma)$	$00lm: l = 3n$
181.2			24	$P6_422(00\gamma)h00$	$00lm: 2l + m = 6n$
182.1	$P6_322$	$(622, \bar{1}\bar{1}\bar{1})$	24	$P6_322(00\gamma)$	
182.2			24	$P6_322(00\gamma)h00$	$00lm: 3l + m = 6n$
183.1	$P6mm$	$(6mm, 111)$	24	$P6mm(00\gamma)$	
183.2			24	$P6mm(00\gamma)ss0$	$00lm: m = 2n; 0klm: m = 2n$

9. BASIC STRUCTURAL FEATURES

Table 9.8.3.5. (3 + 1)-Dimensional superspace groups (cont.)

No.	Basic space group	Point group K_s	Bravais class No.	Group symbol	Special reflection conditions
183.3	$P6cc$	$(6mm, 111)$	24	$P6mm(00\gamma)0ss$	$0klm: m = 2n; hhl m: m = 2n$
183.4			24	$P6mm(00\gamma)s0s$	$00lm: m = 2n; hhl m: m = 2n$
184.1			24	$P6cc(00\gamma)$	$0klm: l = 2n; hhl m: l = 2n$
184.2			24	$P6cc(00\gamma)s0s$	$00lm: m = 2n; 0klm: l = 2n; hhl m: l + m = 2n$
185.1	$P6_3cm$	$(6mm, 111)$	24	$P6_3cm(00\gamma)$	$00lm: l = 2n; 0klm: l = 2n$
185.2			24	$P6_3cm(00\gamma)0ss$	$00lm: l = 2n; 0klm: l + m = 2n; hhl m: m = 2n$
186.1	$P6_3mc$	$(6mm, 111)$	24	$P6_3mc(00\gamma)$	$00lm: l = 2n; hhl m: l = 2n$
186.2			24	$P6_3mc(00\gamma)0ss$	$00lm: l = 2n; 0klm: m = 2n; hhl m: l + m = 2n$
187.1	$P\bar{6}m2$	$(\bar{6}m2, \bar{1}1\bar{1})$	24	$P\bar{6}m2(00\gamma)$	
187.2			24	$P\bar{6}m2(00\gamma)0s0$	$0klm: m = 2n$
188.1	$P\bar{6}c2$	$(\bar{6}m2, \bar{1}1\bar{1})$	24	$P\bar{6}c2(00\gamma)$	$0klm: l = 2n$
189.1			24	$P\bar{6}2m(00\gamma)$	
189.2	$P\bar{6}2c$	$(\bar{6}2m, \bar{1}1\bar{1})$	24	$P\bar{6}2m(00\gamma)00s$	$hhl m: m = 2n$
190.1			24	$P\bar{6}2c(00\gamma)$	$hhl m: l = 2n$
191.1	$P6/mmm$	$(6/mmm, \bar{1}\bar{1}11)$	24	$P6/mmm(00\gamma)$	
191.2			24	$P6/mmm(00\gamma)s0s0$	$00lm: m = 2n; 0klm: m = 2n$
191.3			24	$P6/mmm(00\gamma)00ss$	$0klm: m = 2n; hhl m: m = 2n$
191.4			24	$P6/mmm(00\gamma)s00s$	$00lm: m = 2n; hhl m: m = 2n$
192.1	$P6/mcc$	$(6/mmm, \bar{1}\bar{1}11)$	24	$P6/mcc(00\gamma)$	$0klm: l = 2n; hhl m: l = 2n$
192.2			24	$P6/mcc(00\gamma)s00s$	$00lm: m = 2n; 0klm: l = 2n; hhl m: l + m = 2n$
193.1	$P6_3/mcm$	$(6/mmm, \bar{1}\bar{1}11)$	24	$P6_3/mcm(00\gamma)$	$00lm: l = 2n; 0klm: l = 2n$
193.2			24	$P6_3/mcm(00\gamma)00ss$	$00lm: l = 2n; 0klm: l + m = 2n; hhl m: m = 2n$
194.1	$P6_3/mmc$	$(6/mmm, \bar{1}\bar{1}11)$	24	$P6_3/mmc(00\gamma)$	$00lm: l = 2n; hhl m: l = 2n$
194.2			24	$P6_3/mmc(00\gamma)00ss$	$00lm: l = 2n; 0klm: m = 2n; hhl m: l + m = 2n$

primitive translations in the (3 + 1)-dimensional space group, just as is the case for glide planes and screw axes in three dimensions.

Special reflection conditions can be derived from transformation properties of the structure factor under symmetry operations. Transforming the geometric structure factor by an element $g_s = (\{R|\mathbf{v}\}, \{R_I|v_I\})$, one obtains

$$S_{\mathbf{H}} = S_{R^{-1}\mathbf{H}} \exp[-2\pi i(\mathbf{H} \cdot \mathbf{v} + H_I \cdot v_I)]. \quad (9.8.3.10)$$

Therefore, if $R\mathbf{H} = \mathbf{H}$, the corresponding structure factor vanishes unless $\mathbf{H} \cdot \mathbf{v} + H_I \cdot v_I$ is an integer.

The form of such a reflection condition in terms of allowed or forbidden sets of indices depends on the basis chosen. When a lattice basis is chosen, one has

$$H_s = (\mathbf{H}, H_I) = \sum_{i=1}^4 h_i \mathbf{a}_{si}^*, \quad (9.8.3.11)$$

$$v_s = (\mathbf{v}, v_I) + \sum_{i=1}^4 v_i \mathbf{a}_{si}. \quad (9.8.3.12)$$

Then the reflection condition becomes

$$H_s \cdot v_s = \sum_{i=1}^4 h_i v_i = \text{integer} \quad \text{for } R\mathbf{H} = \mathbf{H}. \quad (9.8.3.13)$$

In terms of external and internal shift components, the reflection condition can be written as

$$H_s \cdot v_s = \mathbf{H} \cdot \mathbf{v} + H_I \cdot v_I = \mathbf{H} \cdot \mathbf{v} + m v_I = \text{integer for } R\mathbf{H} = \mathbf{H}. \quad (9.8.3.14)$$

With $\mathbf{H} = \mathbf{K} + m\mathbf{q}$ and $v_I = \delta - \mathbf{q} \cdot \mathbf{v}$, (9.8.3.14) gives

$$\mathbf{K} \cdot \mathbf{v} + m\delta = \text{integer} \quad \text{for } R\mathbf{H} = \mathbf{H}. \quad (9.8.3.15)$$

For $\mathbf{v} = v_1 \mathbf{a} + v_2 \mathbf{b} + v_3 \mathbf{c}$ and $\mathbf{K} = h\mathbf{a}^* + k\mathbf{b}^* + l\mathbf{c}^*$, (9.8.3.15) takes the form (9.8.3.13):

$$h v_1 + k v_2 + l v_3 + m\delta = \text{integer} \quad \text{for } R\mathbf{H} = \mathbf{H}. \quad (9.8.3.16)$$

When the modulation wavevector has a rational part, one can choose another basis (Subsection 9.8.2.1) such that $\mathbf{K}' = \mathbf{K} + m\mathbf{q}'$ has integer coefficients:

$$\mathbf{H} = \mathbf{K}' + m\mathbf{q}' = H\mathbf{a}_c^* + K\mathbf{b}_c^* + L\mathbf{c}_c^* + m\mathbf{q}'.$$

Then, (9.8.3.15) with $\tau = \delta - \mathbf{q}' \cdot \mathbf{v}$ becomes

$$\mathbf{K}' \cdot \mathbf{v} + m\tau = \text{integer} \quad \text{for } R\mathbf{H} = \mathbf{H} \quad (9.8.3.17)$$

and (9.8.3.16) transforms into

$$H v'_1 + K v'_2 + L v'_3 + m\tau = \text{integer} \quad \text{for } R\mathbf{H} = \mathbf{H}, \quad (9.8.3.18)$$

in which $v'_1, v'_2,$ and v'_3 are the components of \mathbf{v} with respect to the basis $\mathbf{a}_c, \mathbf{b}_c,$ and \mathbf{c}_c .

As an example, consider a (3 + 1)-dimensional space-group transformation with R a mirror perpendicular to the x axis, $\varepsilon = 1, \mathbf{v} = \frac{1}{2}\mathbf{b}$, and $\tau = \frac{1}{4}$ with \mathbf{b} orthogonal to \mathbf{a} . The modulation wavevector is supposed to be $(\frac{1}{2}\frac{\gamma}{2})$. Then $\delta = \frac{1}{4} + \mathbf{q}' \cdot \mathbf{v} = \frac{1}{2}$. The vectors \mathbf{H} left invariant by R satisfy the relation $2h + m = 0$. For such a vector, the reflection condition becomes

$$\mathbf{K} \cdot \mathbf{v} + m\delta = \frac{1}{2}\mathbf{K} \cdot \mathbf{b} + \frac{1}{2}m = \frac{k+m}{2} = \text{integer}, \quad \text{or } k+m = 2n.$$

For the basis $\frac{1}{2}(\mathbf{a}^* + \mathbf{b}^*), \frac{1}{2}(\mathbf{a}^* - \mathbf{b}^*), \mathbf{c}^*$, the rational part of the wavevector vanishes. The indices with respect to this basis are $H = h + k + m, K = h - k, L = l$ and m . The condition now becomes

$$\mathbf{K}' \cdot \mathbf{v} + m\tau = \frac{H - K + m}{4} = \text{integer},$$

$$\text{or } H - K + m = 4n, \quad \text{for } K = -H.$$

Of course, both calculations give the same result: $k + m = 2n$ for $h, k, l, -2h$ and $H - K + m = 4n$ for $H, -H, L, m$.